



Set of Exercises - 01

Chapter 01: The atomic nucleus

Useful data: $1uc^2 = 931.5[MeV]$; $m_p = 1.0073u$; $m_n = 1.0087u$; $R_0 = 1.2 \times 10^{-15}fm$;
 $a_V = 14.64MeV$, $a_S = 14.08MeV$, $a_C = 0.64MeV$, $a_A = 21.07MeV$, $a_P = 11.54MeV$ (Benzaid, NST 2020)

Exercise 01:

By considering the nucleus as a spherical volume with a radius is given as a function of mass number: $R = R_0A^{1/3}$

Find the density of the $^{12}_6C$ nucleus.

Exercise 02:

Find the repulsive electric force on a proton whose center is $2.4 fm$ from the center of another proton. Assume the protons are uniformly charged spheres of positive charge.

Exercise 03:

(a) Find the energy difference between the spin-up and spin-down states of a proton in a magnetic field of $B = 1.000 T$ (which is quite strong).

(b) What is the Larmor frequency of a proton in this field?

Exercise 04:

(a) To penetrate the Coulomb barrier of a light nucleus, what should be the energy order of magnitude for the incoming proton.

Take the H nucleus as target and the characteristic distance $r = 1fm$.

(b) What will be this energy in the case of 2_2He or 3_3Li as a target?

Exercise 05:

The binding energy of the neon isotope $^{20}_{10}Ne$ is $160.647 MeV$. Find its atomic mass

Exercise 06:

(a) Find the energy needed to remove a neutron from the nucleus of the calcium isotope $^{42}_{20}Ca$.

(b) Find the energy needed to remove a proton from this nucleus.

(c) Why are these energies different?

$M(20, 42) = 41.958622$, $M(20, 41) = 40.962278$,

$M(19, 41) = 40.961825$

Exercise 07:

Find the energy needed to remove a neutron, proton, or an α particle from the following isotopes: $^{238}_{92}U$, $^{232}_{90}Th$

$M(92, 238) = 238.050786$, $M(91, 237) = 237.051023$
 $M(92, 237) = 237.048728$, $M(90, 234) = 234.043599$
 $M(90, 232) = 232.038053$, $M(89, 231) = 231.038393$
 $M(90, 231) = 231.036302$, $M(88, 228) = 228.031068$

Exercise 08:

(a) The atomic mass of the zinc isotope $^{64}_{30}Zn$ is $63.929 u$. Compare its binding energy with the Theoretical prediction:

$$E_B^{SEMF}(Z, A) = a_V A - a_S A^{2/3} - a_C \frac{Z(Z-1)}{A^{1/3}} - a_A \frac{(A-2Z)^2}{A} + a_P \frac{\delta}{A^{3/4}}$$

(b) Do the same for the isotopes given in Ex.06.

Exercise 09:

Isobars are nuclides that have the same mass number A. Derive a formula for the atomic number of the most stable isobar of a given A and use it to find the most stable isobars for:

$$A = 12, 16, 25, 56, 107, 197, 238$$

Compare with available data.

Exercise 10:

What is the Coulomb repulsion energy of two protons in 3_2He if it is assumed that they separated by a nuclear radius?

Exercise 11:

What is the difference between the binding energy of 3_2He and 3_1H ? Comment the result.

Exercise 12:

Compare the separation energy of a neutron from the following isotopes: $^{41}_{20}Ca$, $^{42}_{20}Ca$ and $^{43}_{20}Ca$

$M(20, 43) = 42.958770$

Exercise 13:

(a) "Mirror" nuclei have the same odd value of A, but the values of N and Z are interchanged. Determine the mass difference between two mirror nuclei which have $N - Z = 1$.

(b) the masses of $^{23}_{11}Na$ and $^{23}_{12}Mg$ are $22.989771u$ and $22.994125u$, respectively. From these data determine the Coulomb coefficient a_C in the semiempirical formula.

