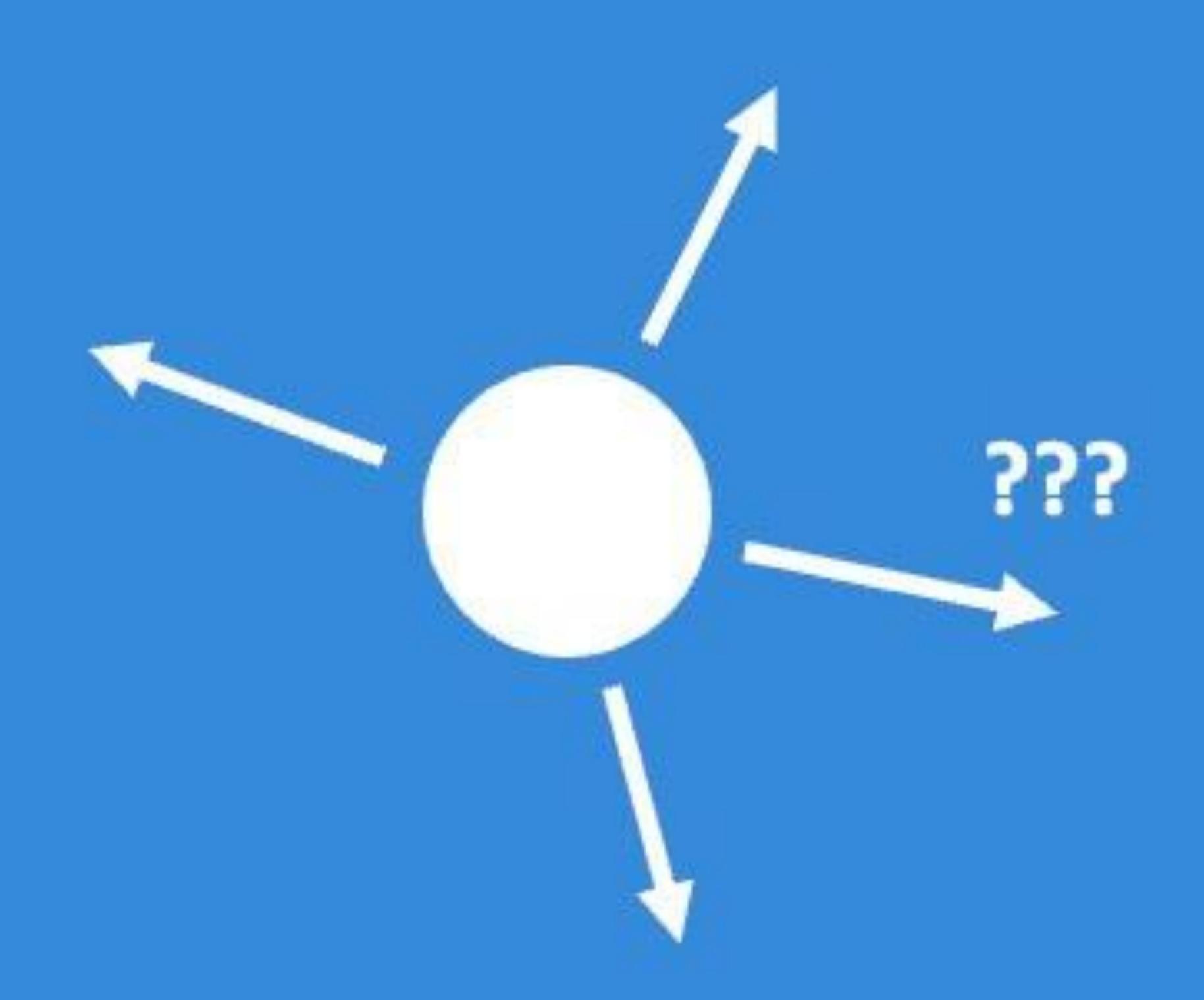
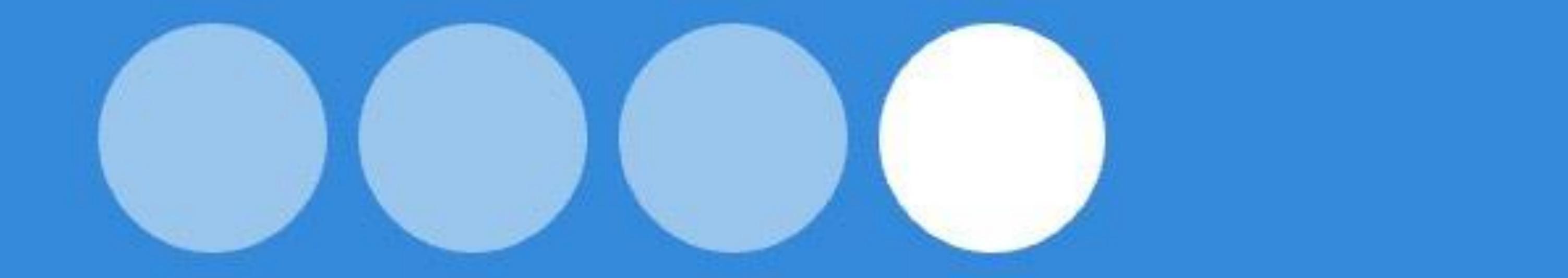
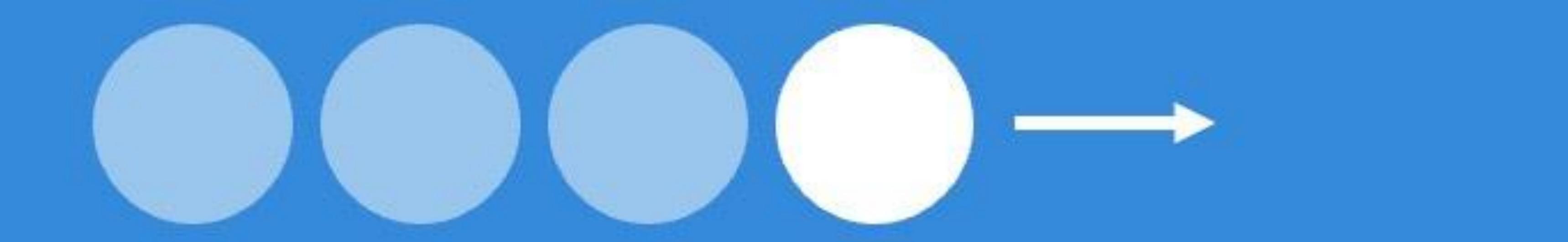
RECURRENT NEURAL NETWORK

Chapter 2





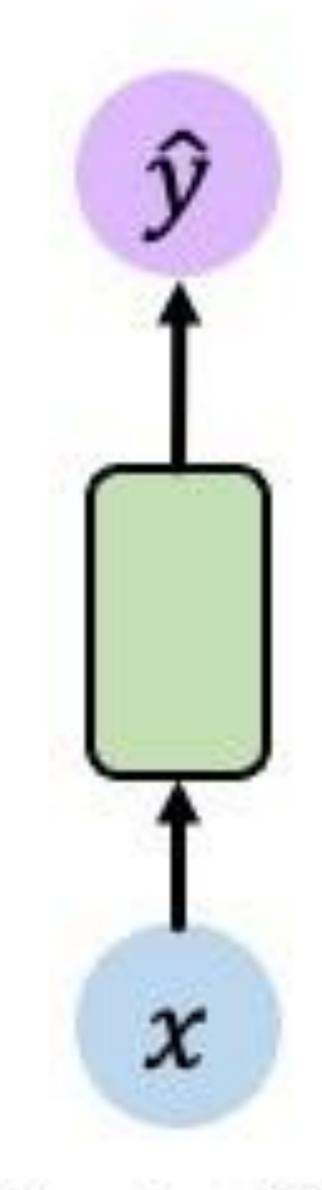


Sequences in the Wild

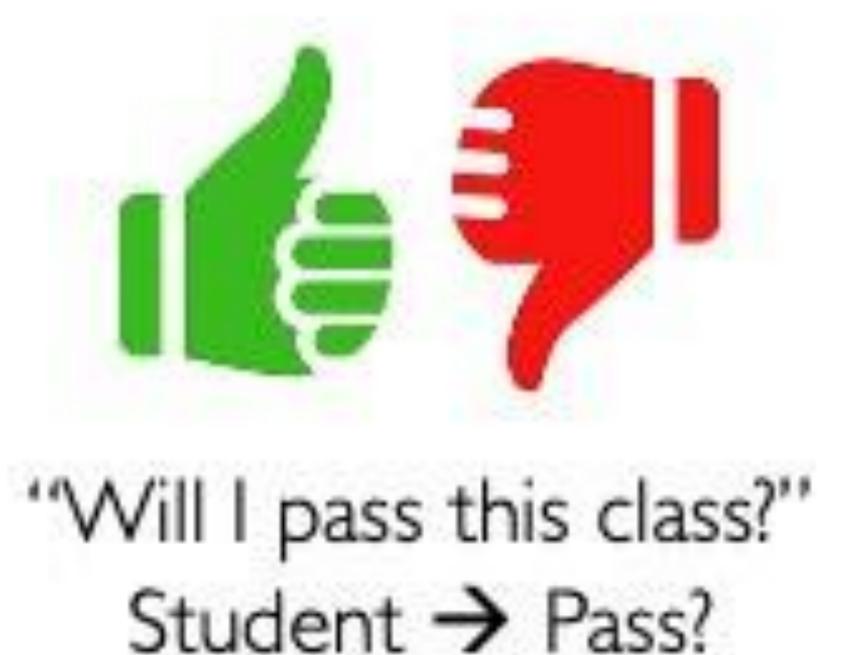


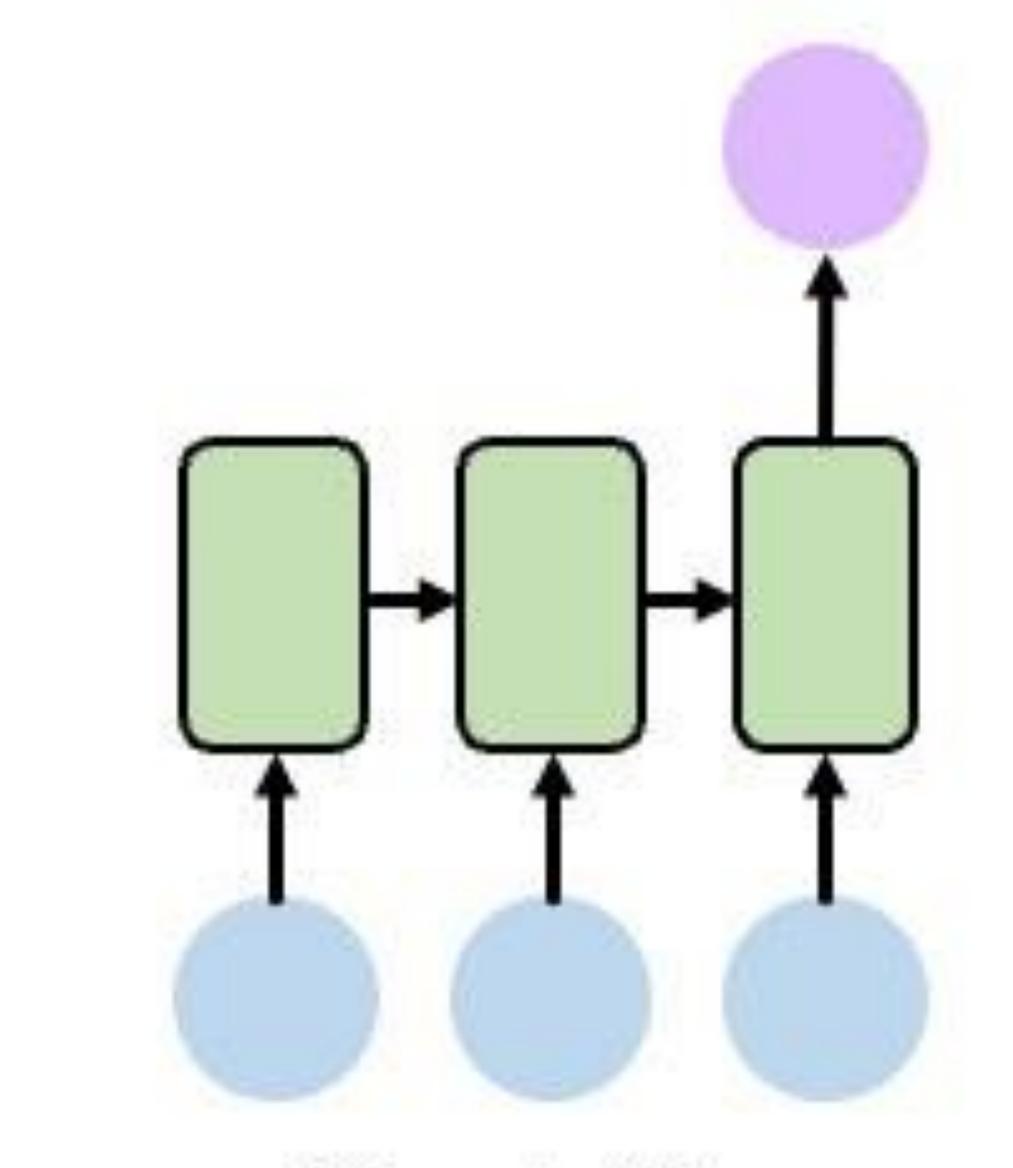
Audio

Sequence Modeling Applications



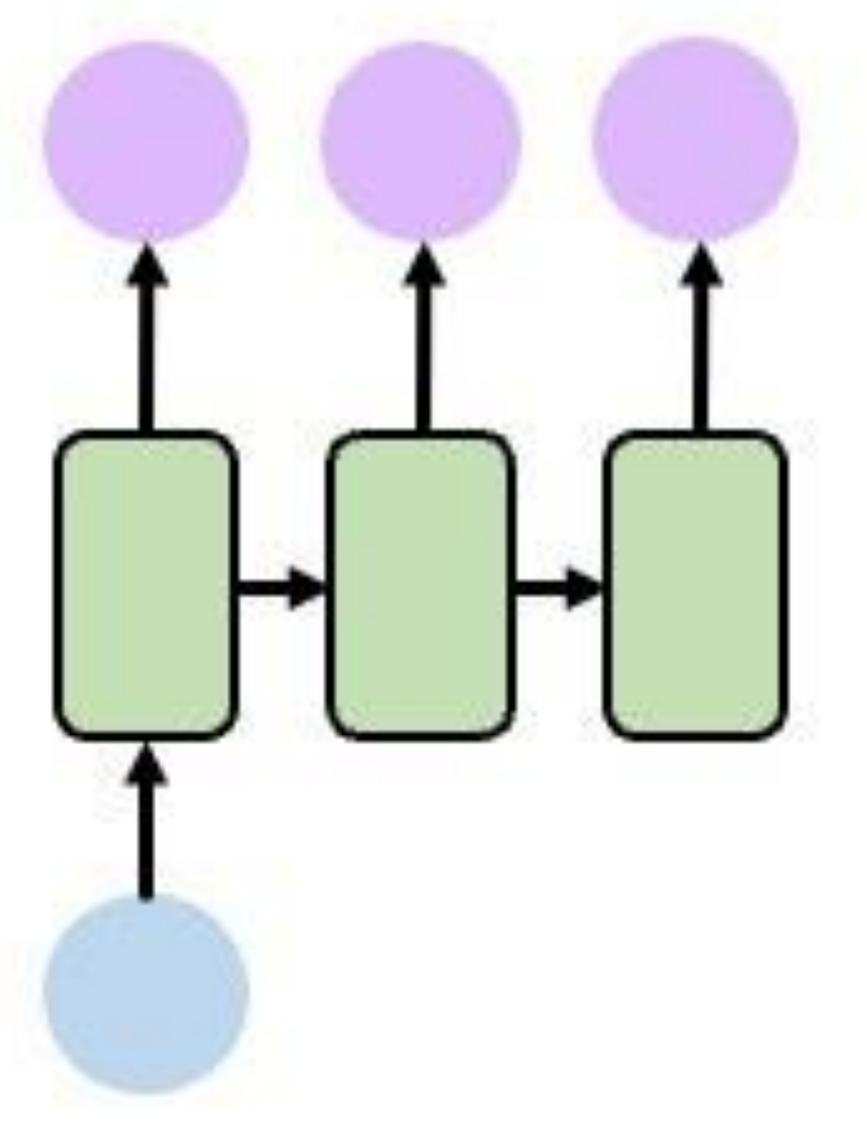
One to One Binary Classification





Many to One Sentiment Classification

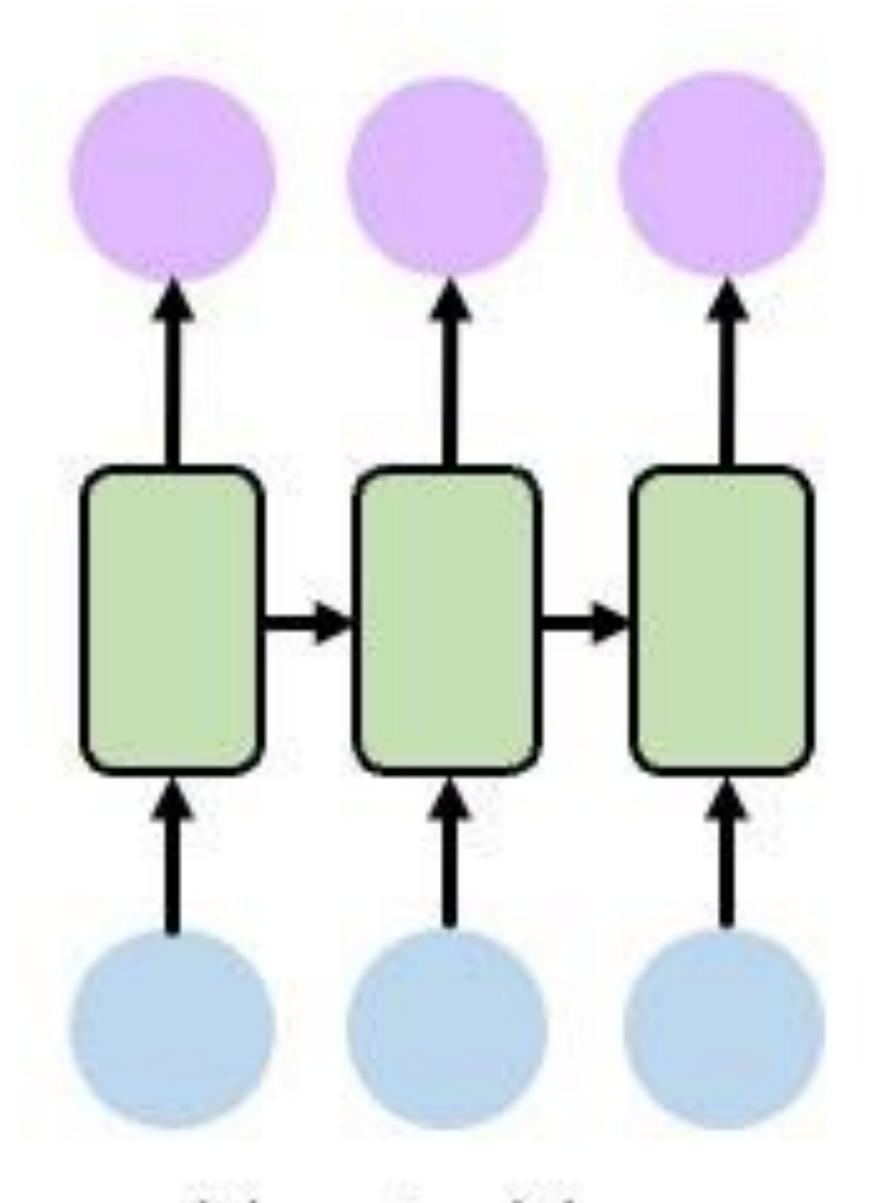




One to Many Image Captioning



"A baseball player throws a ball."



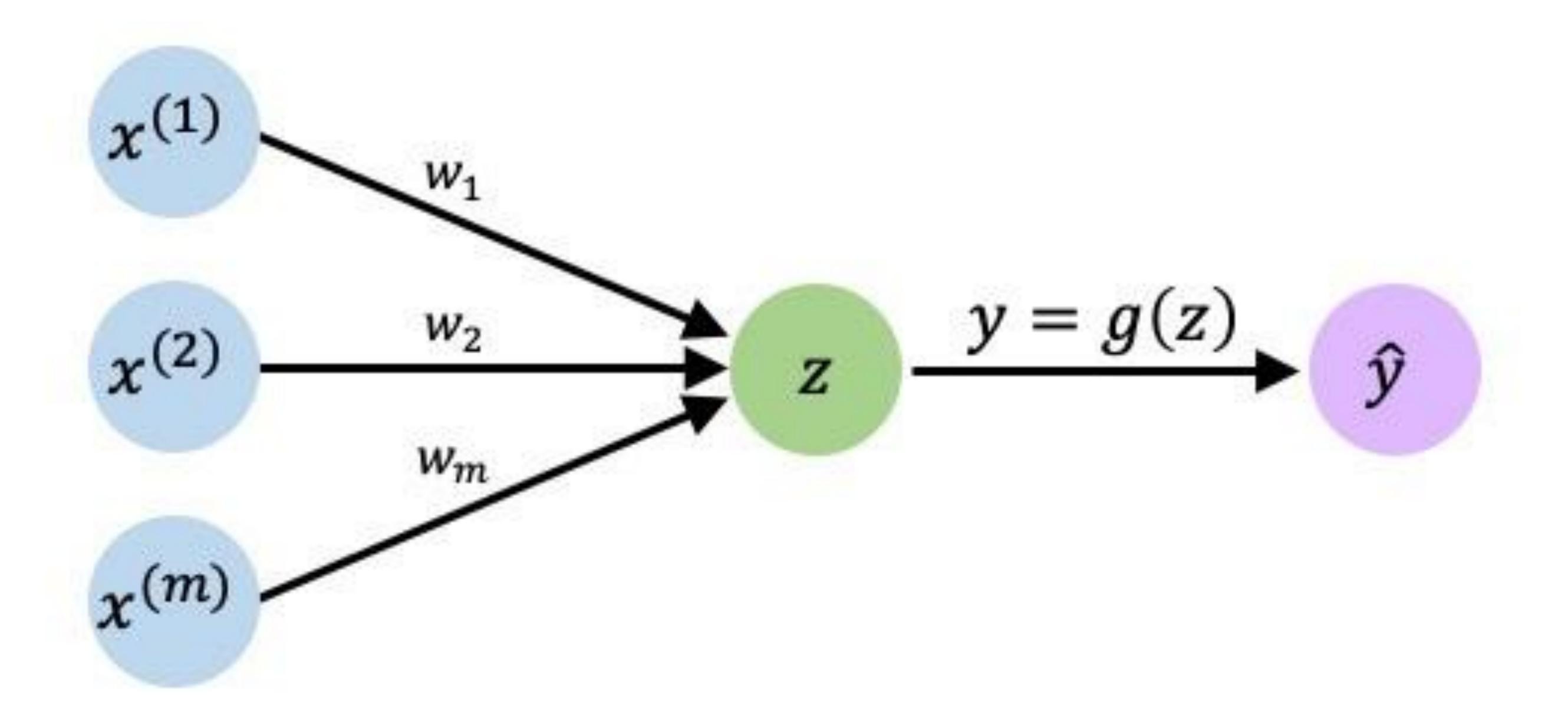
Many to Many

Machine Translation

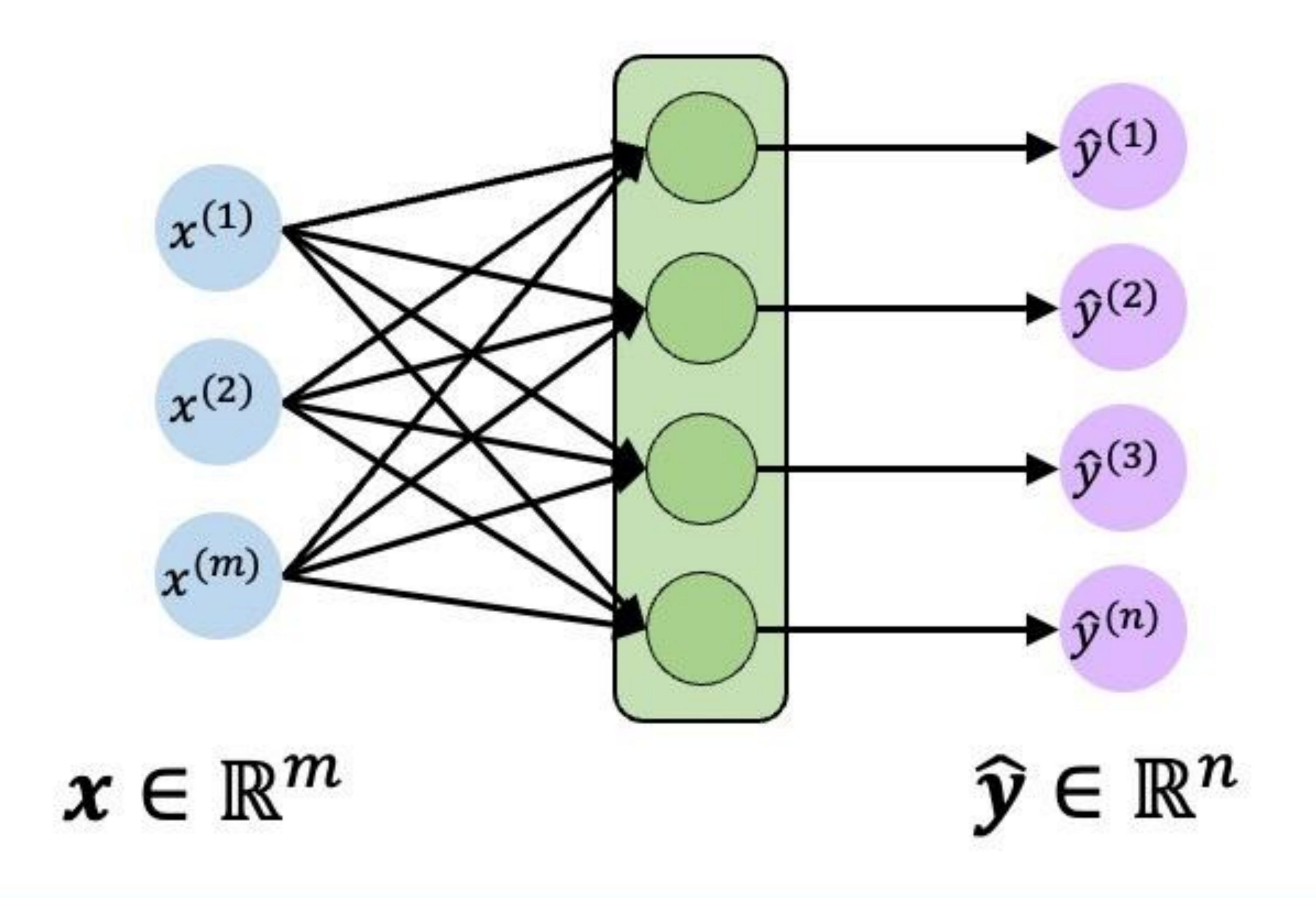


Neurons with Recurrence

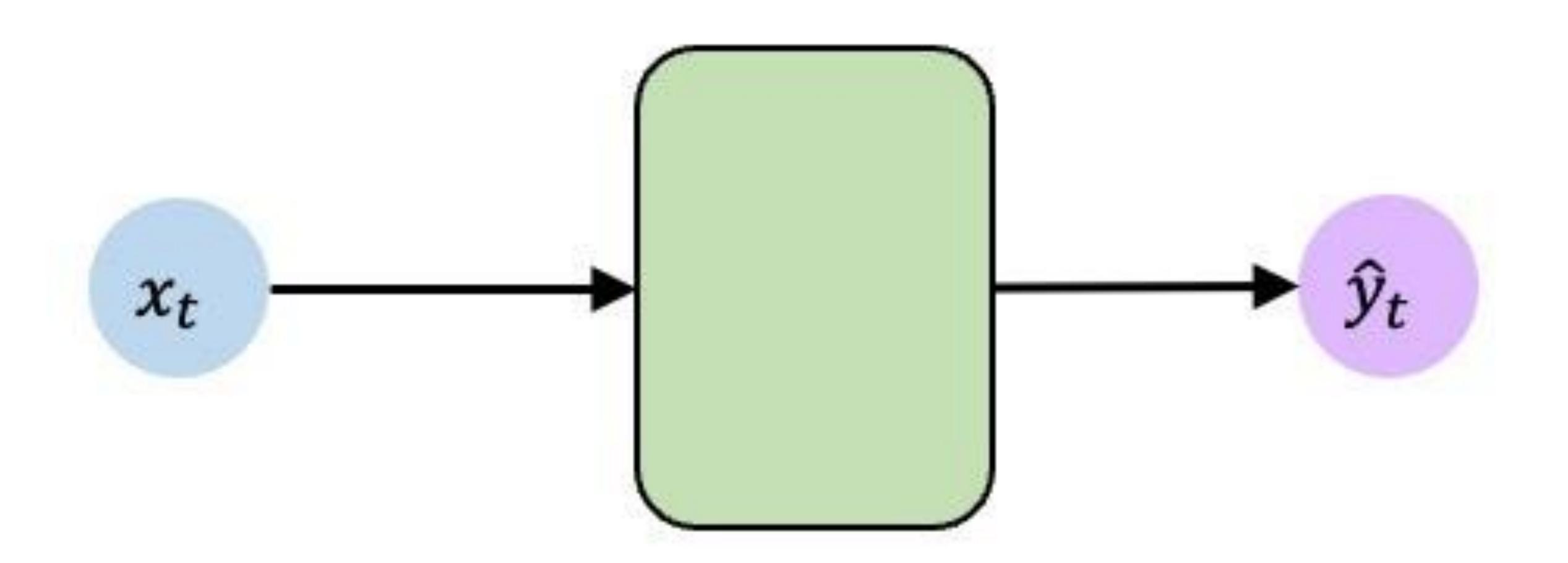
The Perceptron Revisited



Feed-Forward Networks Revisited



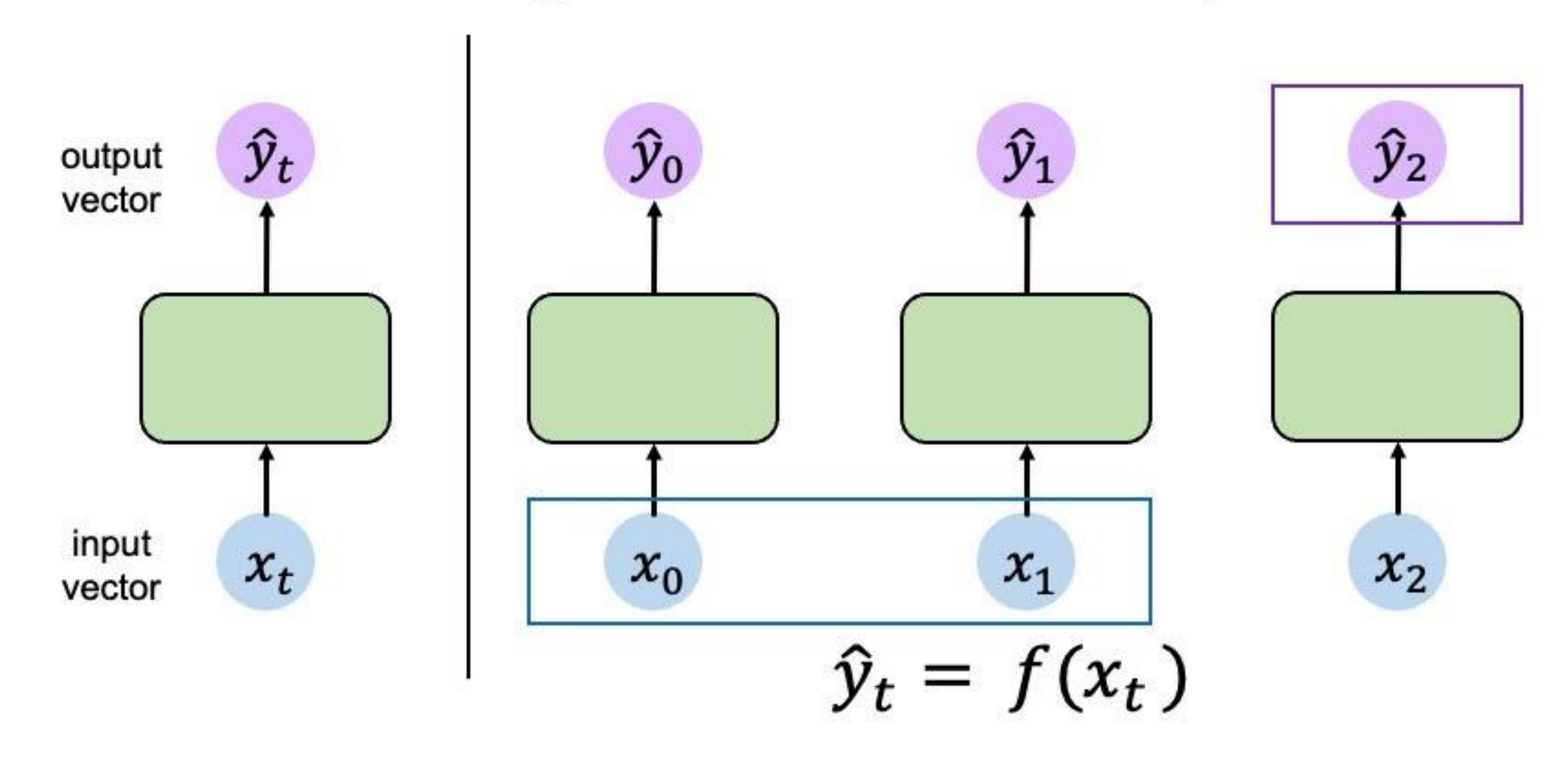
Feed-Forward Networks Revisited



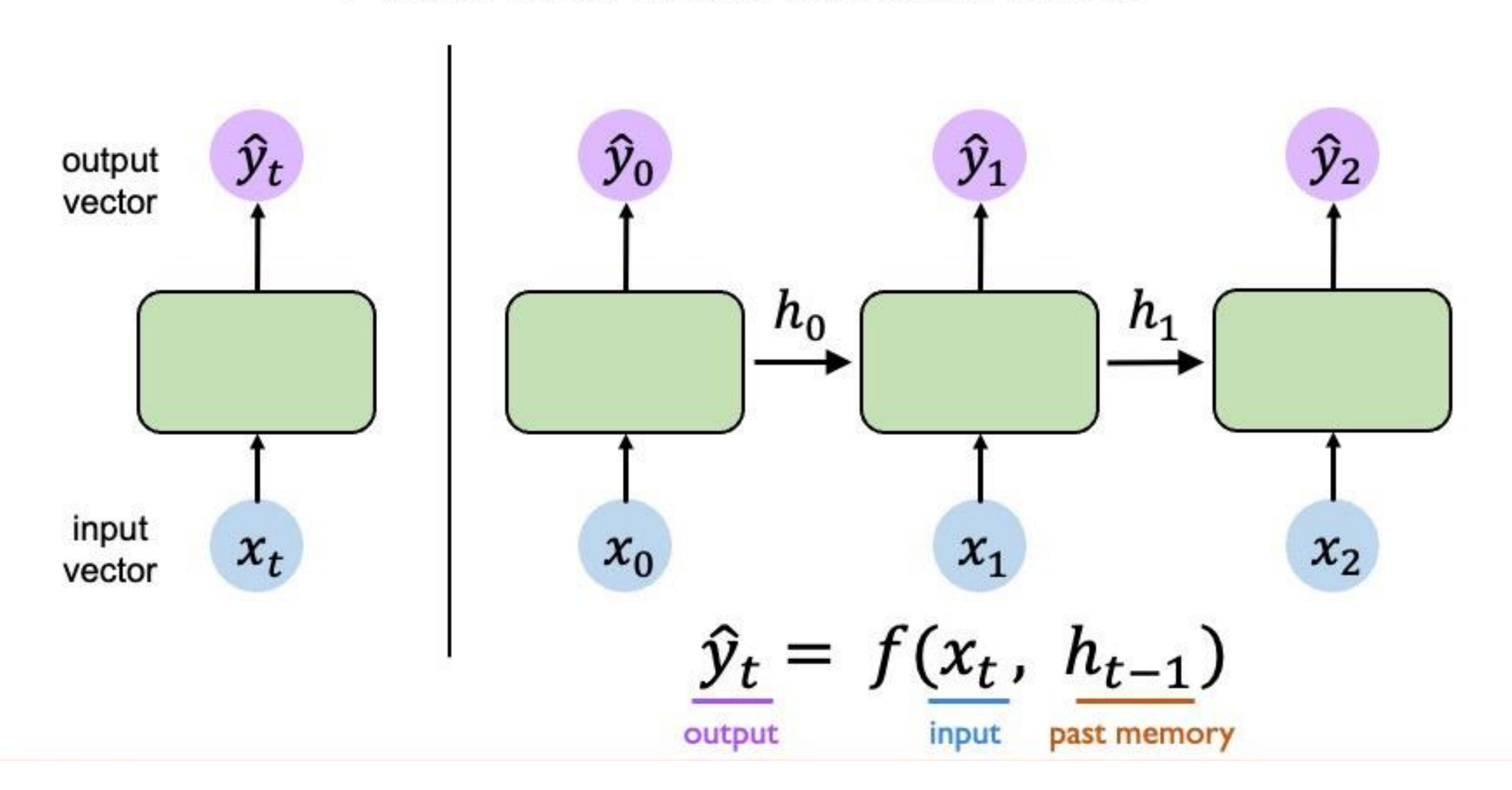
$$x_t \in \mathbb{R}^m$$

$$\hat{y}_t \in \mathbb{R}^n$$

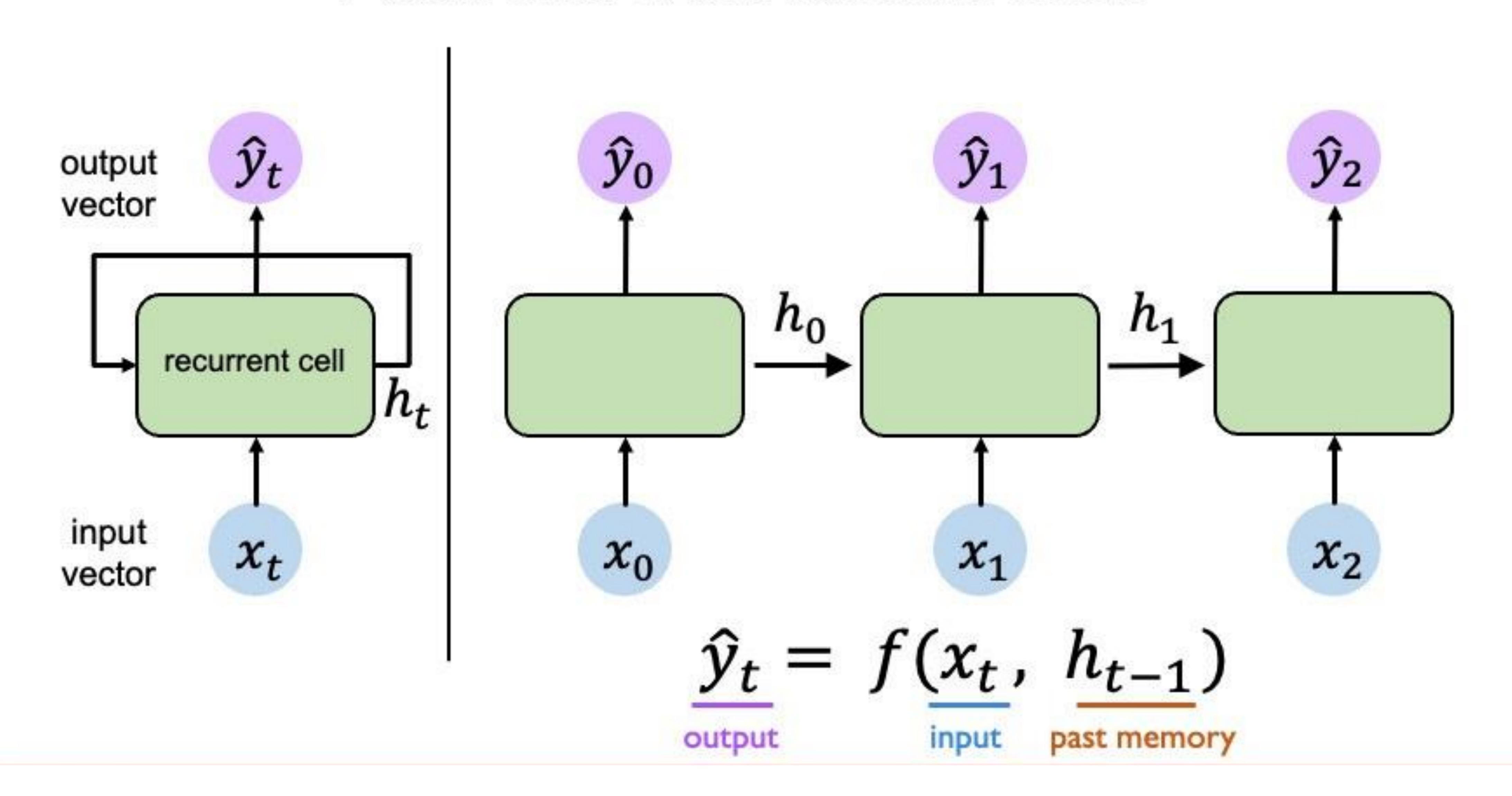
Handling Individual Time Steps



Neurons with Recurrence

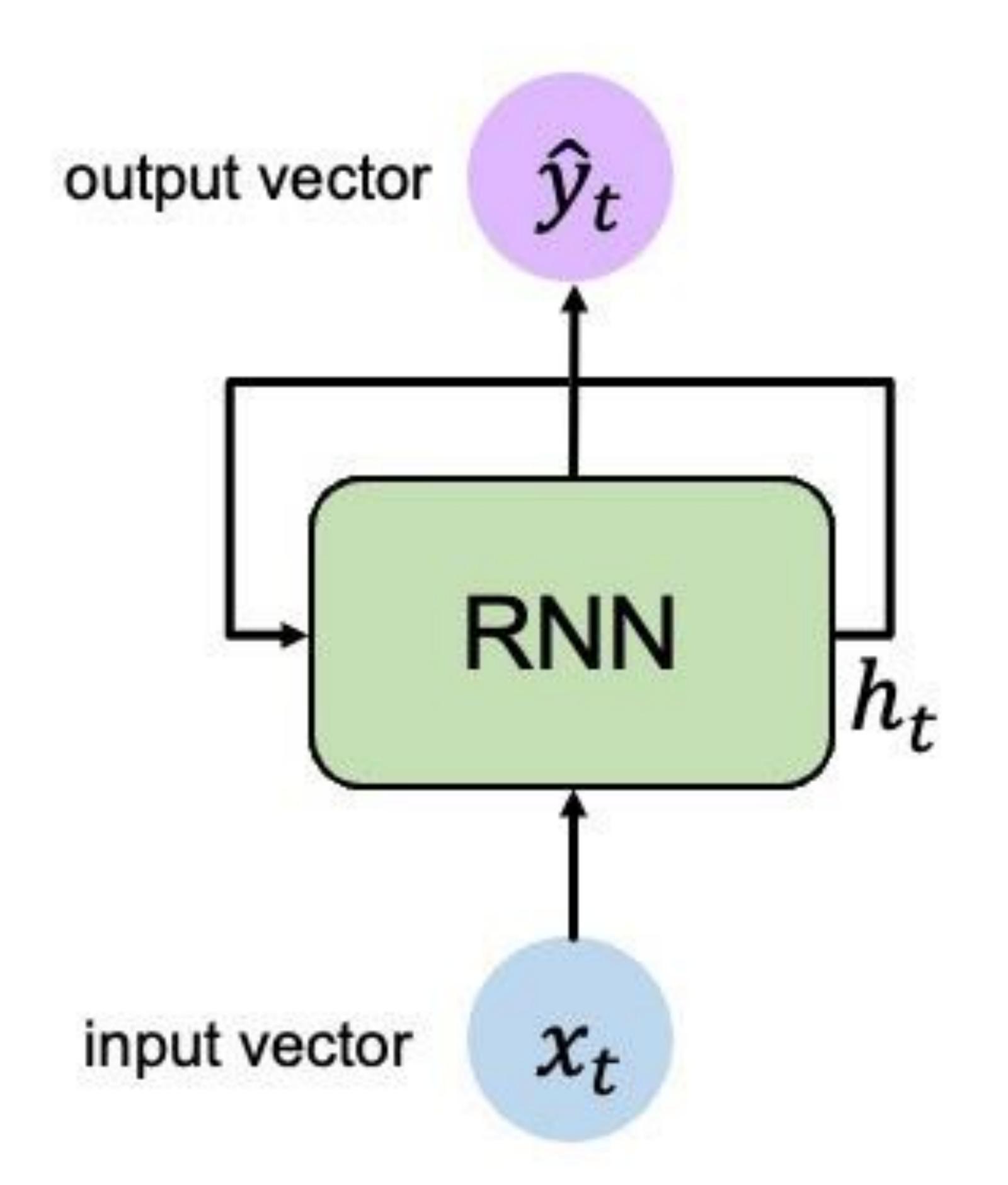


Neurons with Recurrence



Recurrent Neural Networks (RNNs)

Recurrent Neural Networks (RNNs)



Apply a recurrence relation at every time step to process a sequence:

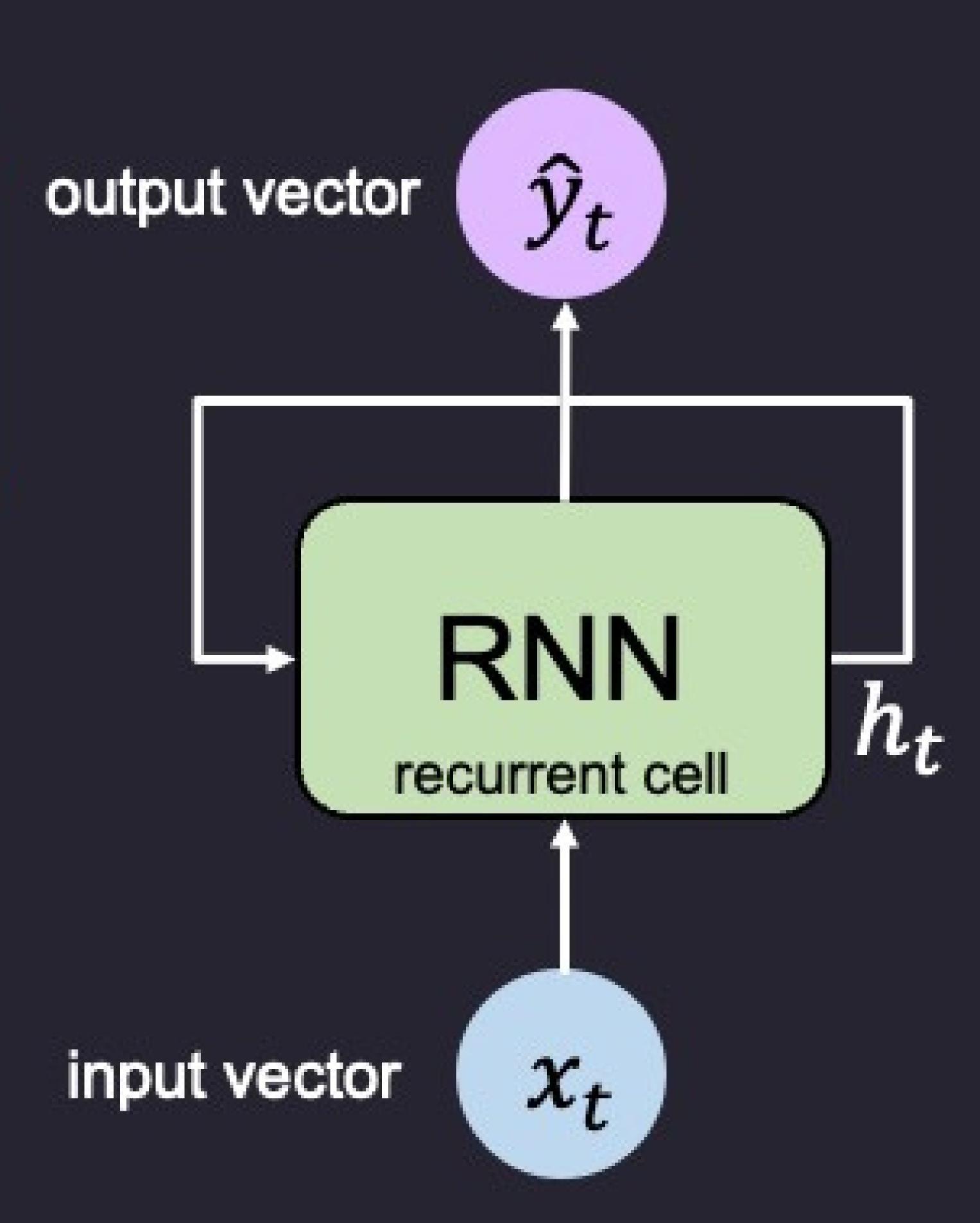
$$h_t = f_W(x_t, h_{t-1})$$
cell state function input old state with weights w

Note: the same function and set of parameters are used at every time step

RNNs have a state, h_t , that is updated at each time step as a sequence is processed

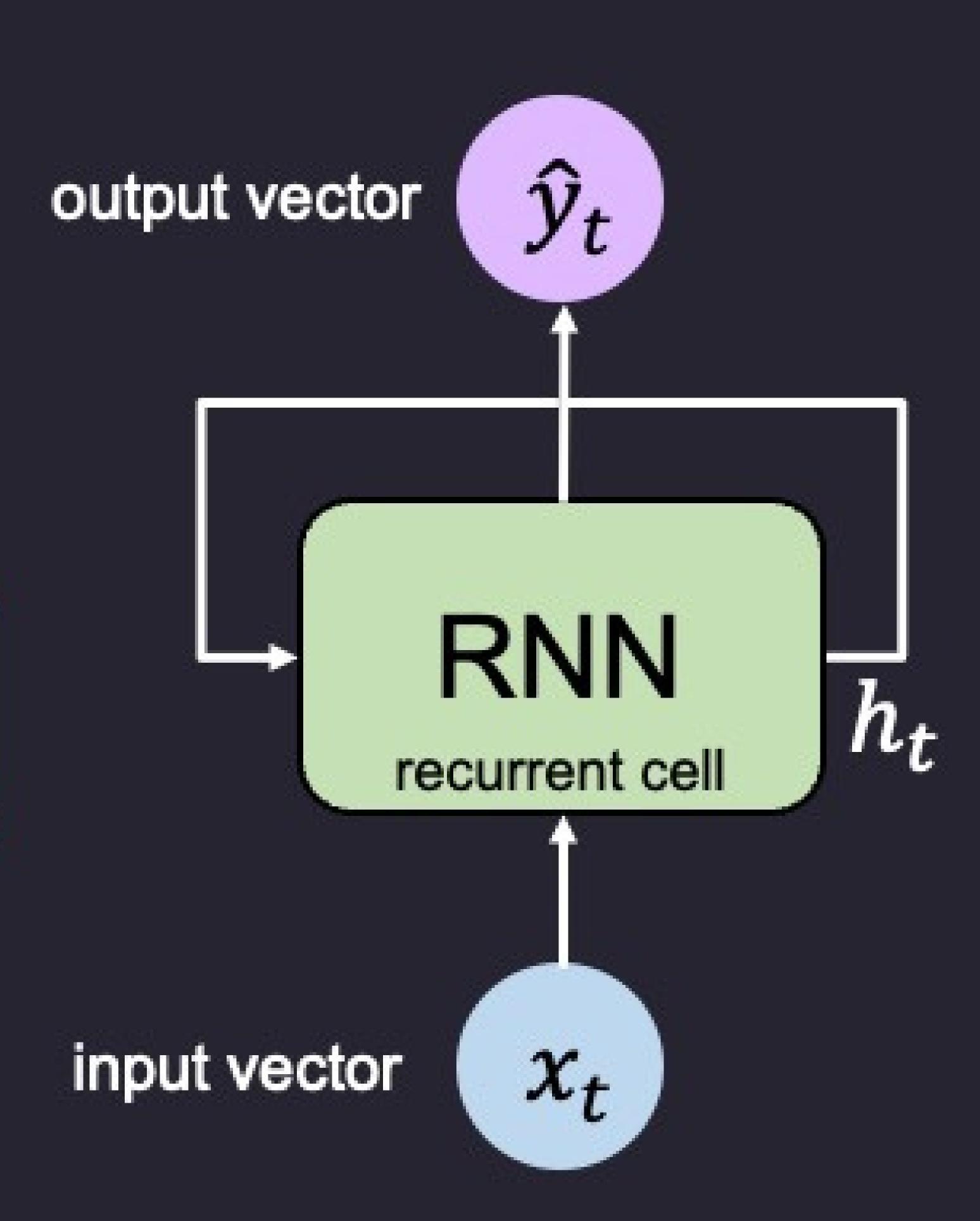
RNN Intuition

```
my rnn - RNN()
hidden state = [0, 0, 0, 0]
sentence = ["I", "love", "recurrent", "neural"]
for word in sentence:
    prediction, hidden state = my rnn (word, hidden state)
next word prediction = prediction
# >>> "networks!"
```



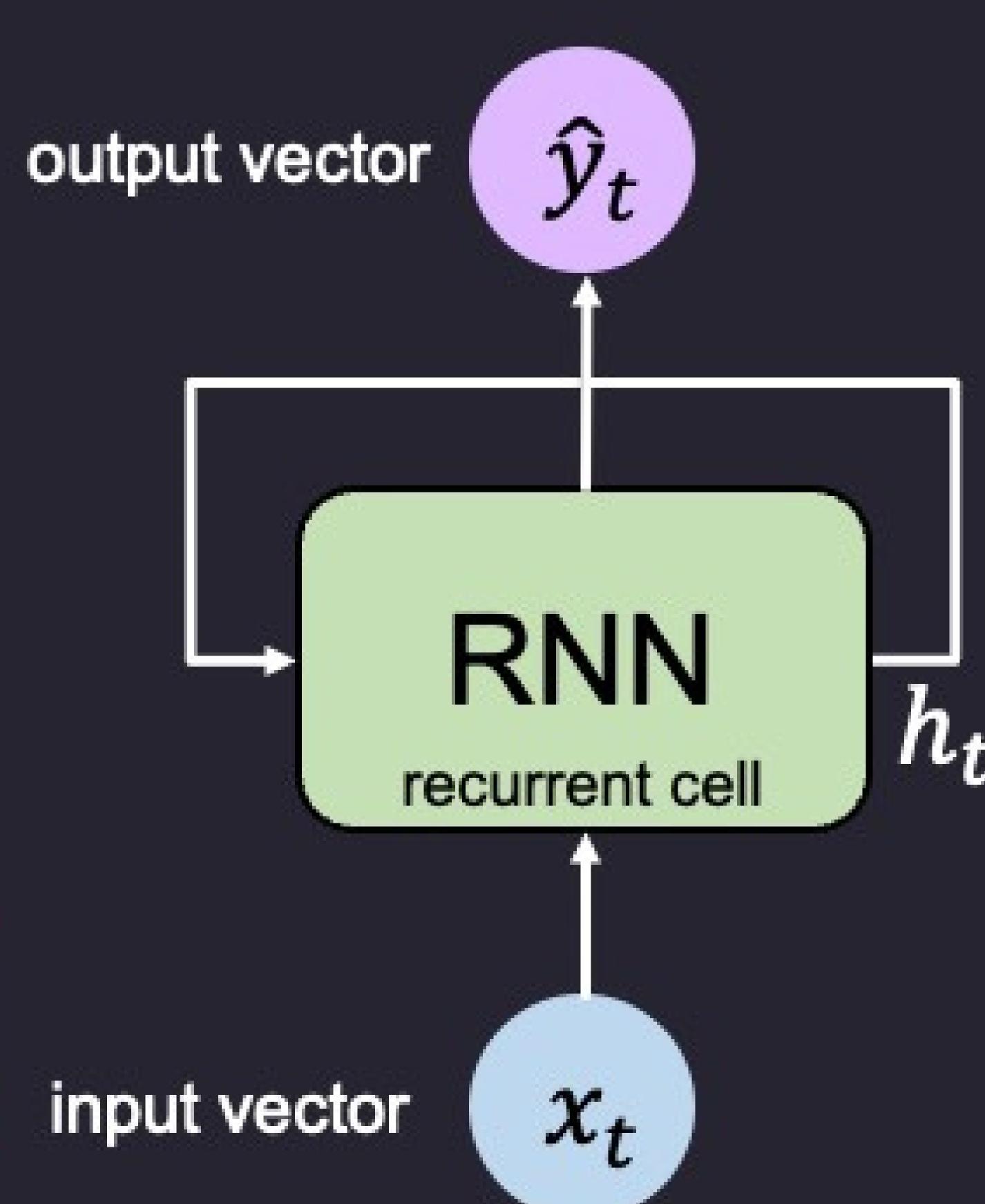
RNN Intuition

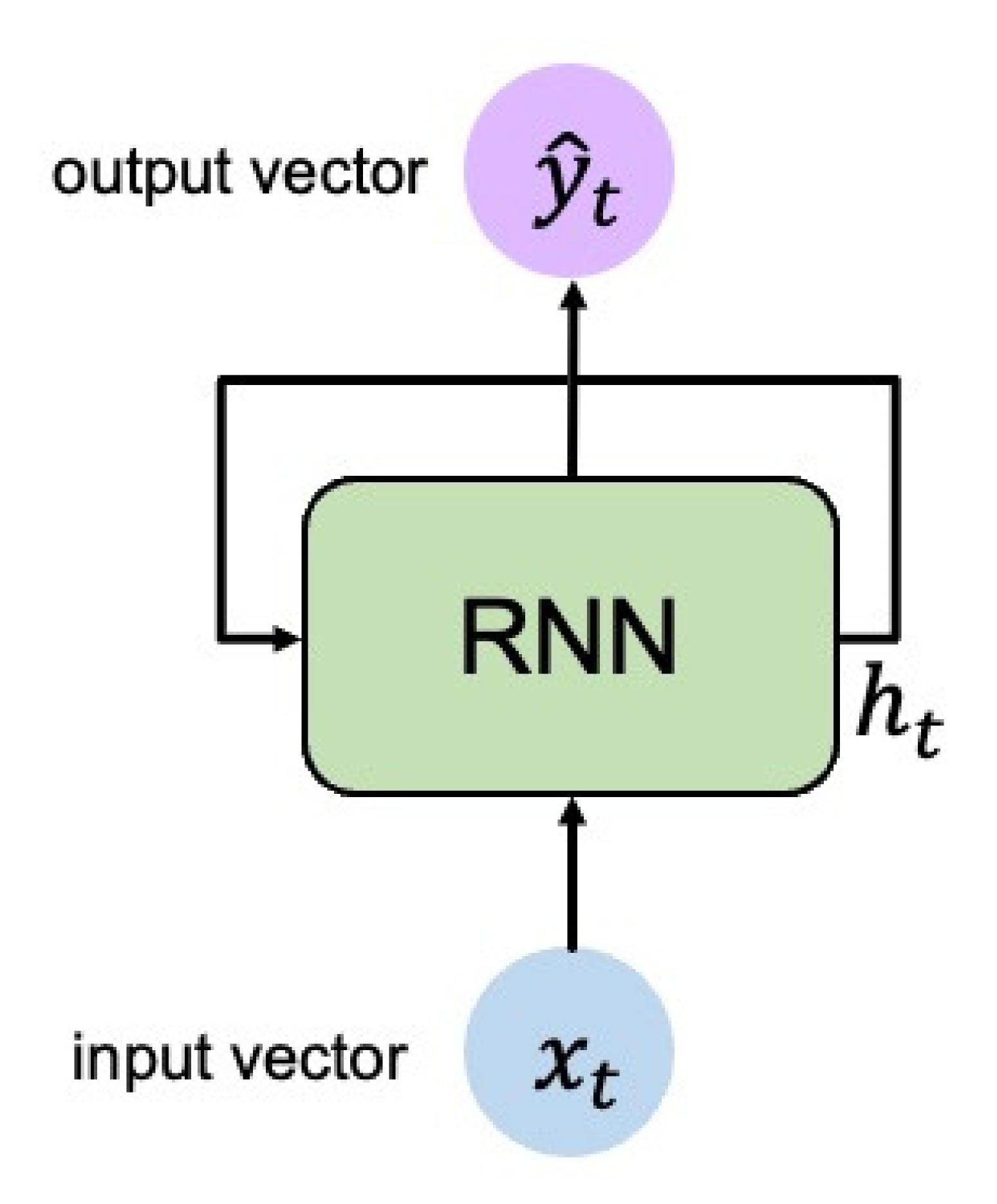
```
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```

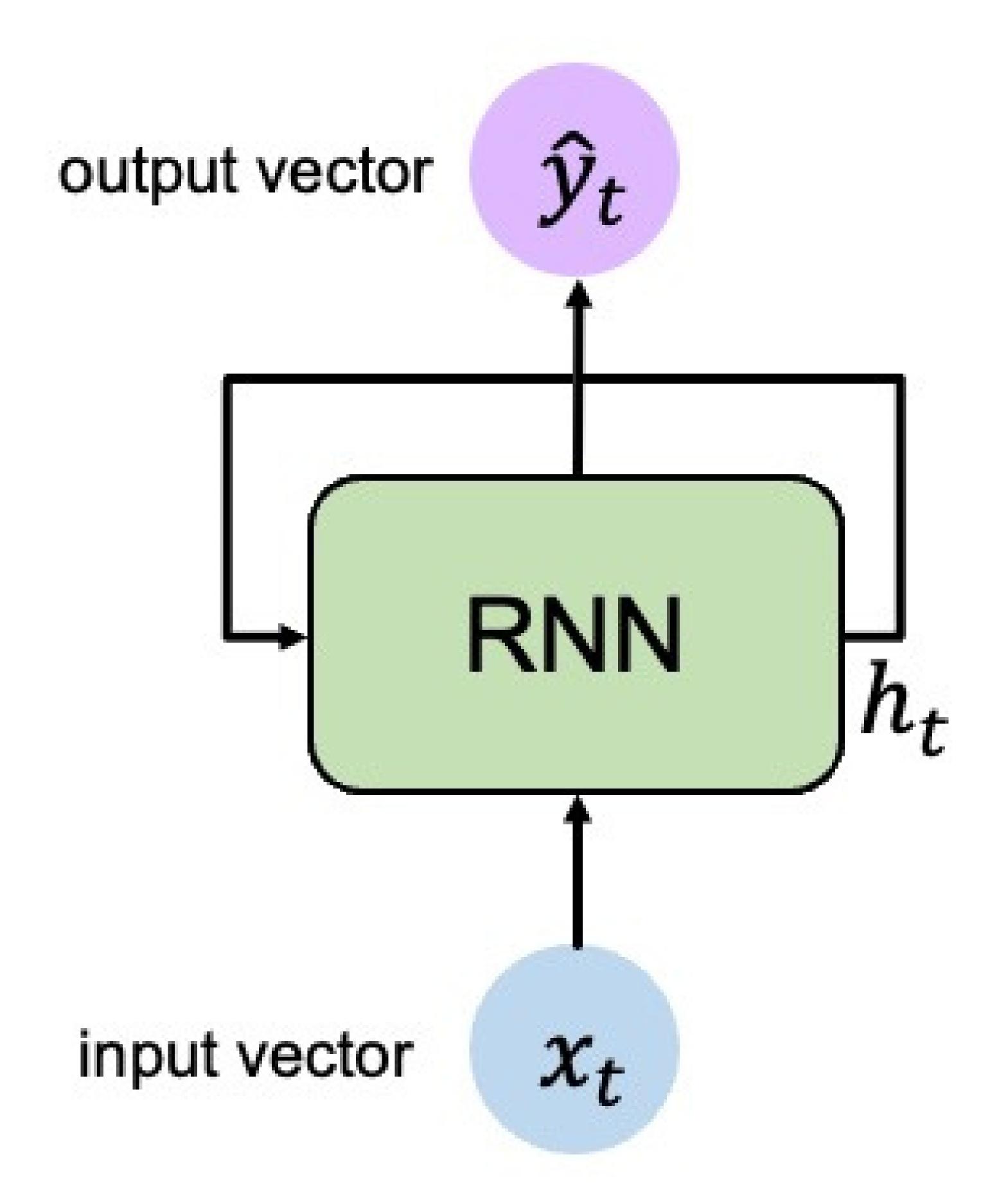


RINI Intuition

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for word in sentence:
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next word prediction = prediction
# >>> "networks!"
```

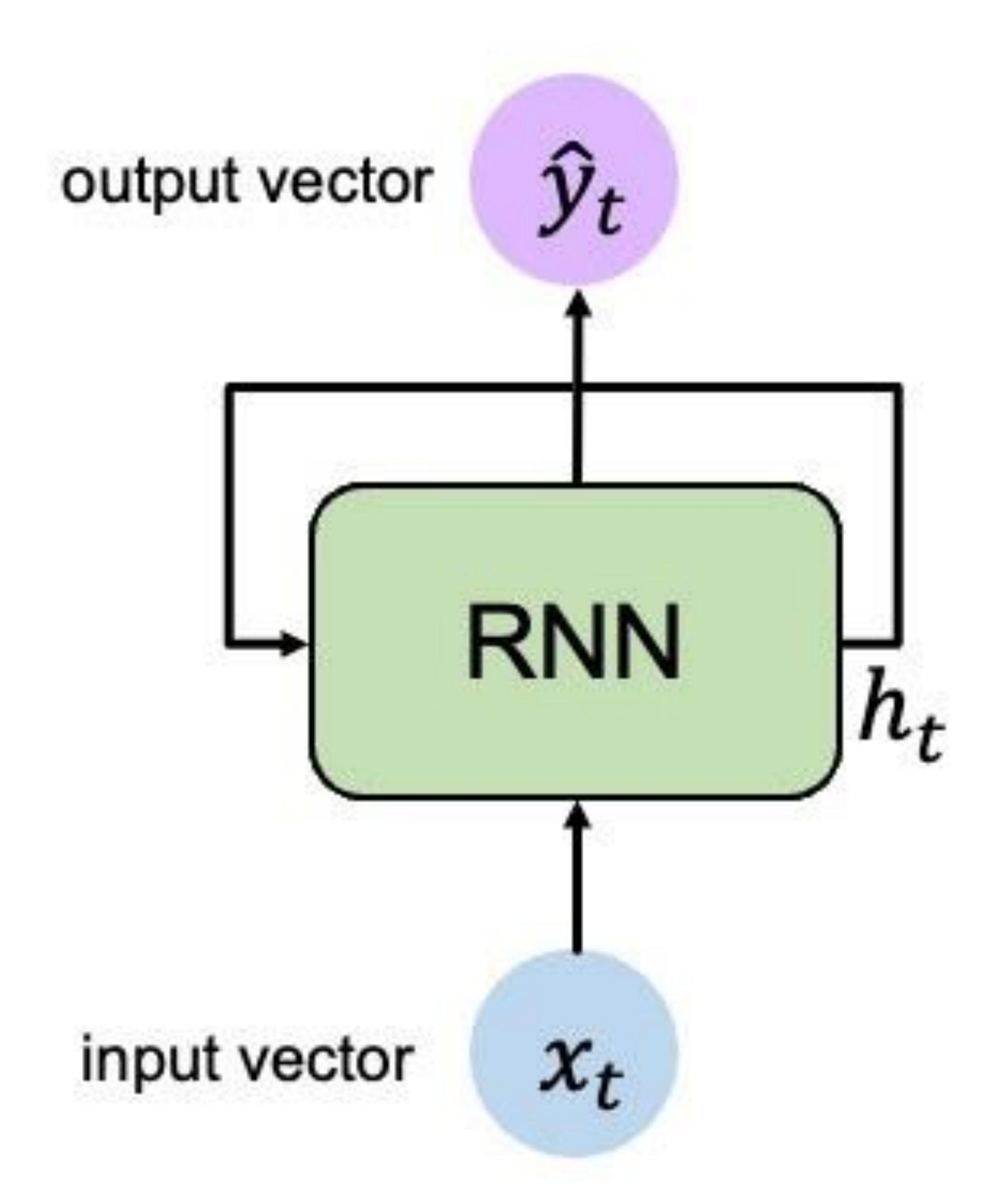






Input Vector

X_t

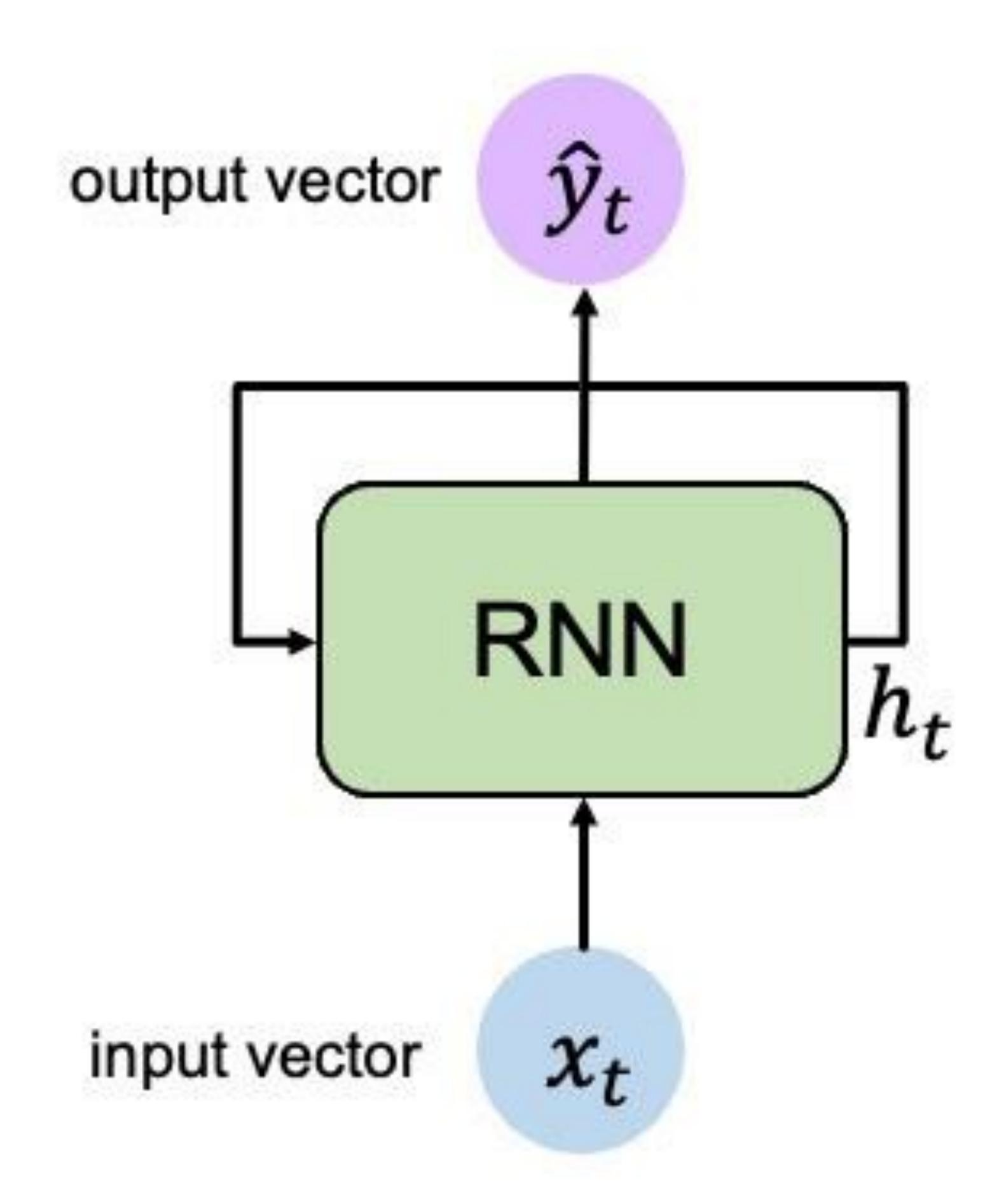


Update Hidden State

$$h_t = \tanh(\boldsymbol{W}_{hh}^T h_{t-1} + \boldsymbol{W}_{xh}^T x_t)$$

Input Vector

$$x_t$$



Output Vector

$$\hat{y}_t = W_{hy}^T h_t$$

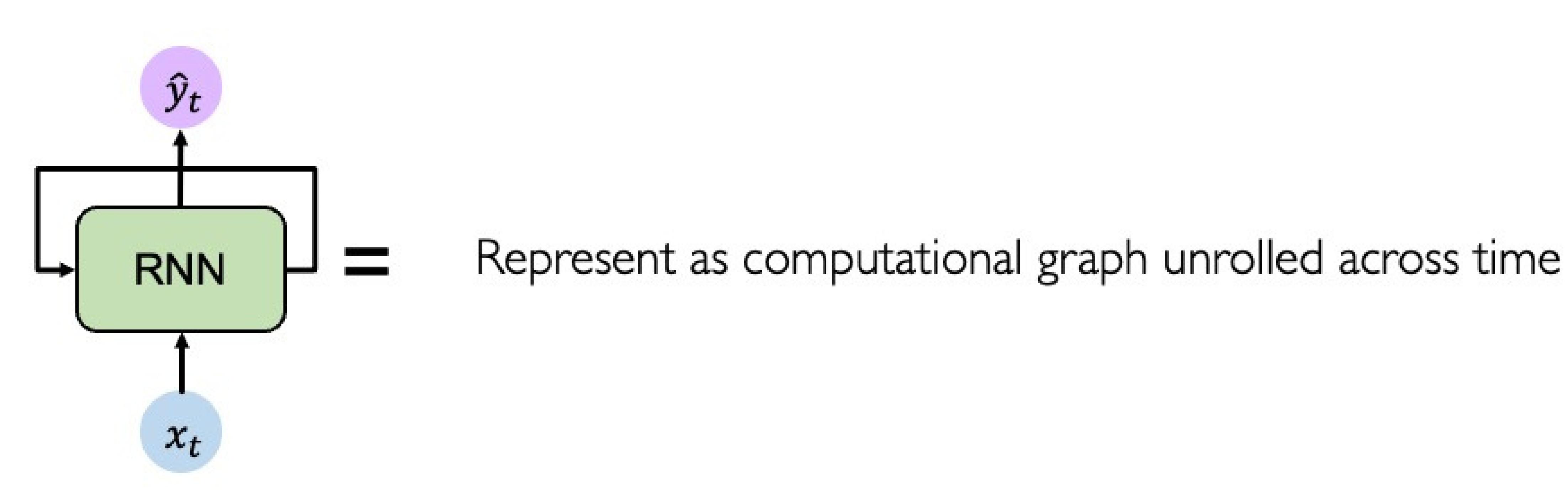
Update Hidden State

$$h_t = \tanh(\boldsymbol{W}_{hh}^T h_{t-1} + \boldsymbol{W}_{xh}^T x_t)$$

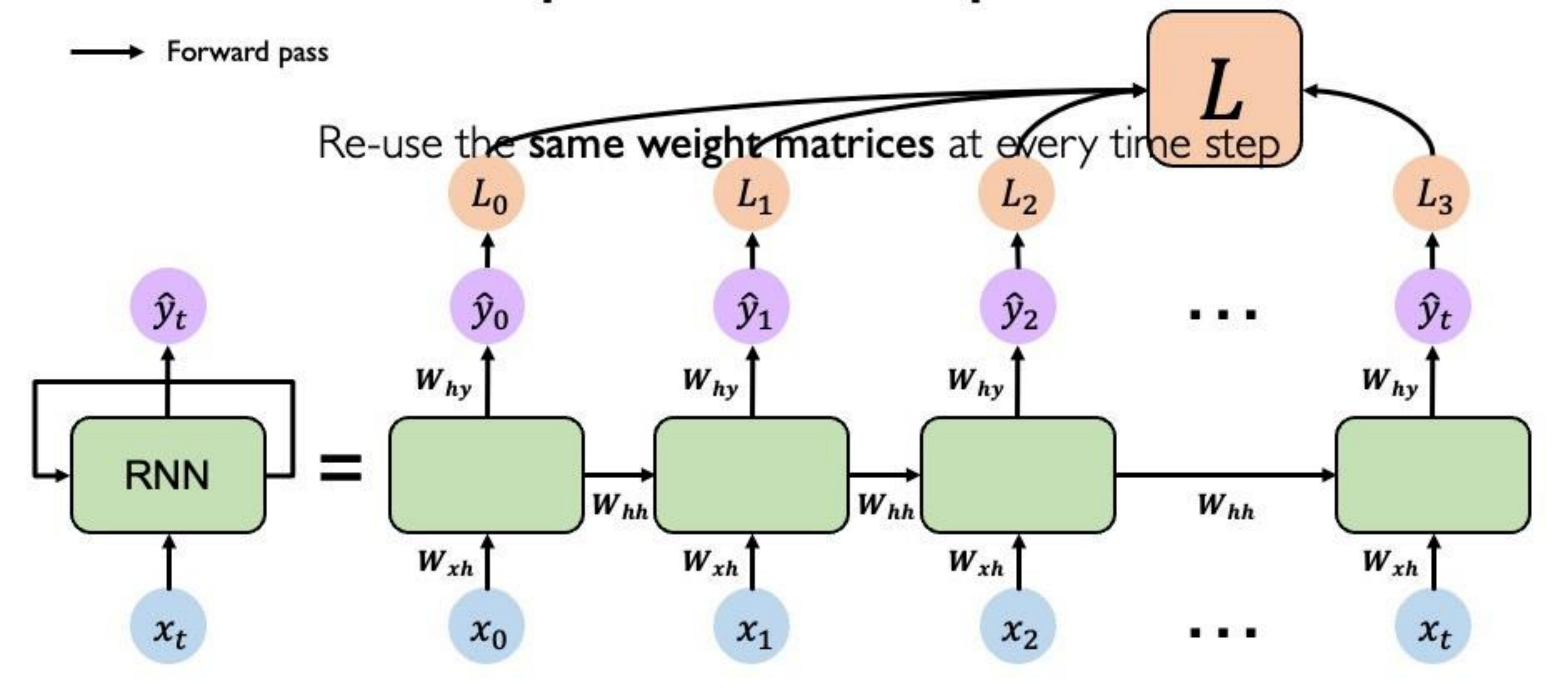
Input Vector

$$x_t$$

RNNs: Computational Graph Across Time



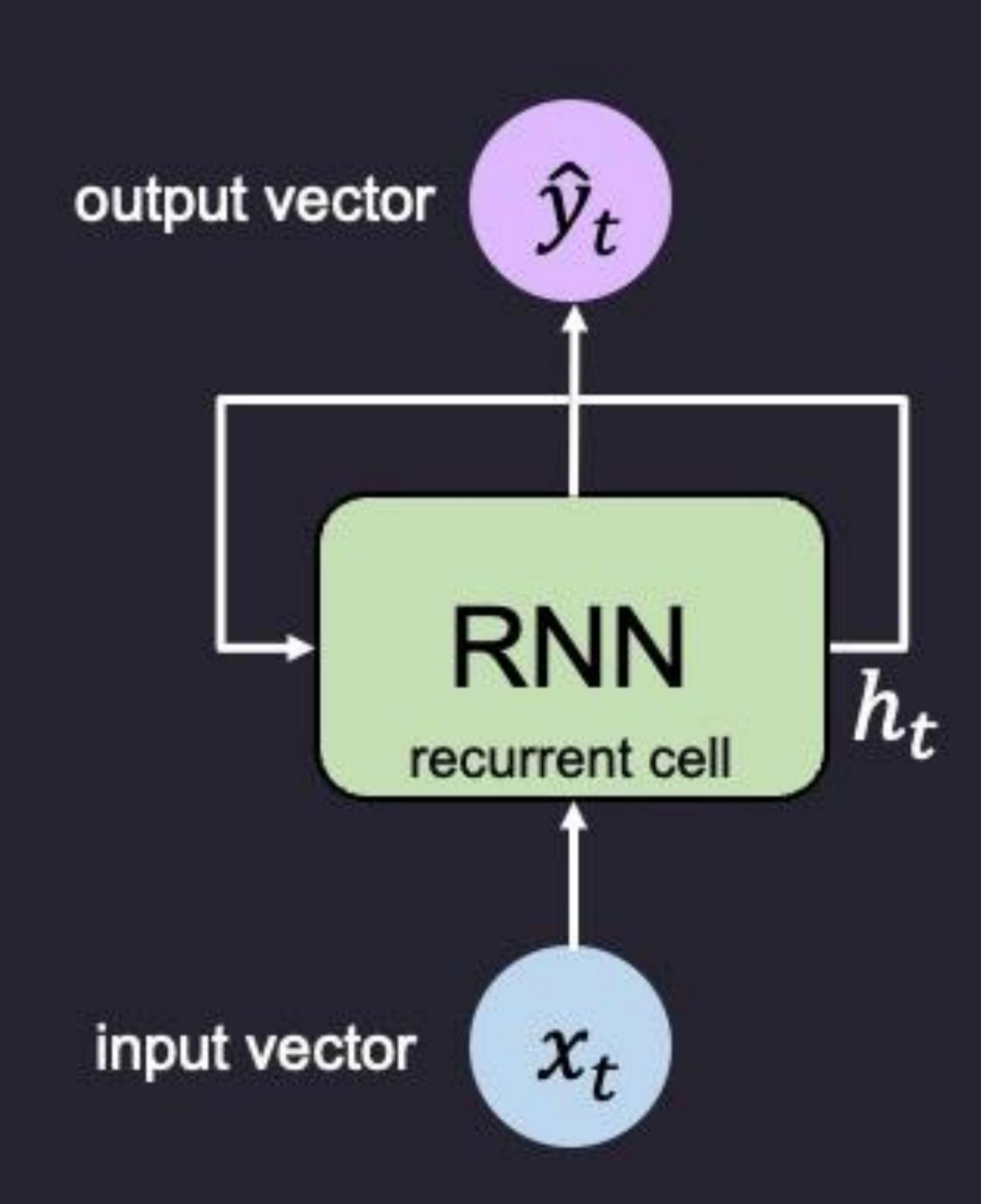
RNNs: Computational Graph Across Time



RNNs from Scratch



```
class MyRNNCell(tf keras layers Layer):
  def init (self, rnn units, input dim, output dim):
    super (MyRNNCell, self) init ()
    # Initialize weight matrices
                self add_weight([rnn_units, input_dim])
    self W hh self add weight([rnn_units, rnn_units])
    self W hy self add weight ([output_dim, rnn_units])
    # Initialize hidden state to zeros
             tf zeros([rnn_units, 1])
    self h
  def call(self, x):
    # Update the hidden state
    self h tf math tanh ( self W hh * self h * self W xh * x )
    # Compute the output
    output self W hy self h
    # Return the current output and hidden state
    return output, self h
```

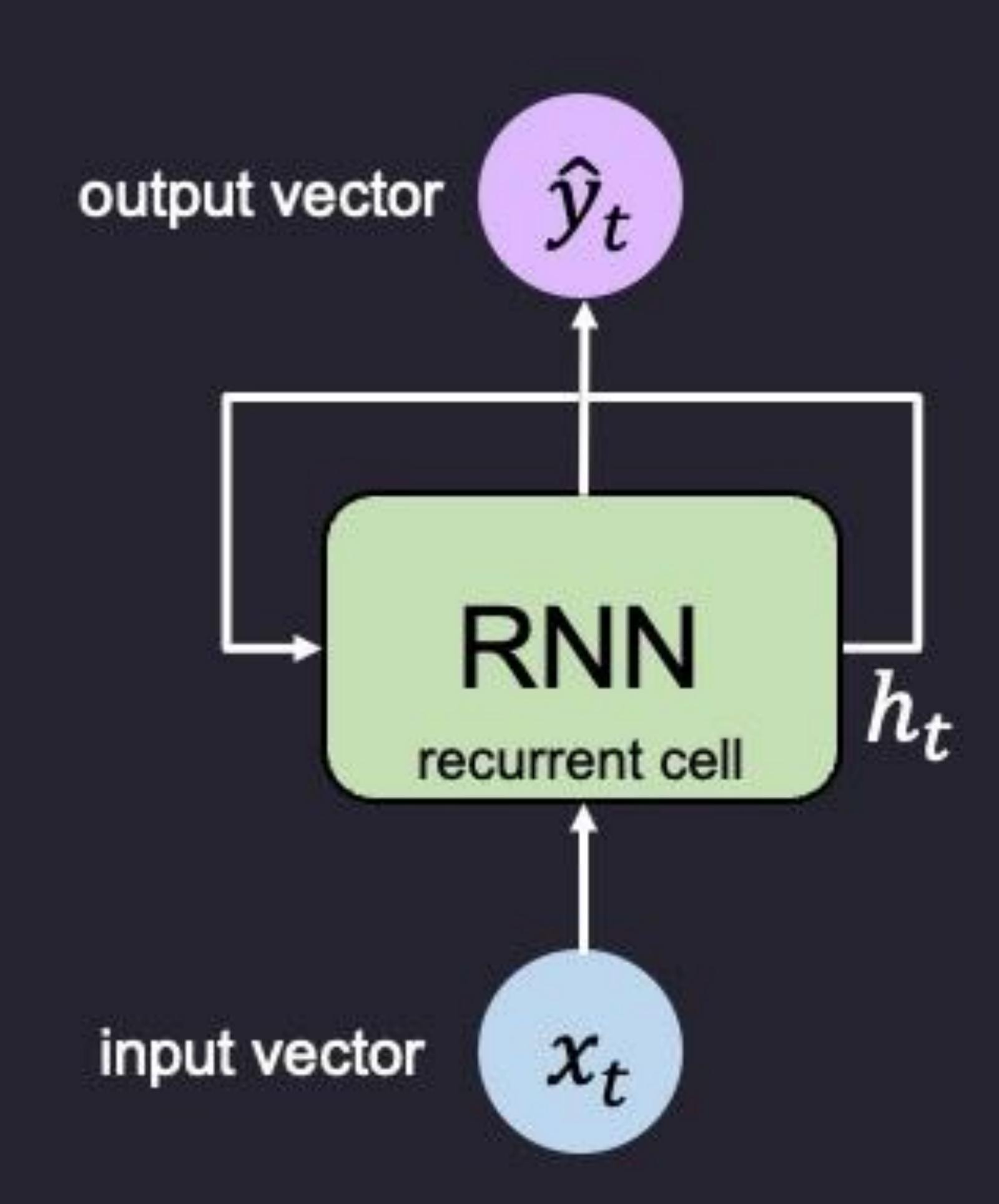


RNN Implementation in TensorFlow

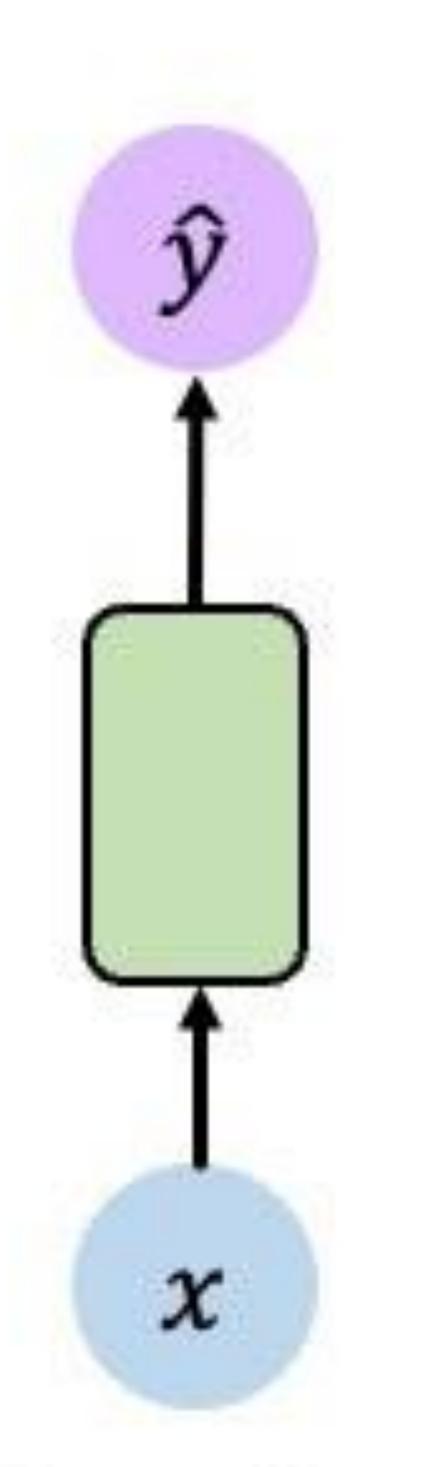


tf keras layers SimpleRNN(rnn_units)

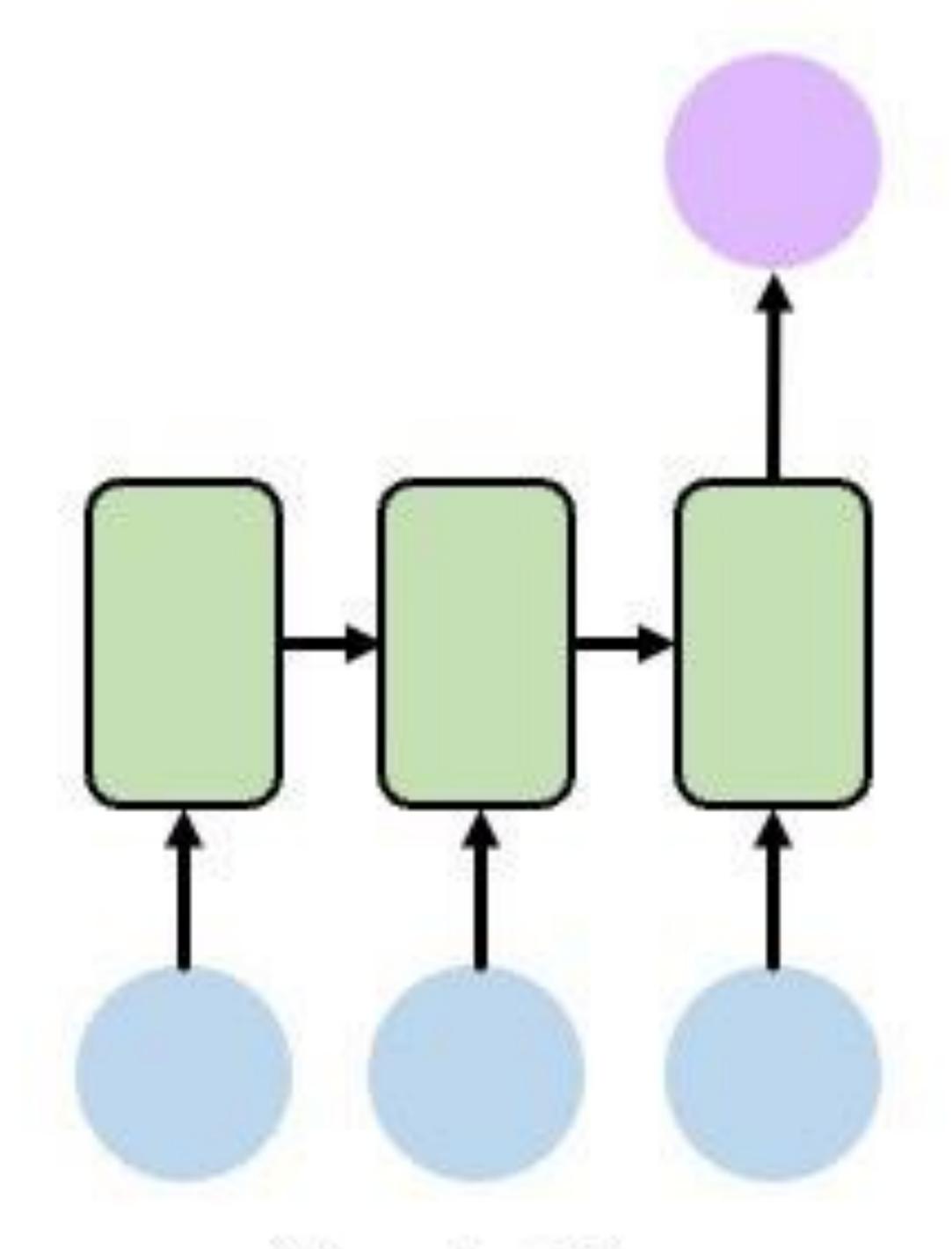




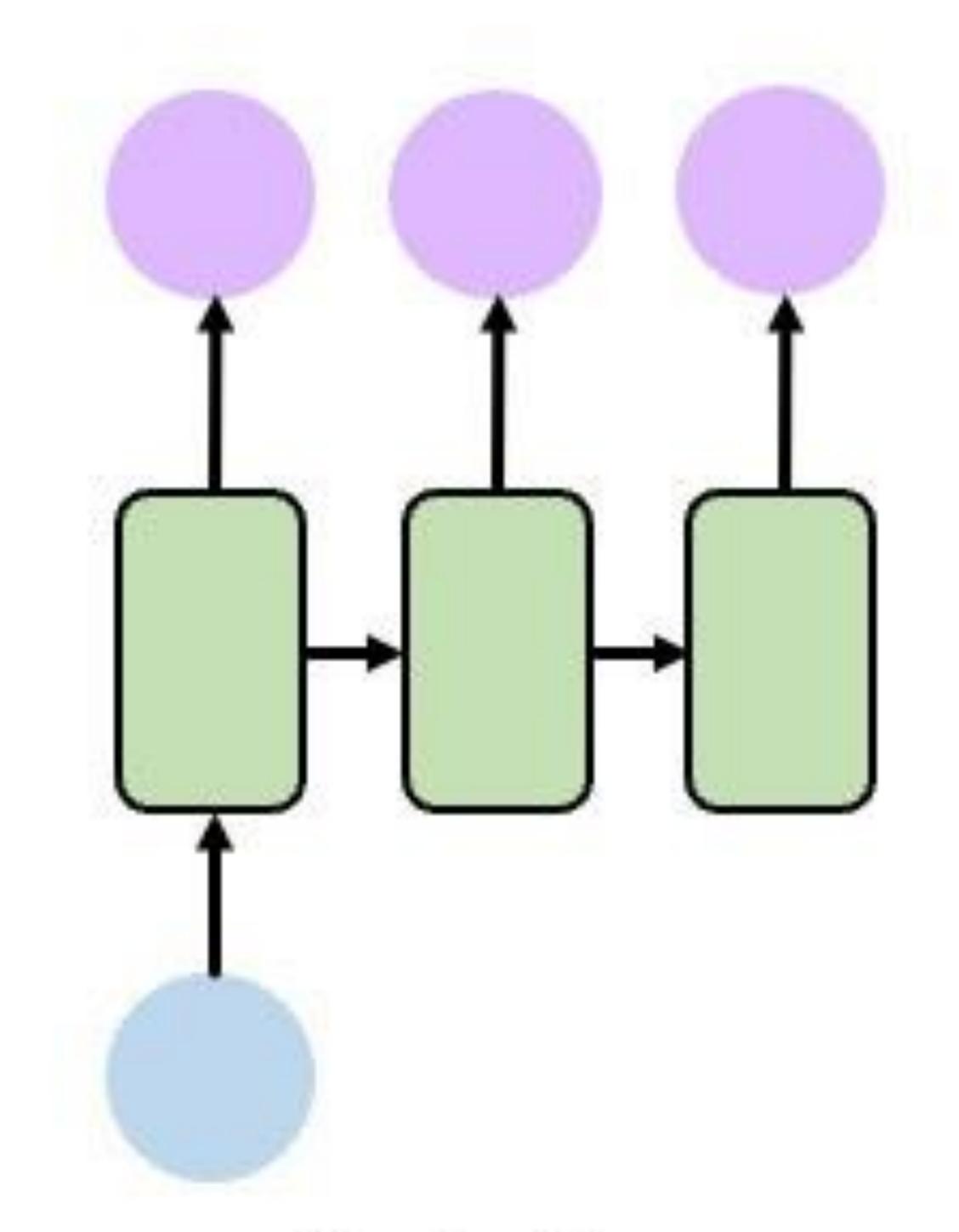
RNNs for Sequence Modeling



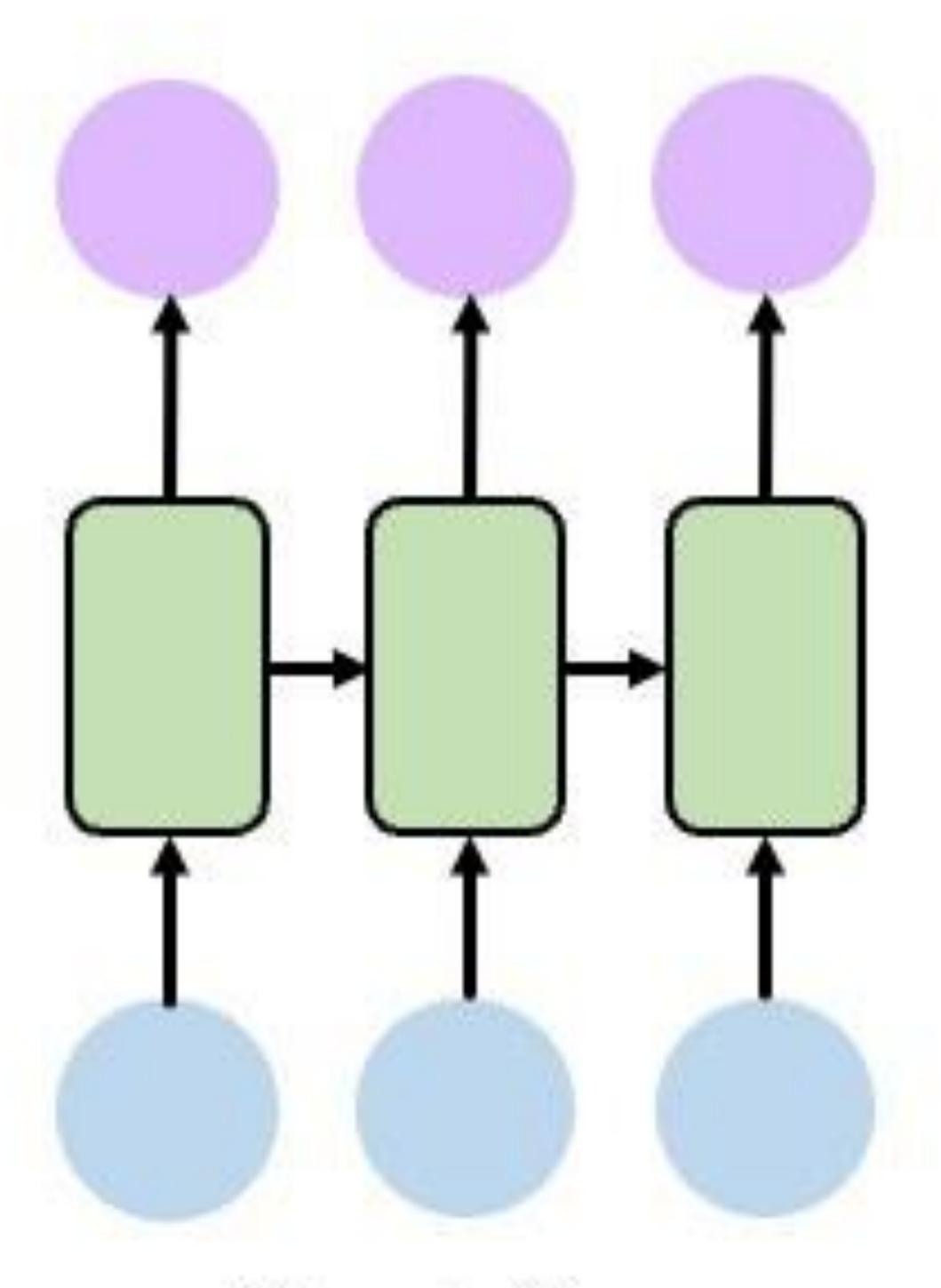
One to One "Vanilla" NN Binary classification



Many to One Sentiment Classification



One to Many Text Generation Image Captioning



Many to Many
Translation & Forecasting
Music Generation

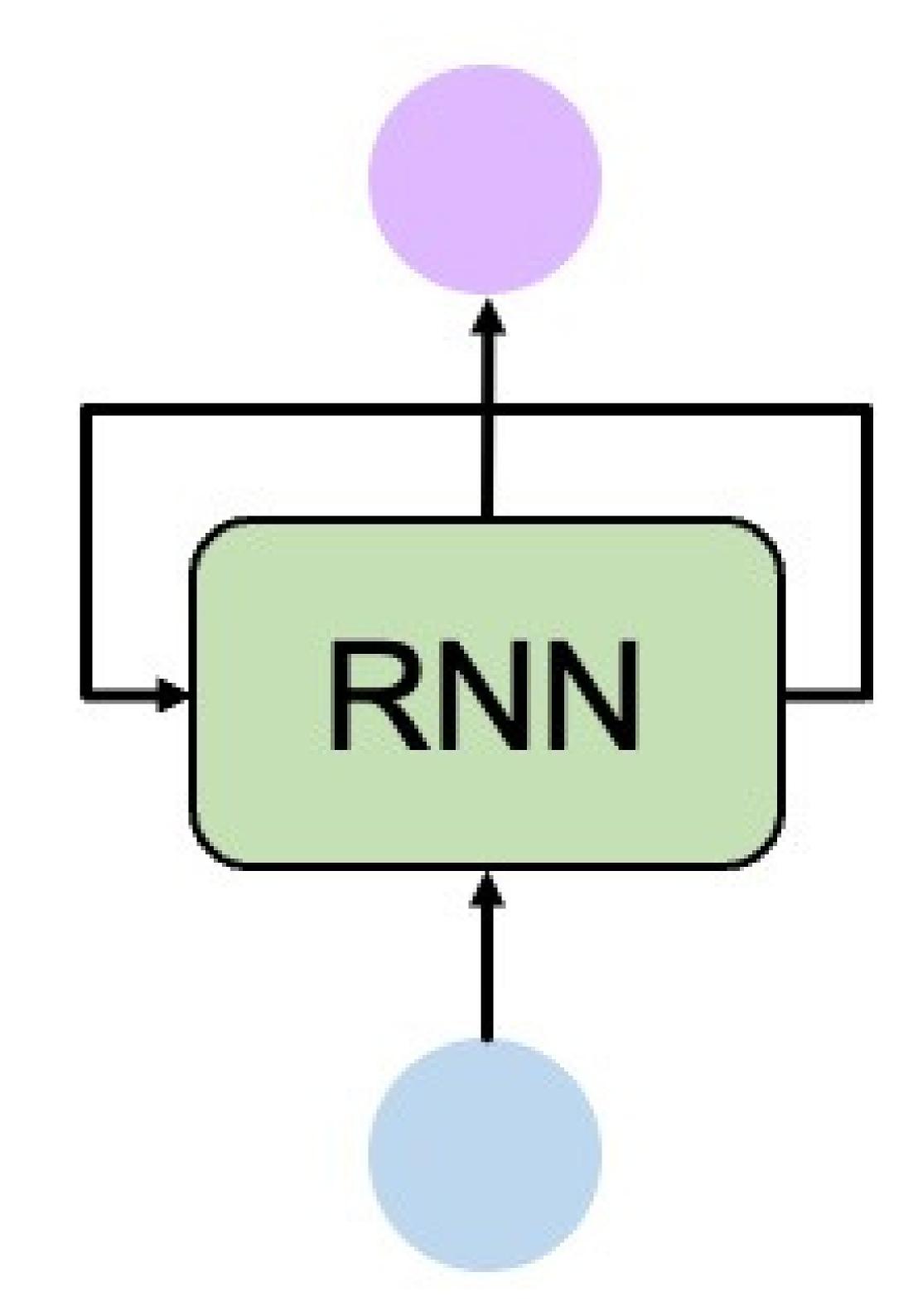


... and many other architectures and applications

Sequence Modeling: Design Criteria

To model sequences, we need to:

- 1. Handle variable-length sequences
- 2. Track long-term dependencies
- 3. Maintain information about order
- 4. Share parameters across the sequence



Recurrent Neural Networks (RNNs) meet these sequence modeling design criteria

"This morning I took my cat for a walk."

"This morning I took my cat for a walk."

given these words

```
"This morning I took my cat for a walk."

given these words

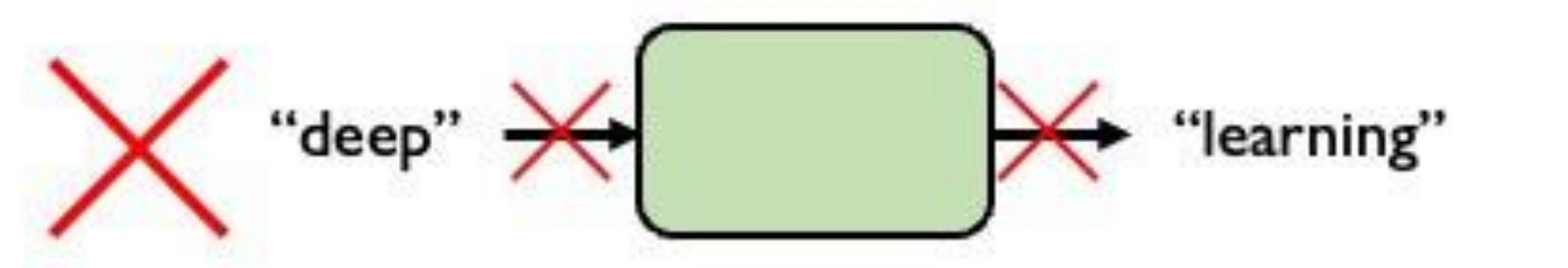
predict the
next word
```

"This morning I took my cat for a walk."

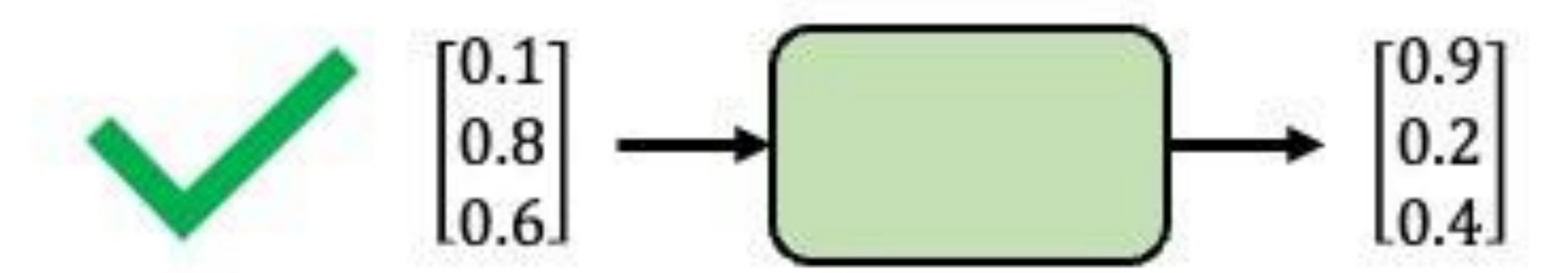
given these words

predict the
next word

Representing Language to a Neural Network

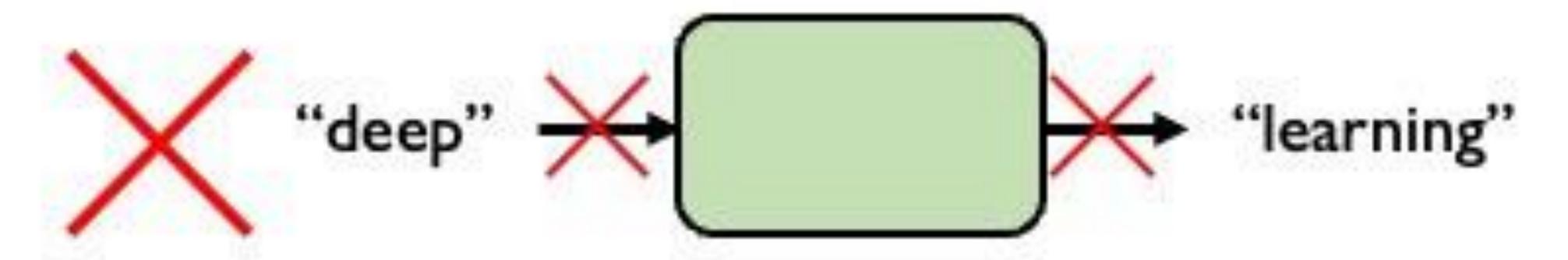


Neural networks cannot interpret words

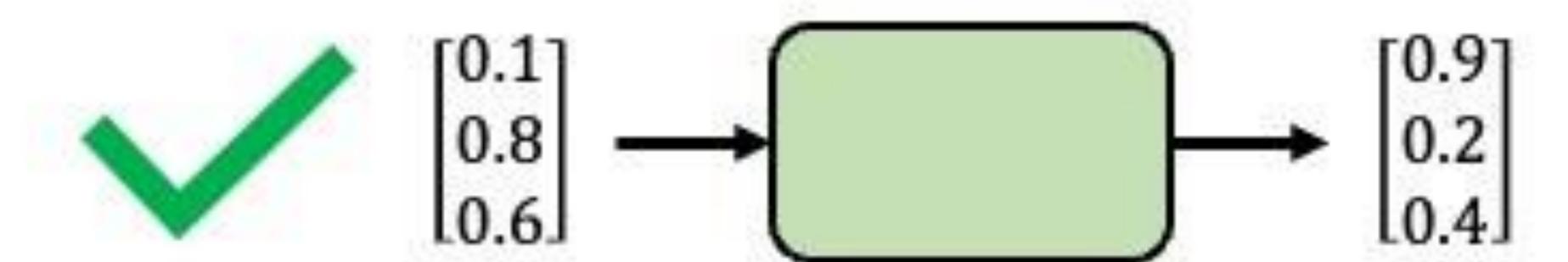


Neural networks require numerical inputs

Encoding Language for a Neural Network

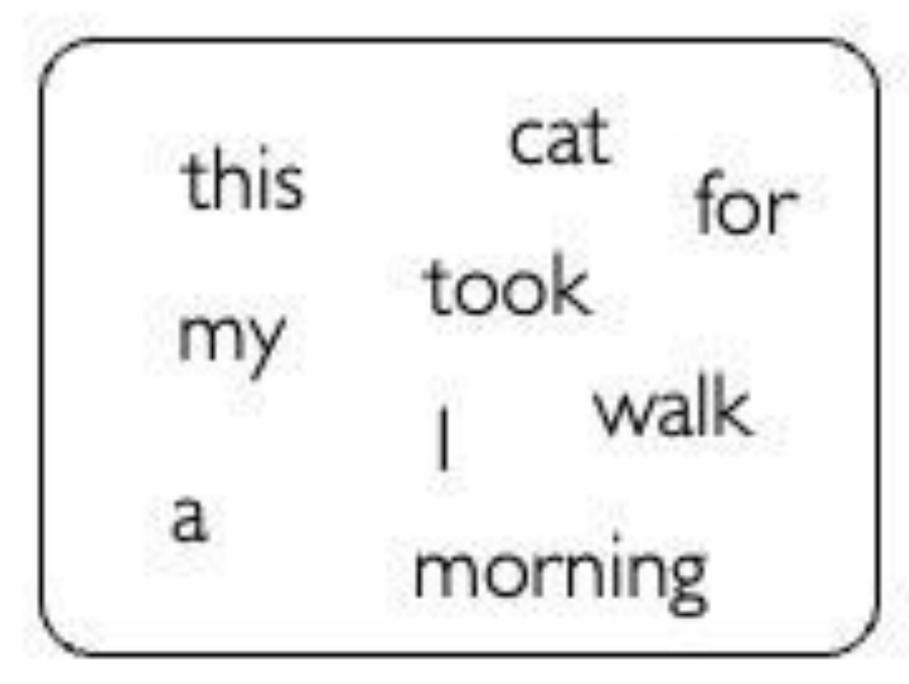


Neural networks cannot interpret words

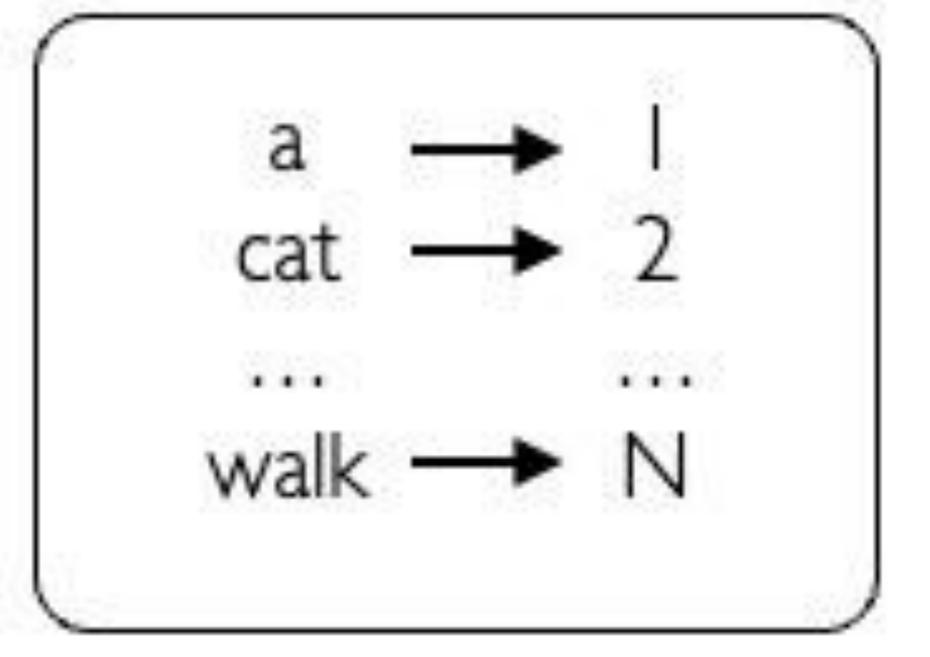


Neural networks require numerical inputs

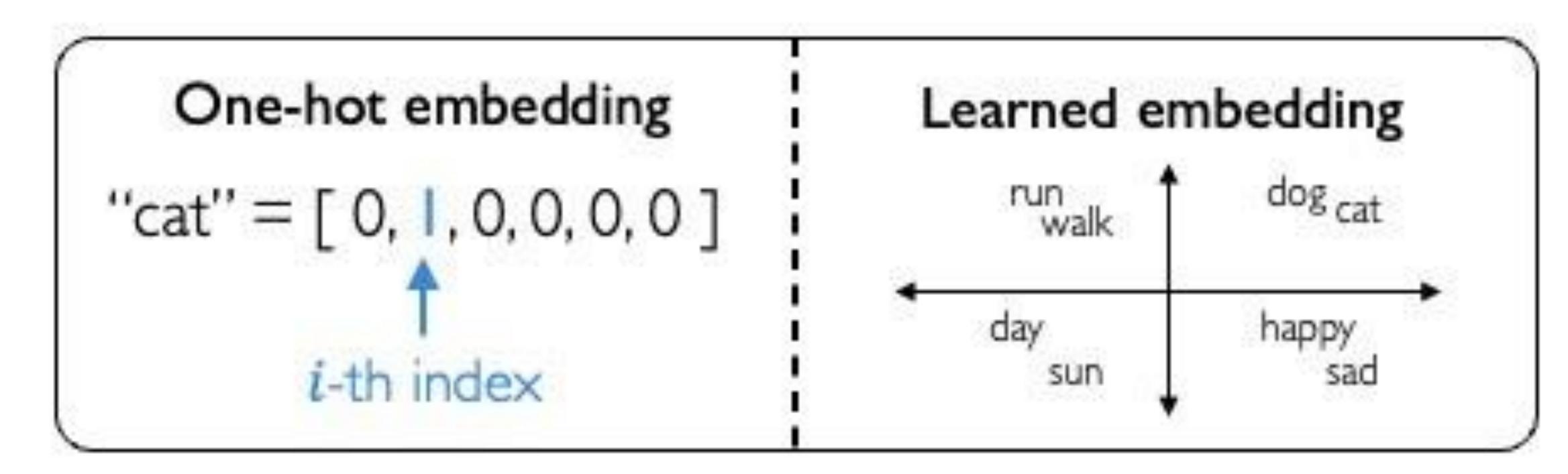
Embedding: transform indexes into a vector of fixed size.



Corpus of words



2. Indexing: Word to index



3. Embedding: Index to fixed-sized vector

Handle Variable Sequence Lengths

The food was great

VS.

We visited a restaurant for <u>lunch</u>

VS.

We were hungry but cleaned the house before eating

Model Long-Term Dependencies

"France is where I grew up, but I now live in Boston. I speak fluent ___."

We need information from **the distant past** to accurately predict the correct word.

Capture Differences in Sequence Order



The state of the s

The food was good, not bad at all.

VS.

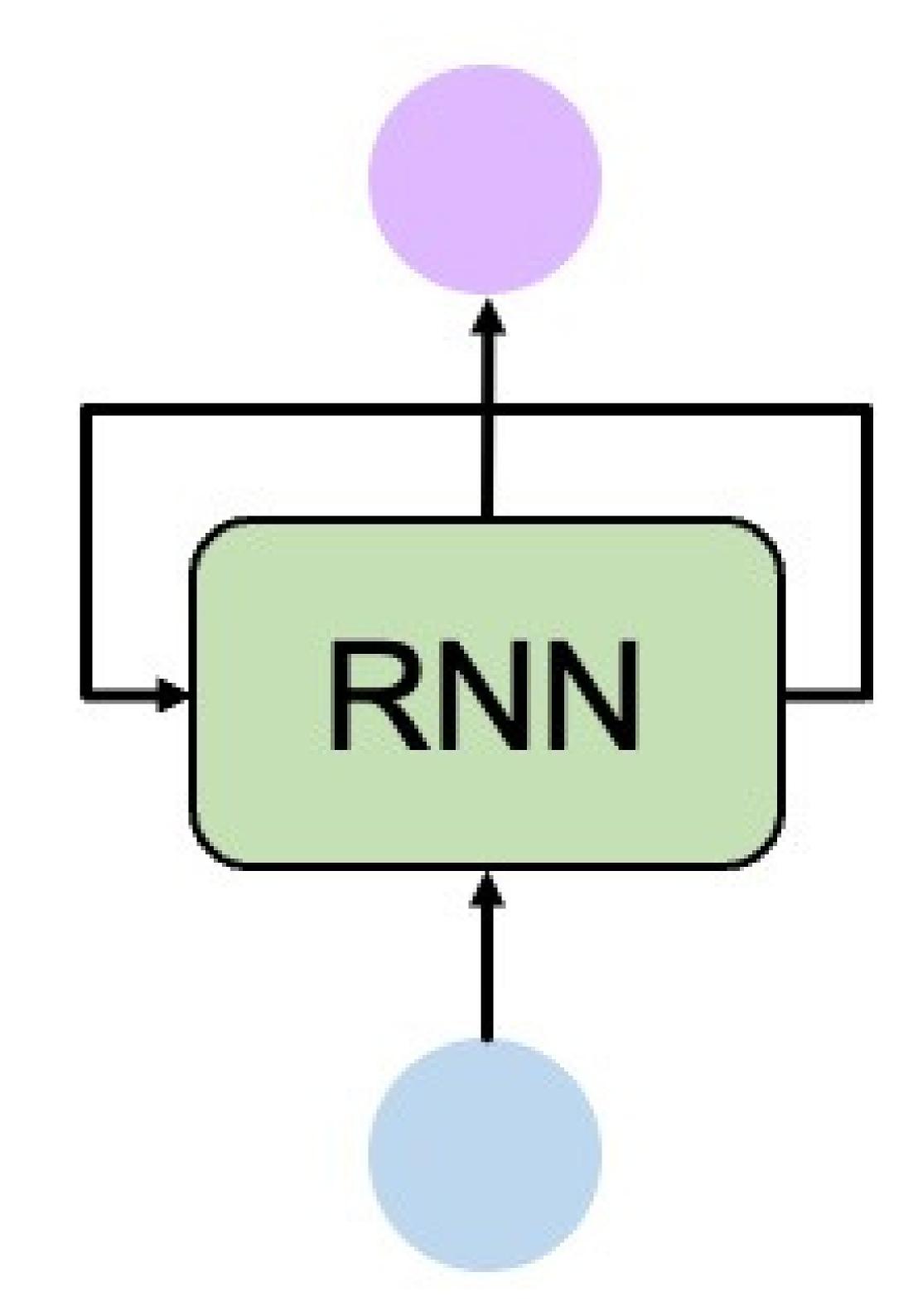
The food was bad, not good at all.



Sequence Modeling: Design Criteria

To model sequences, we need to:

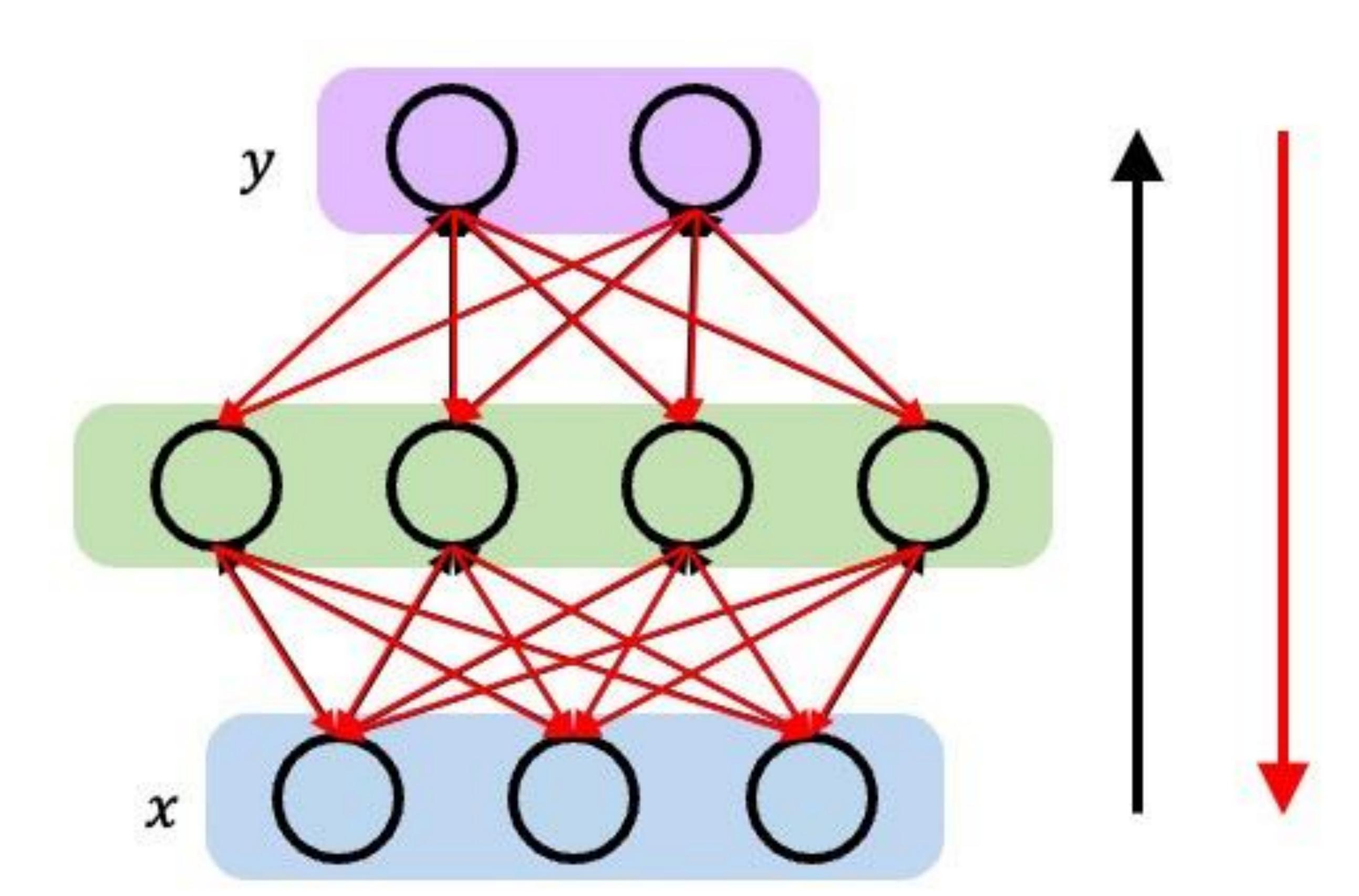
- 1. Handle variable-length sequences
- 2. Track long-term dependencies
- 3. Maintain information about order
- 4. Share parameters across the sequence



Recurrent Neural Networks (RNNs) meet these sequence modeling design criteria

Backpropagation Through Time (BPTT)

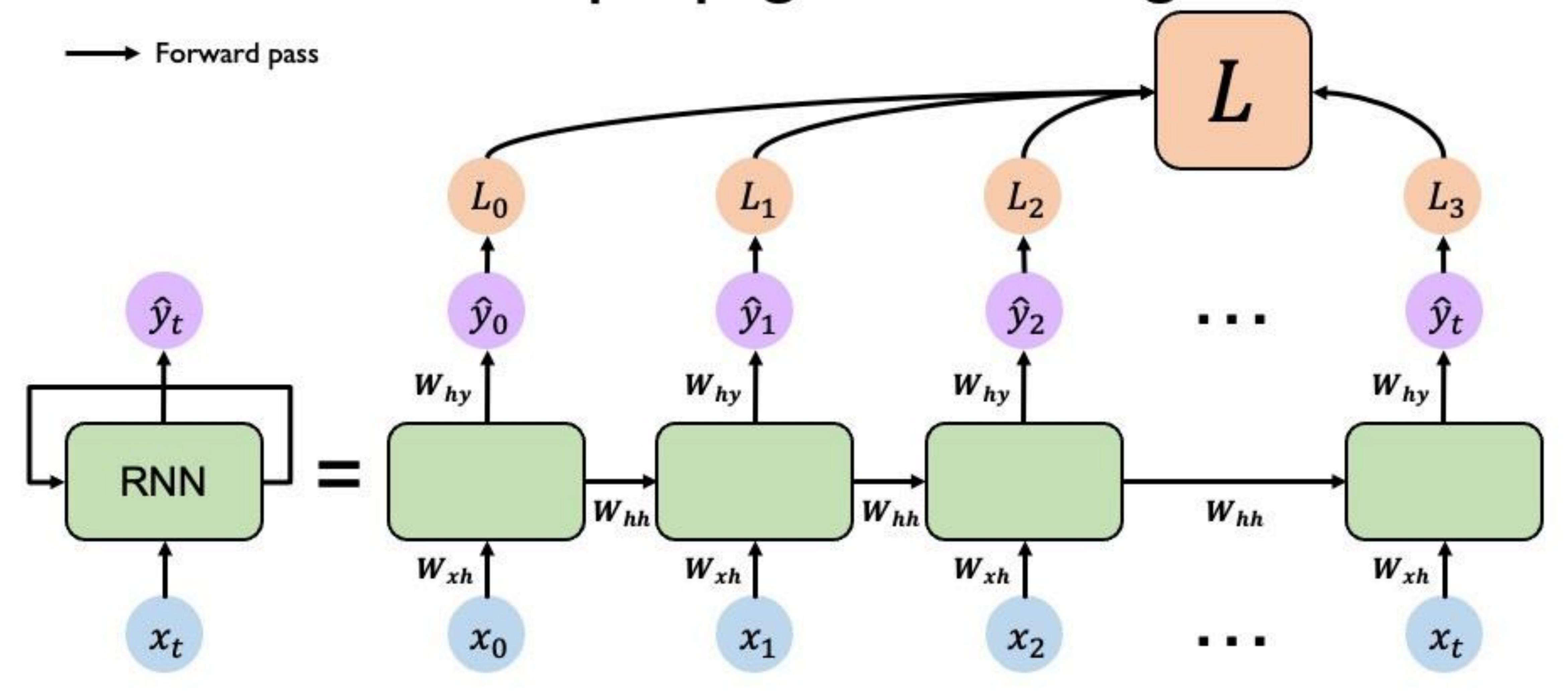
Recall: Backpropagation in Feed Forward Models



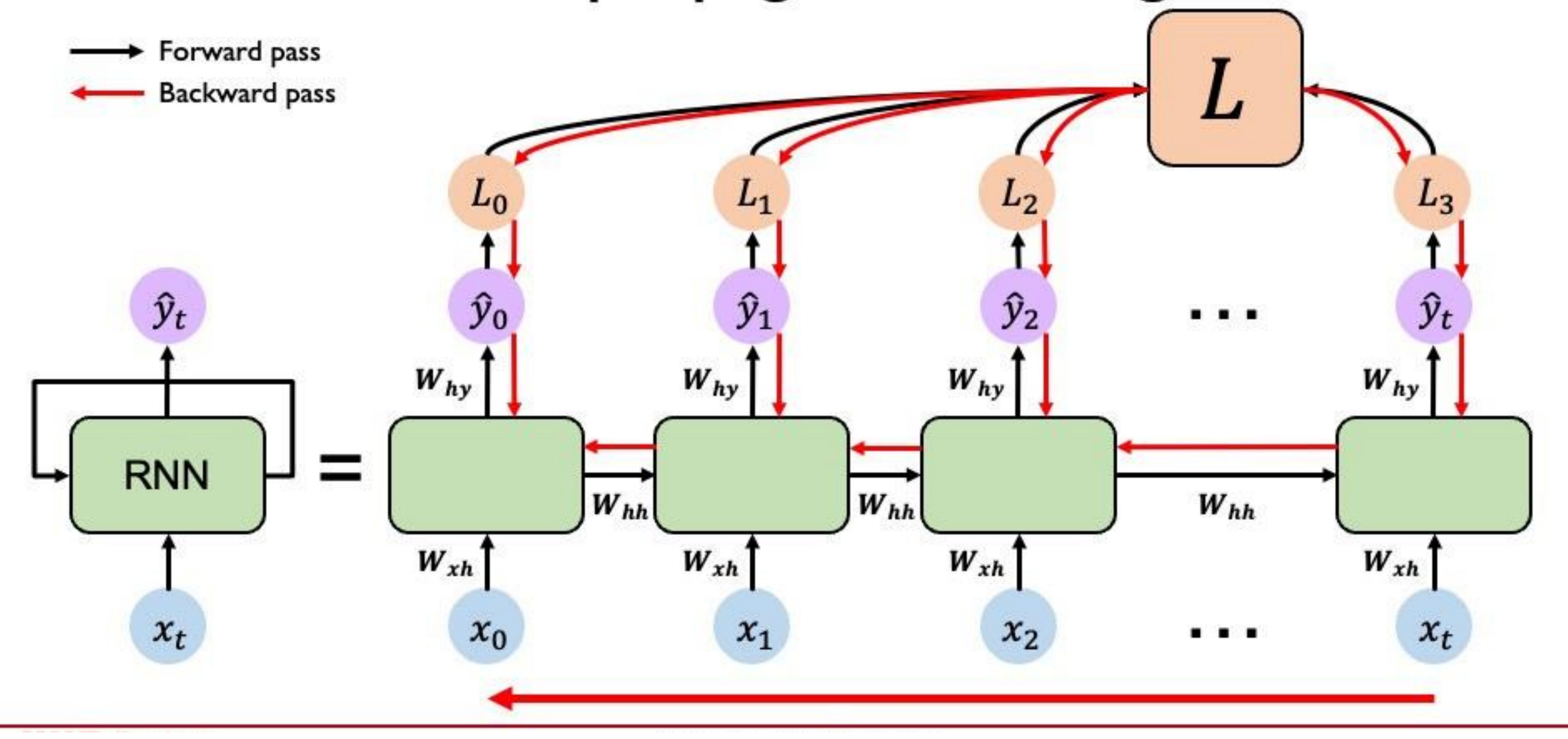
Backpropagation algorithm:

- Take the derivative (gradient) of the loss with respect to each parameter
- Shift parameters in order to minimize loss

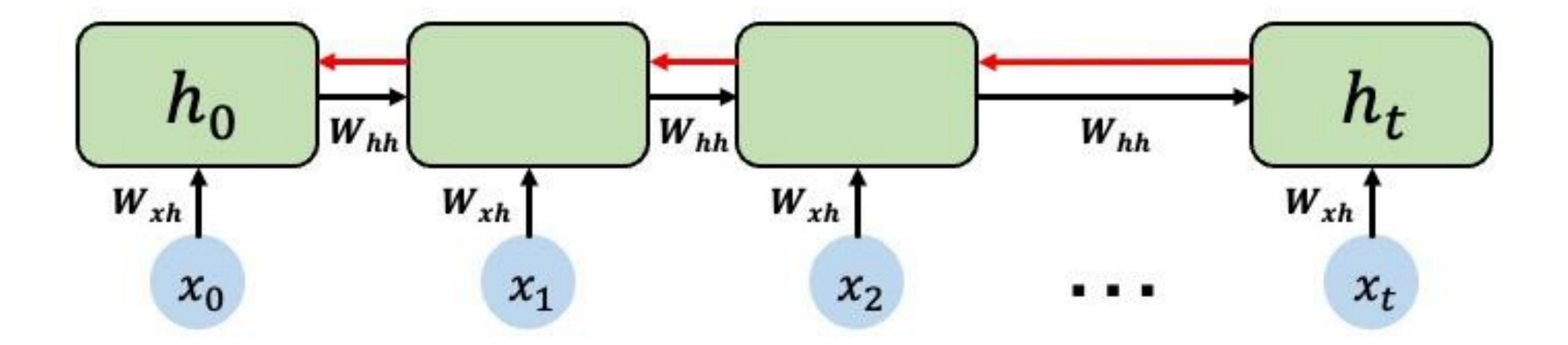
RNNs: Backpropagation Through Time



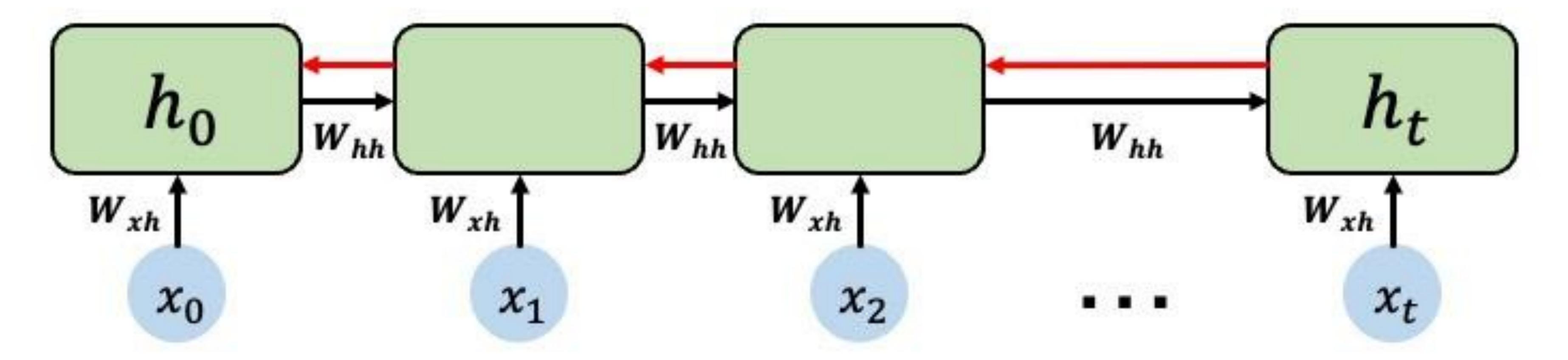
RNNs: Backpropagation Through Time



Standard RNN Gradient Flow

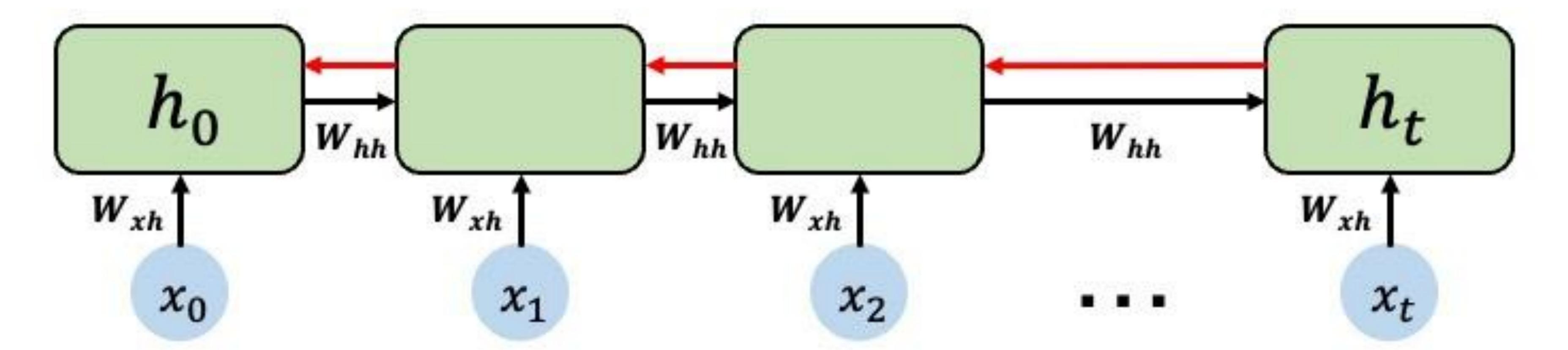


Standard RNN Gradient Flow



Computing the gradient wrt h_0 involves many factors of W_{hh} + repeated gradient computation!

Standard RNN Gradient Flow: Exploding Gradients



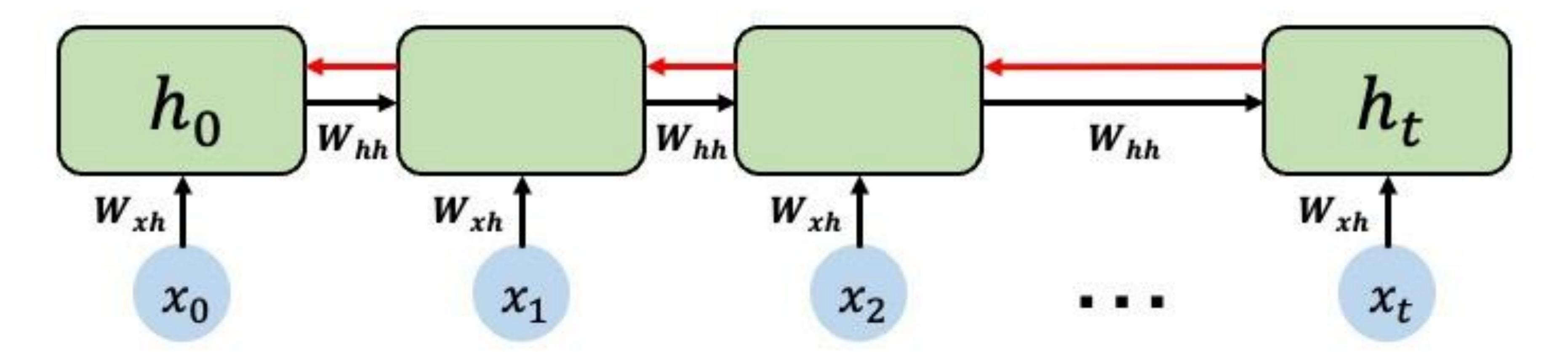
Computing the gradient wrt h_0 involves many factors of W_{hh} + repeated gradient computation!

Many values > 1:

exploding gradients

Gradient clipping to scale big gradients

Standard RNN Gradient Flow: Vanishing Gradients



Computing the gradient wrt h_0 involves many factors of W_{hh} + repeated gradient computation!

Many values > 1;
exploding gradients

Gradient clipping to scale big gradients

Many values < 1: vanishing gradients

- 1. Activation function
- 2. Weight initialization
- 3. Network architecture

Why are vanishing gradients a problem?

Multiply many small numbers together

Errors due to further back time steps have smaller and smaller gradients

Bias parameters to capture short-term dependencies

"The clouds are in the ____"

Why are vanishing gradients a problem?

Multiply many small numbers together

Errors due to further back time steps have smaller and smaller gradients

Bias parameters to capture short-term dependencies

Why are vanishing gradients a problem?

Multiply many small numbers together

Errors due to further back time steps have smaller and smaller gradients

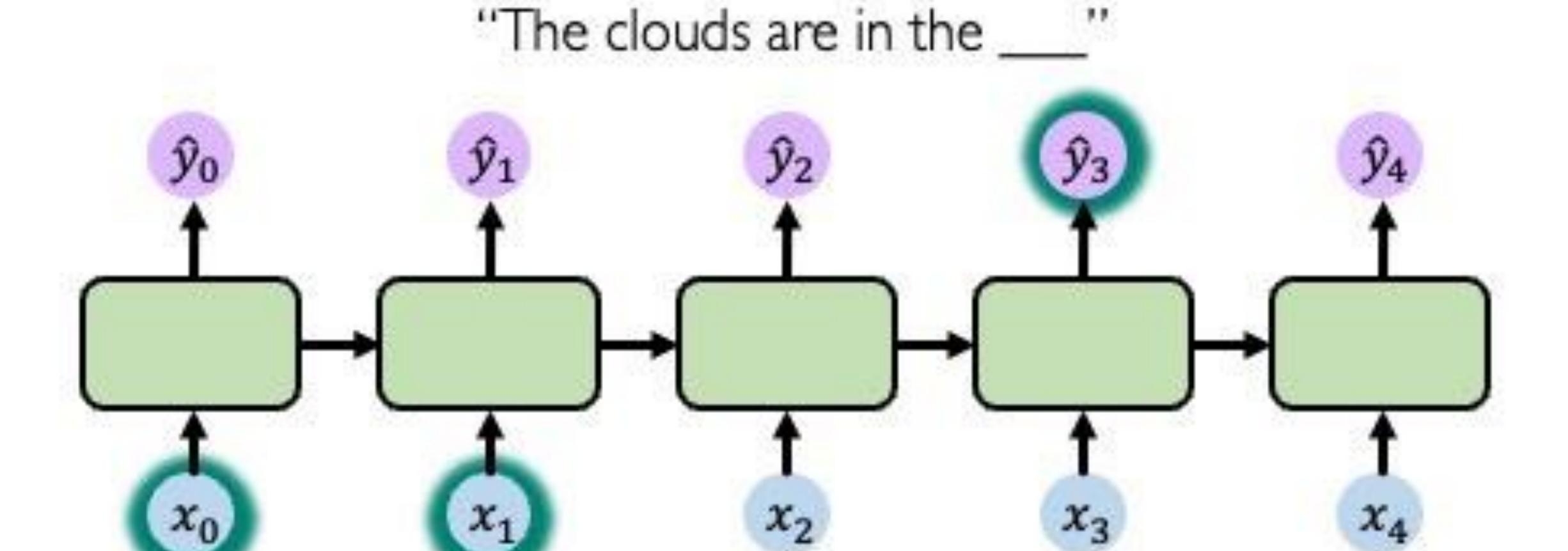
Bias parameters to capture short-term dependencies

Why are vanishing gradients a problem?

Multiply many small numbers together

Errors due to further back time steps have smaller and smaller gradients

Bias parameters to capture short-term dependencies



"I grew up in France, ... and I speak fluent___"

 x_1

Why are vanishing gradients a problem?

Multiply many small numbers together

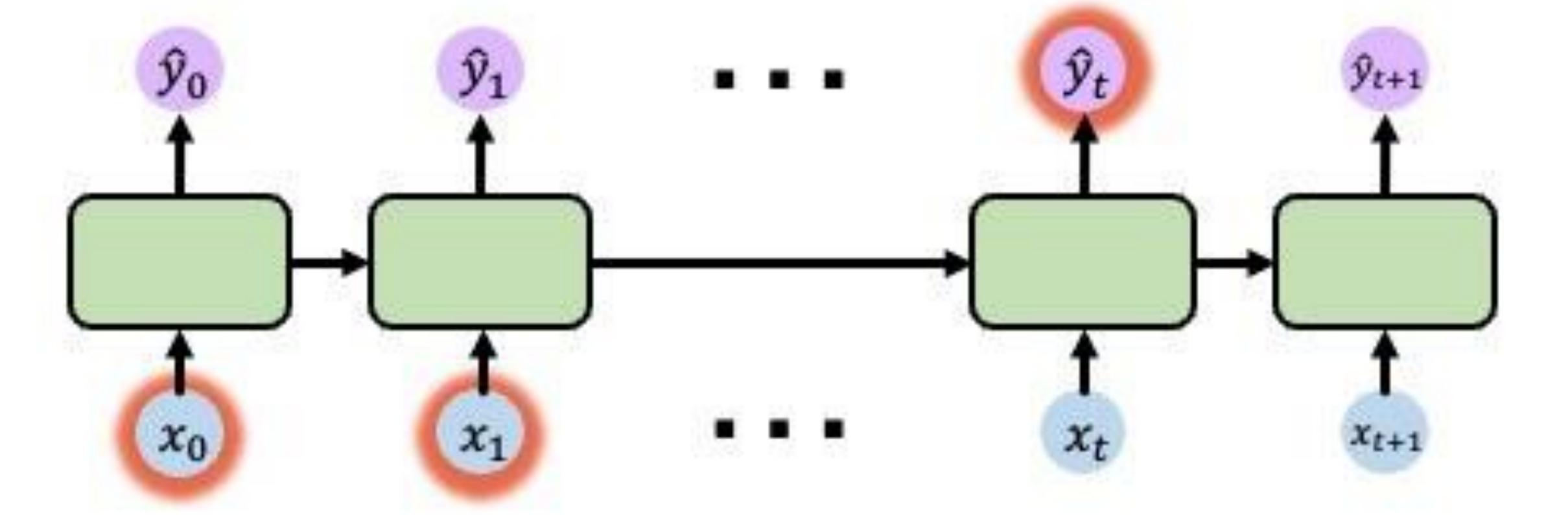
Errors due to further back time steps have smaller and smaller gradients

Bias parameters to capture short-term dependencies

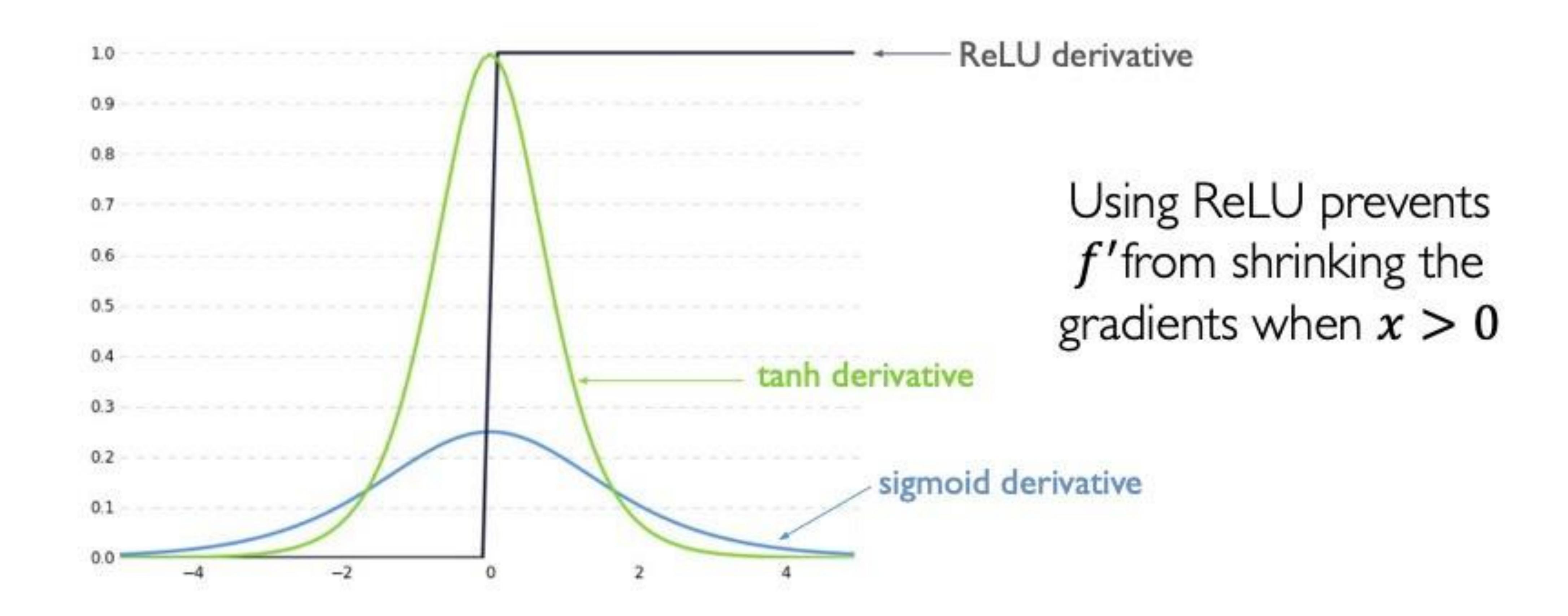
 y_0 y_1 y_2 y_3 y_4 x_0 x_1 x_2 x_3 x_4

"The clouds are in the

"I grew up in France, ... and I speak fluent___"



Trick #1: Activation Functions



Trick #2: Parameter Initialization

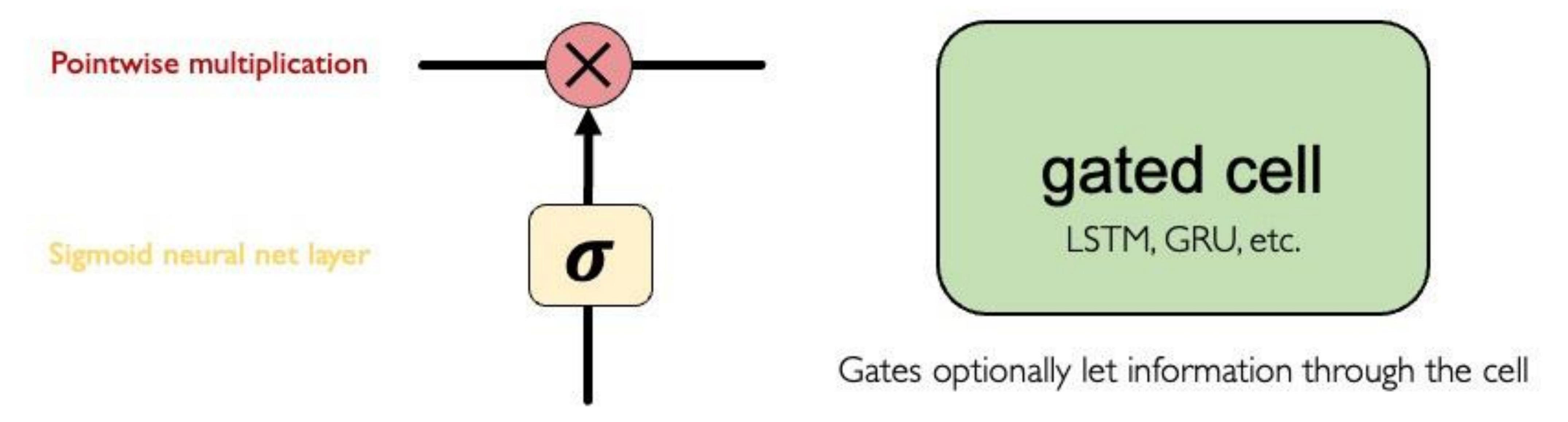
Initialize biases to zero

Initialize **weights** to identity matrix
$$I_n = \begin{pmatrix} 1 & 0 & 0 & \cdots & 0 \\ 0 & 1 & 0 & \cdots & 0 \\ 0 & 0 & 1 & \cdots & 0 \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ 0 & 0 & 0 & \cdots & 1 \end{pmatrix}$$

This helps prevent the weights from shrinking to zero.

Trick #3: Gated Cells

Idea: use gates to selectively add or remove information within each recurrent unit with

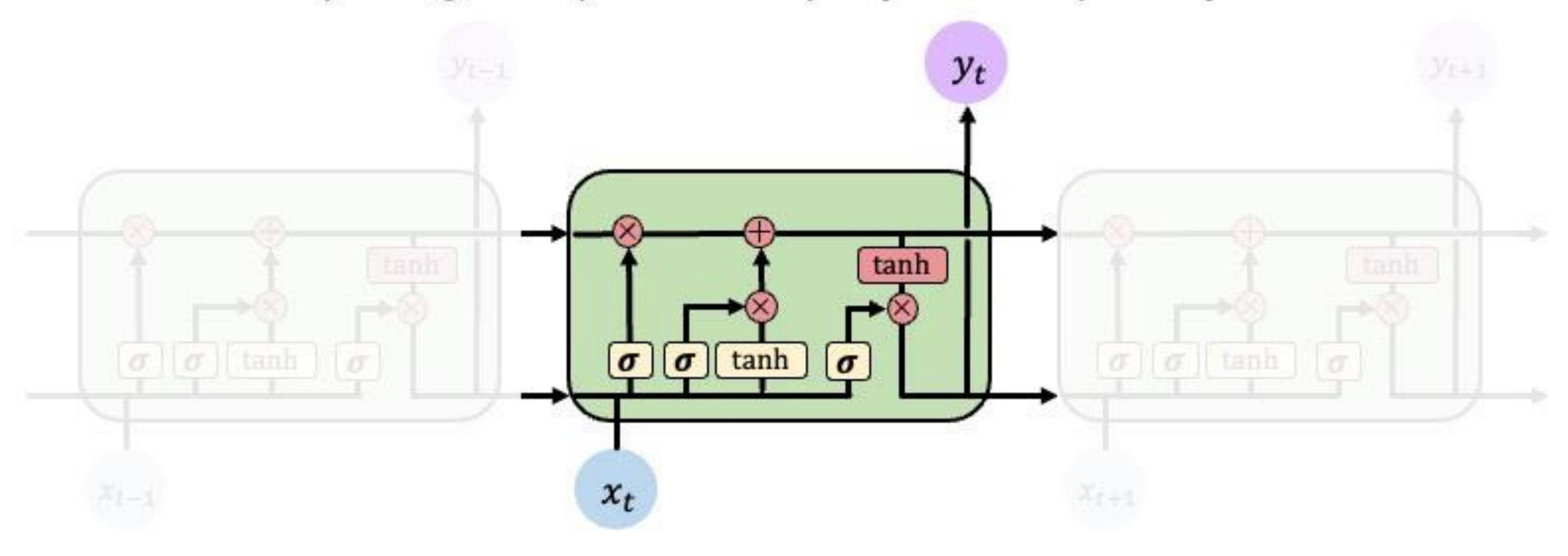


Long Short Term Memory (LSTMs) networks rely on a gated cell to track information throughout many time steps.

Long Short Term Memory (LSTMs)

Gated LSTM cells control information flow:

1) Forget 2) Store 3) Update 4) Output



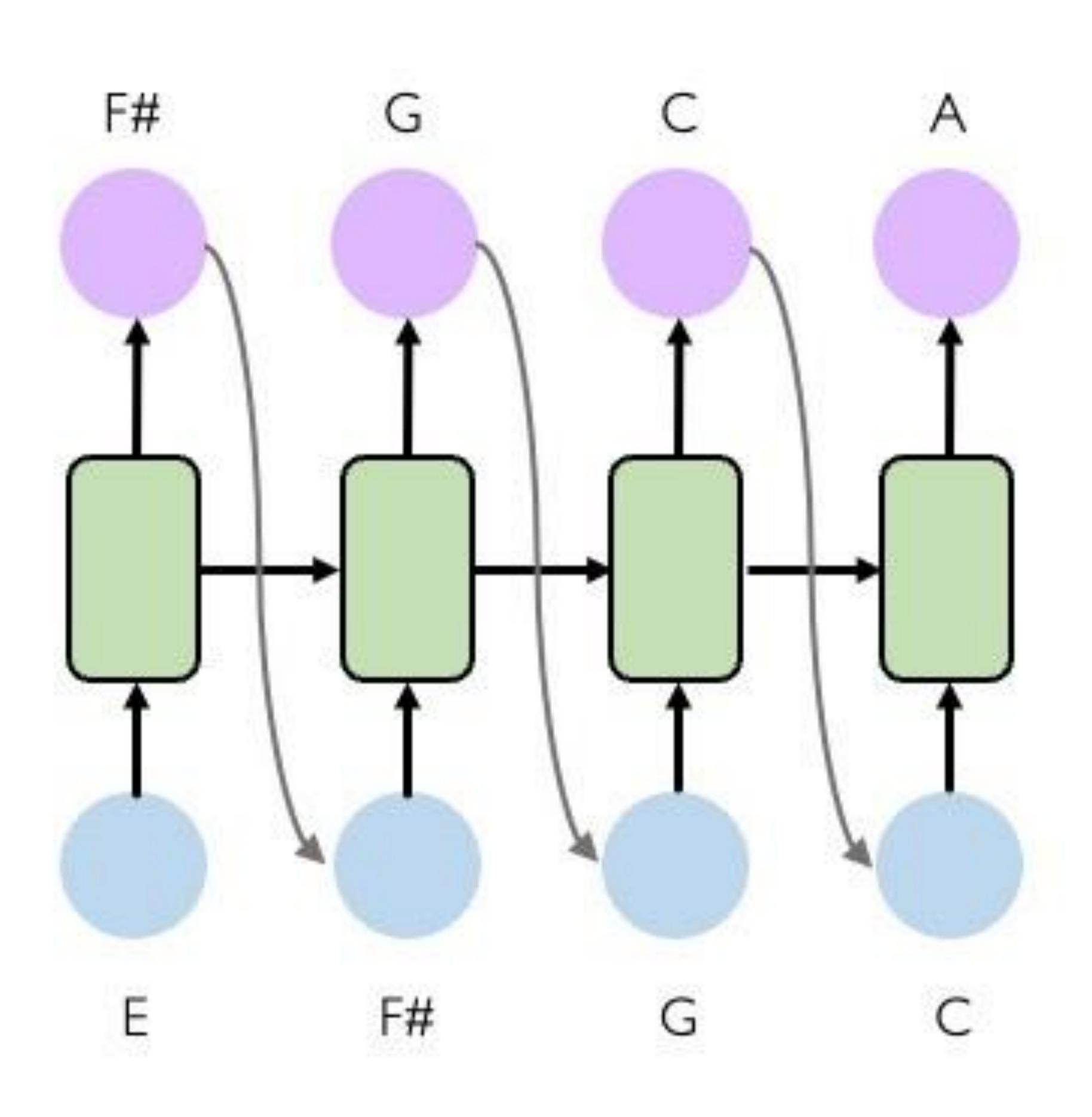
LSTM cells are able to track information throughout many timesteps

LSTMs: Key Concepts

- 1. Maintain a cell state
- 2. Use gates to control the flow of information
 - Forget gate gets rid of irrelevant information
 - Store relevant information from current input
 - Selectively update cell state
 - Output gate returns a filtered version of the cell state
- 3. Backpropagation through time with partially uninterrupted gradient flow

RNN Applications & Limitations

Example Task: Music Generation

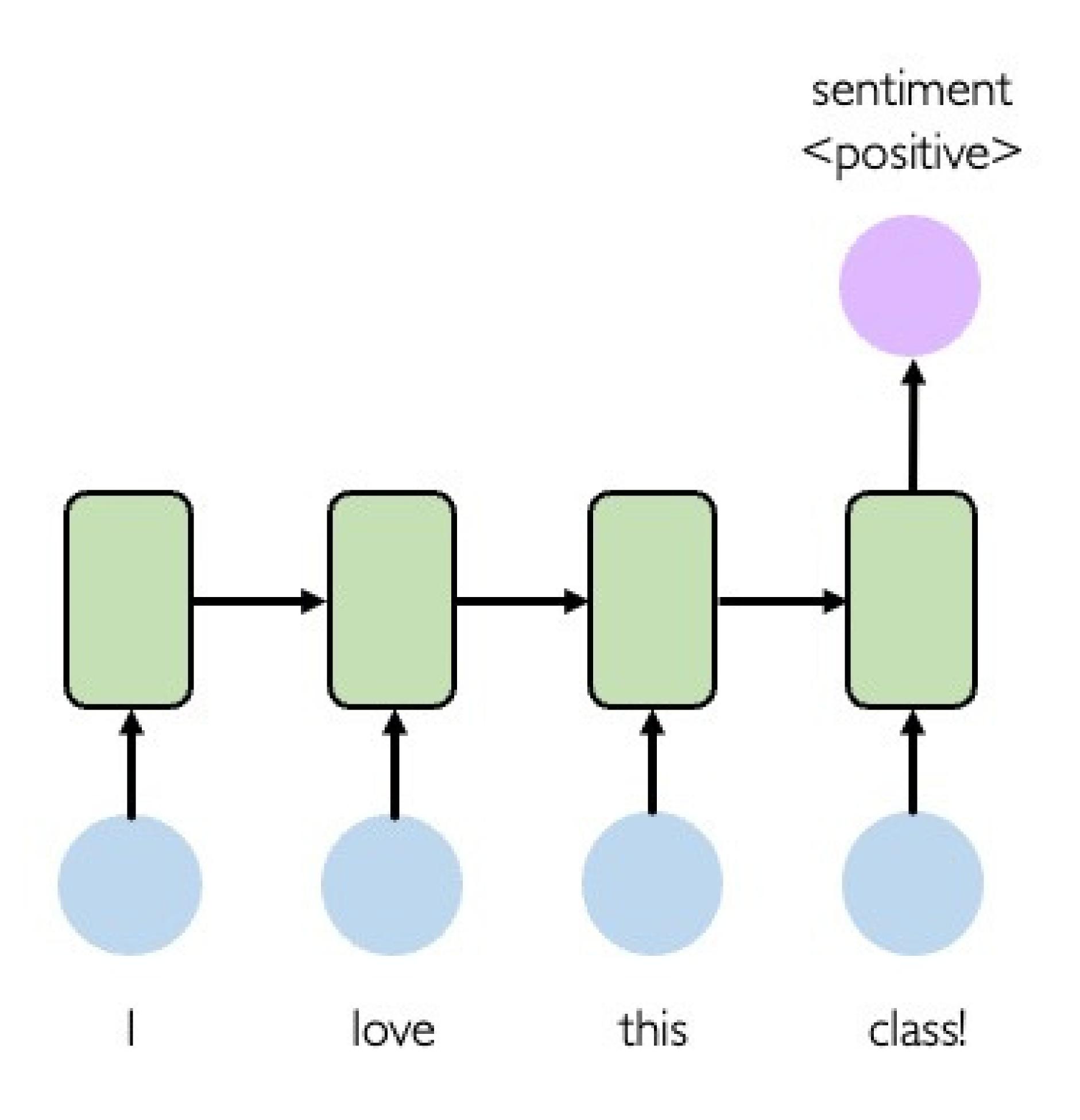


Input: sheet music

Output: next character in sheet music



Example Task: Sentiment Classification

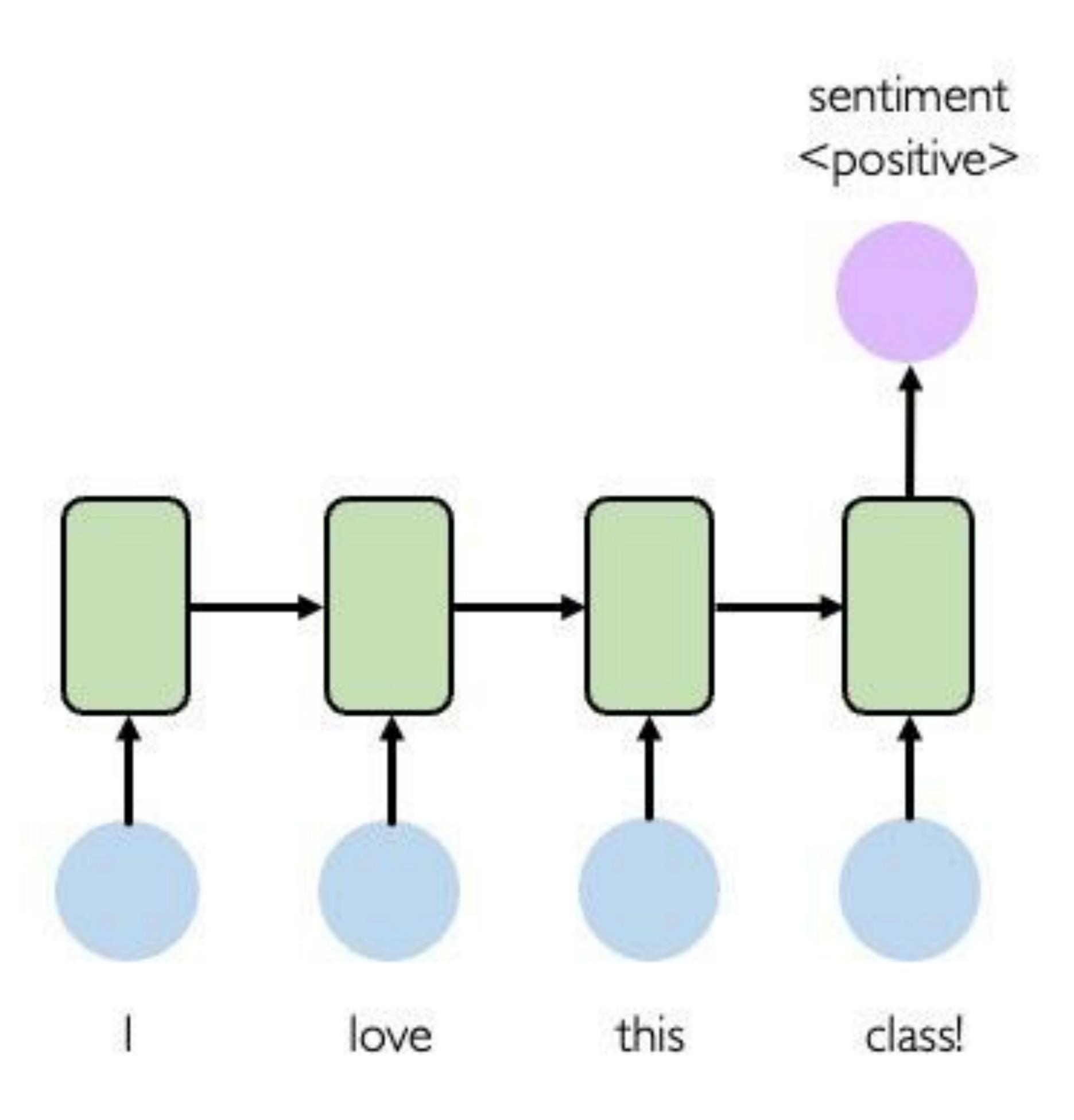


Input: sequence of words

Output: probability of having positive sentiment

loss = tf.nn.softmax_cross_entropy_with_logits(y, predicted)

Example Task: Sentiment Classification



Tweet sentiment classification





The @MIT Introduction to #DeepLearning is definitely one of the best courses of its kind currently available online introtodeeplearning.com

12:45 PM - 12 Feb 2018



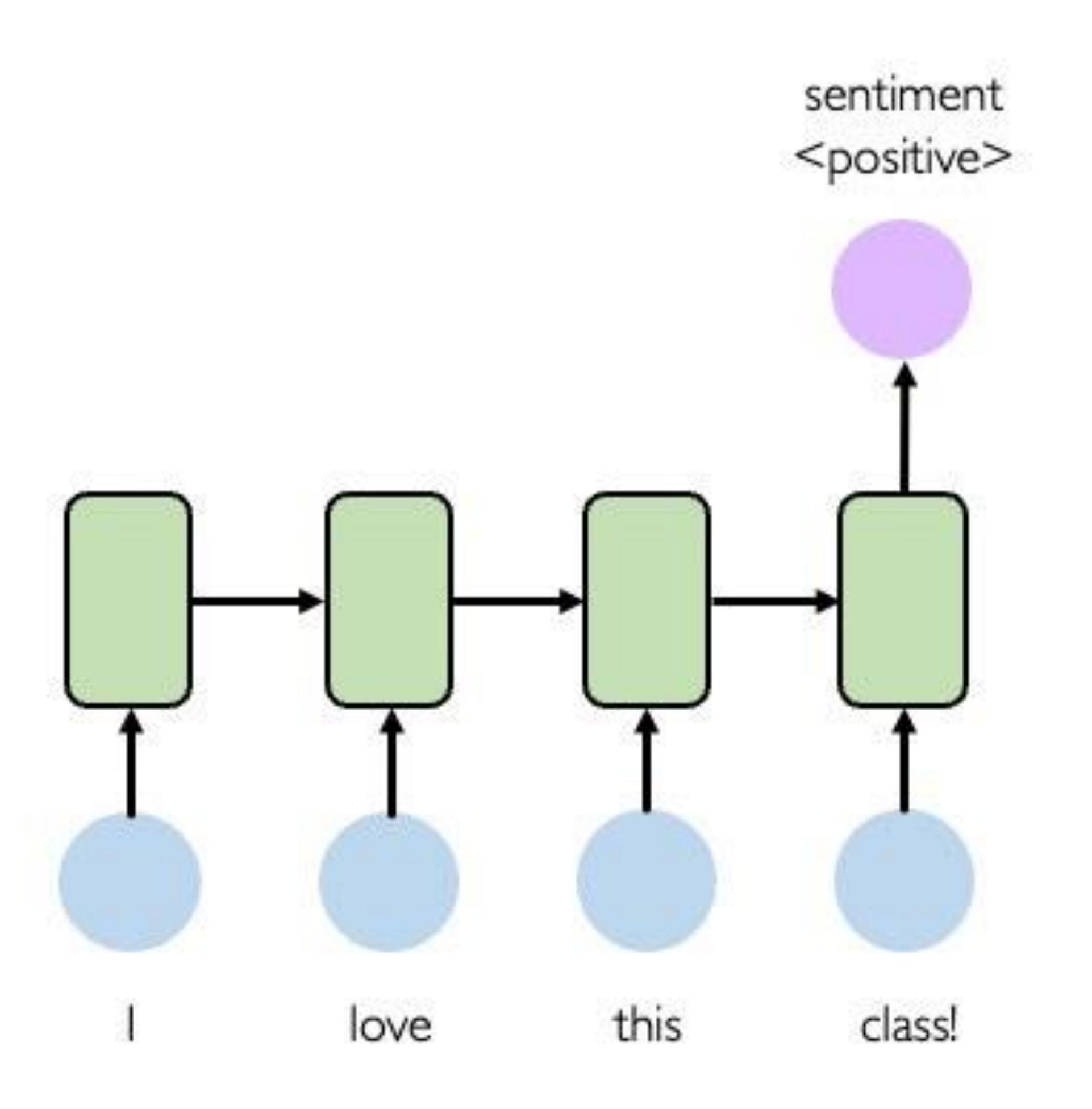


Replying to @Kazuki2048

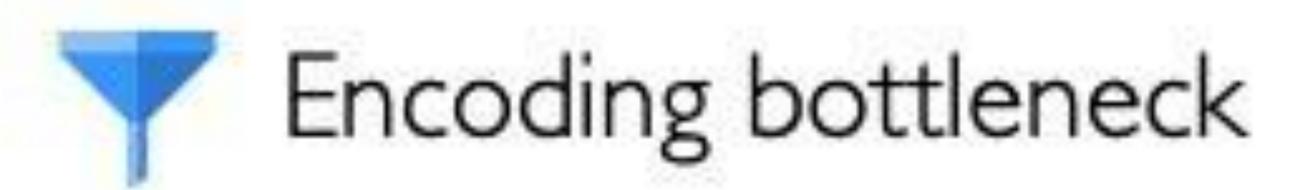
I wouldn't mind a bit of snow right now. We haven't had any in my bit of the Midlands this winter! :(

2:19 AM - 25 Jan 2019

Limitations of Recurrent Models



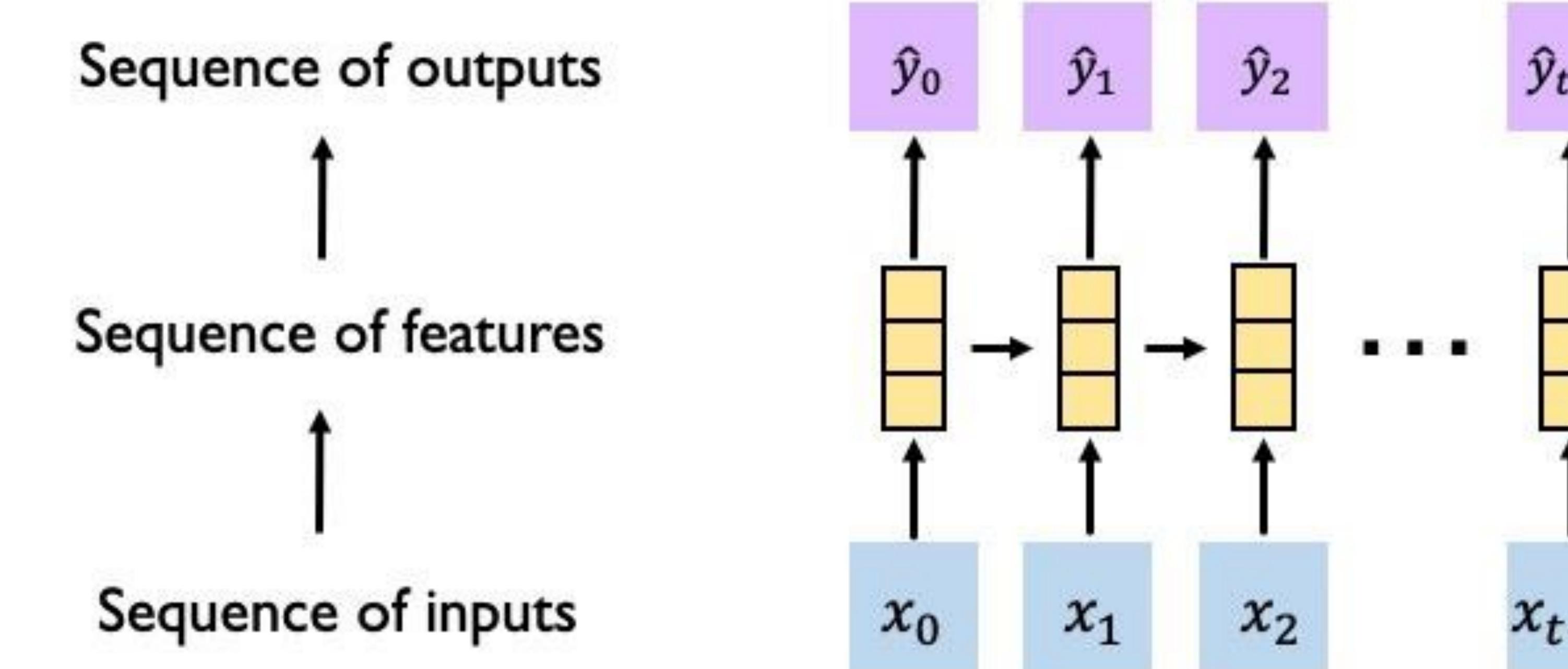
Limitations of RNNs

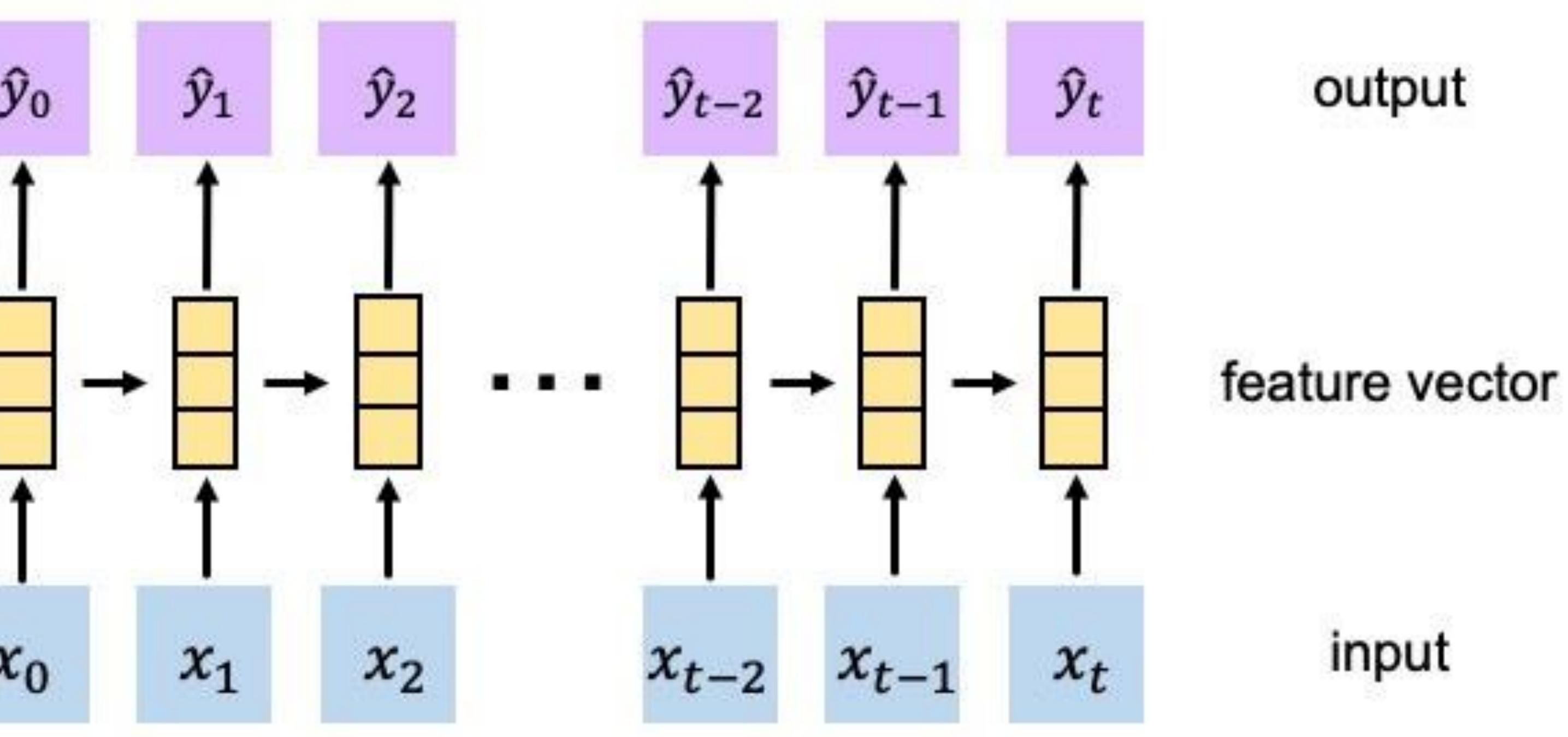


Slow, no parallelization

Not long memory

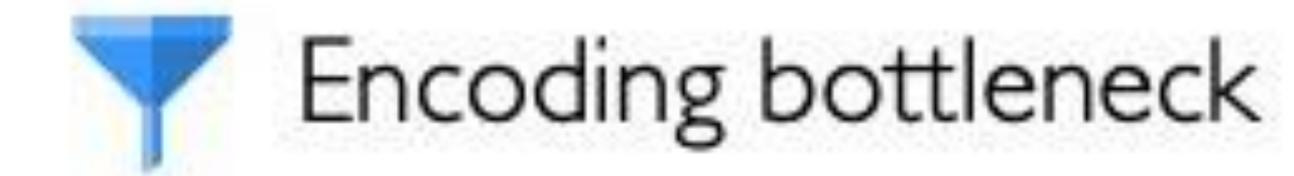
RNNs: recurrence to model sequence dependencies





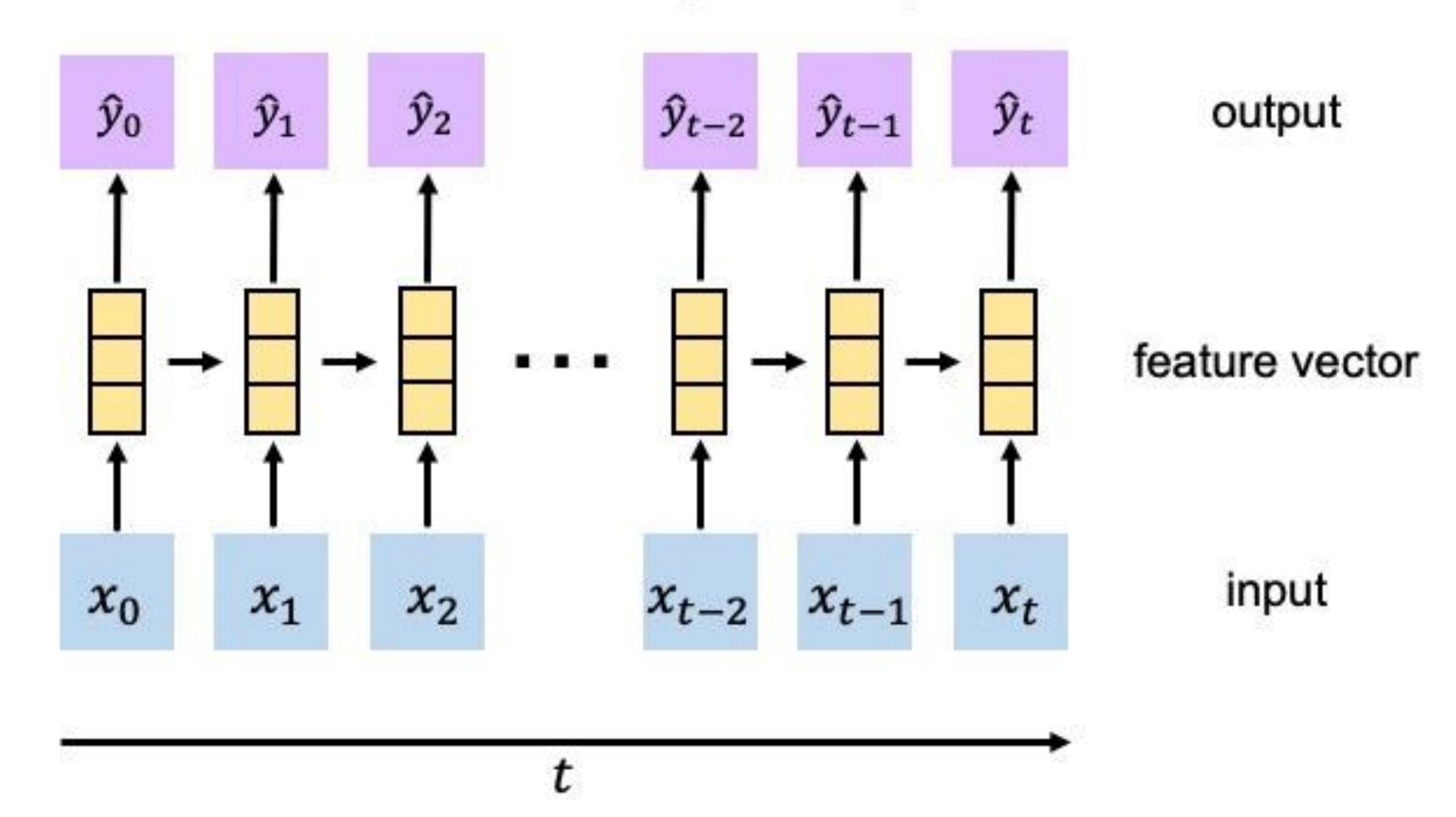
RNNs: recurrence to model sequence dependencies

Limitations of RNNs



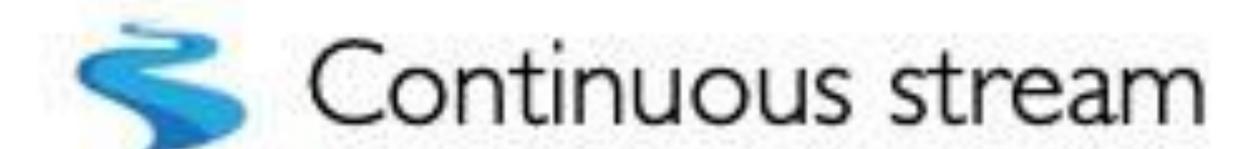
Slow, no parallelization

Not long memory



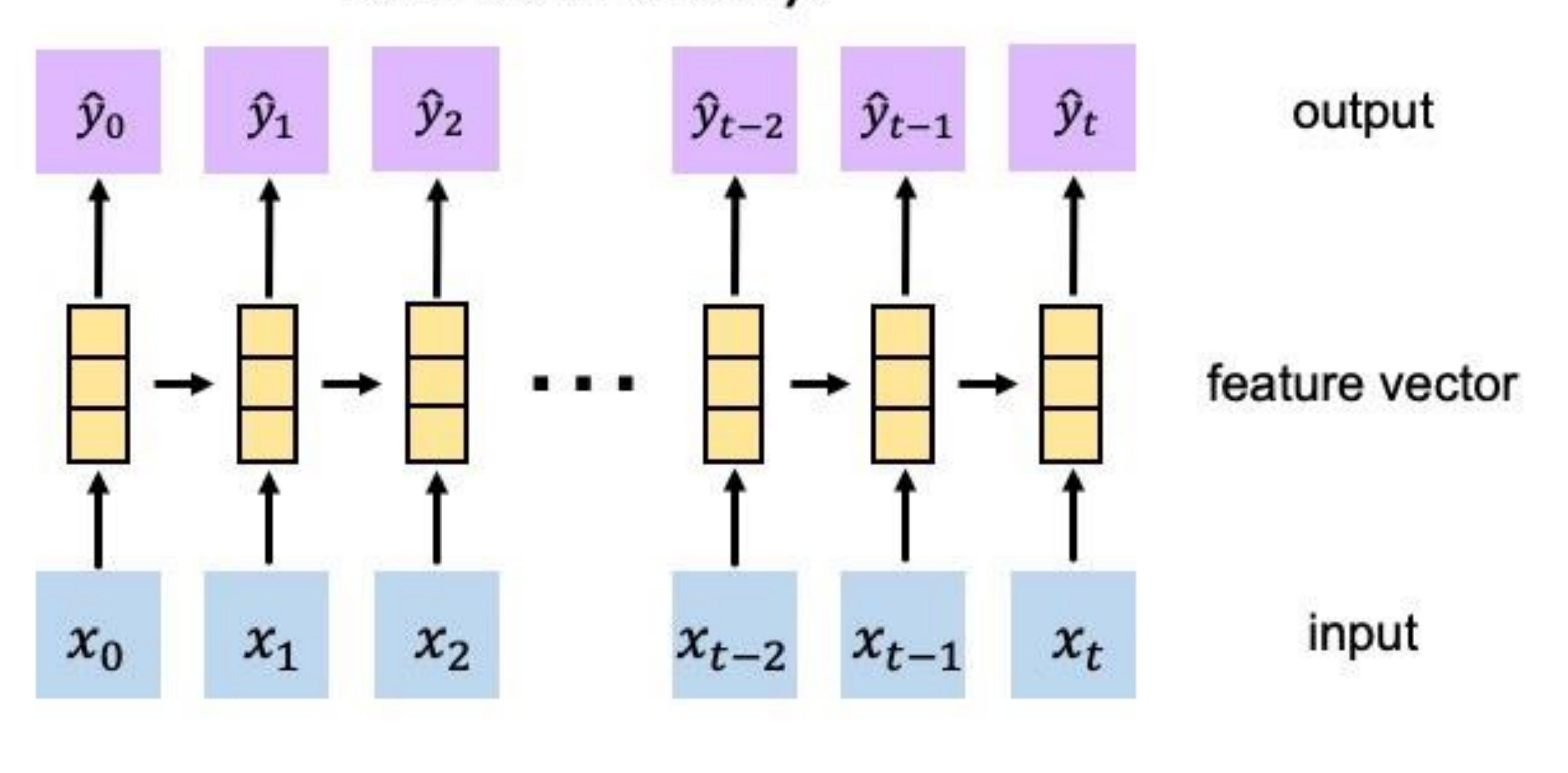
Can we eliminate the need for recurrence entirely?

Desired Capabilities



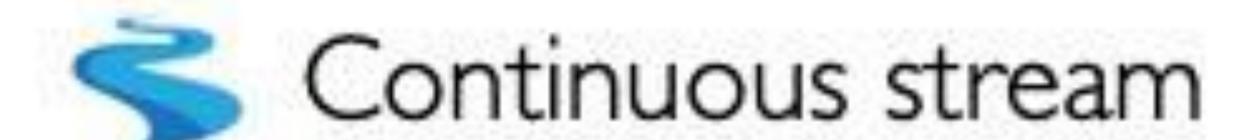


Long memory



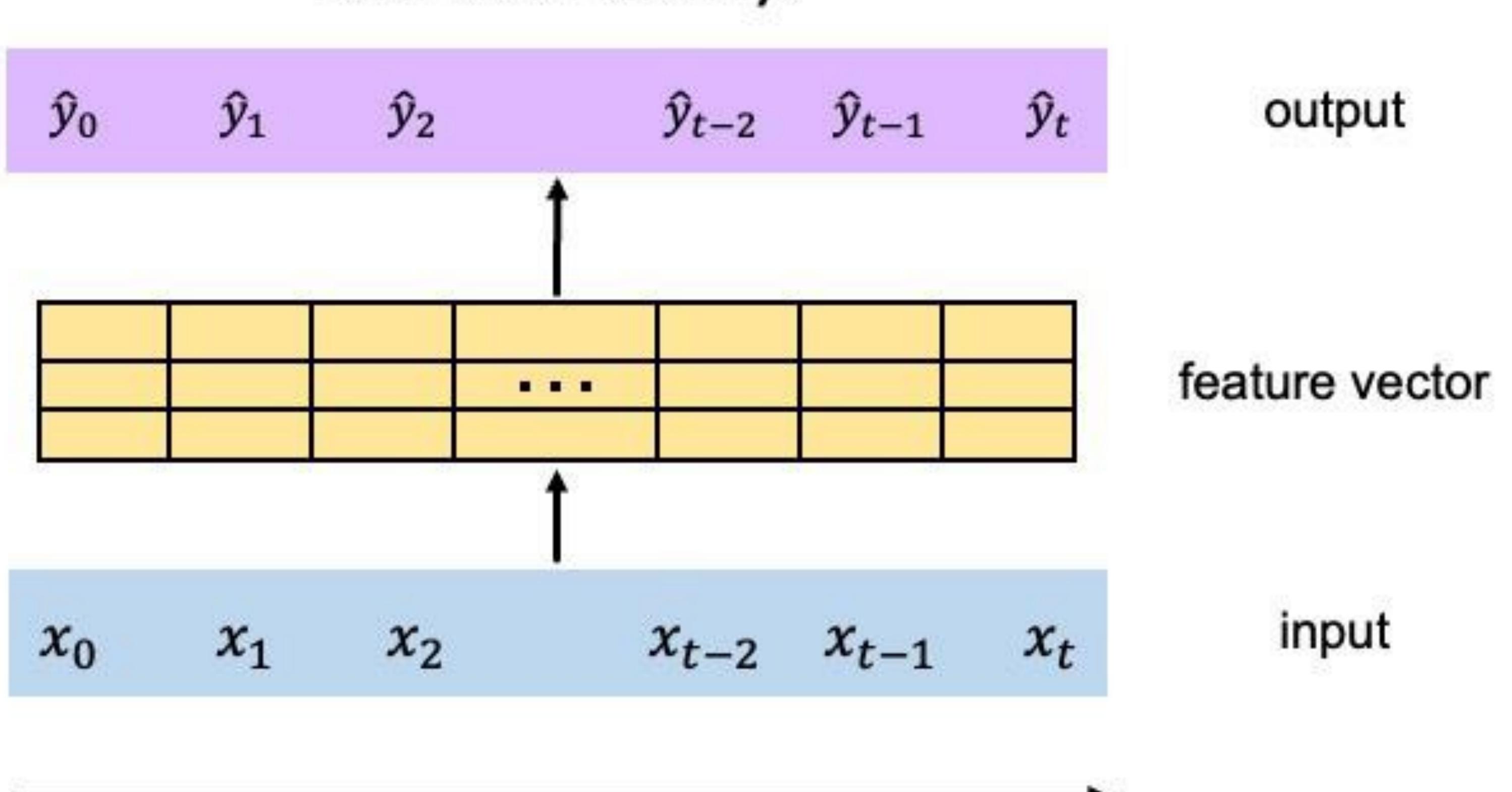
Can we eliminate the need for recurrence entirely?

Desired Capabilities





Long memory



Idea I: Feed everything into dense network



No recurrence



Not scalable



No order

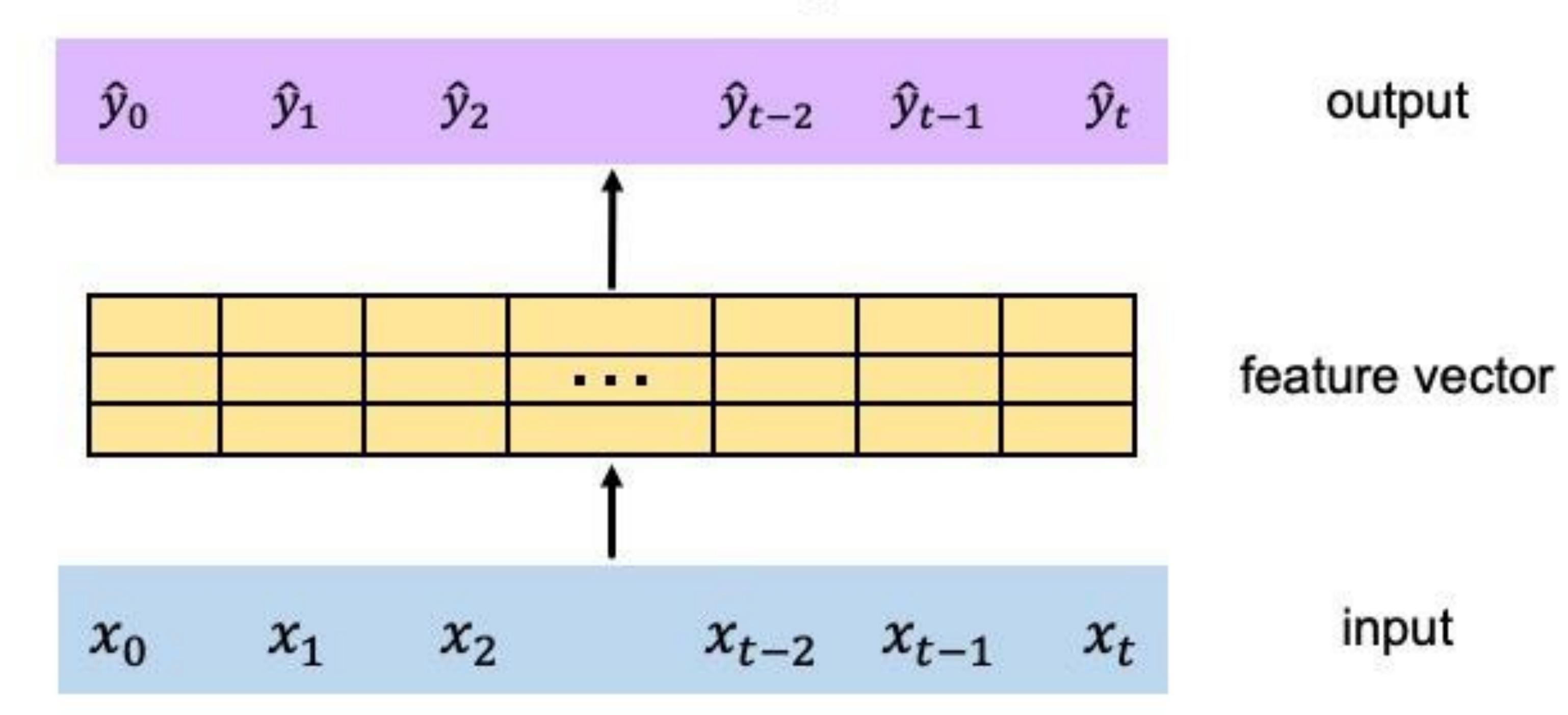


No long memory



Idea: Identify and attend to what's important

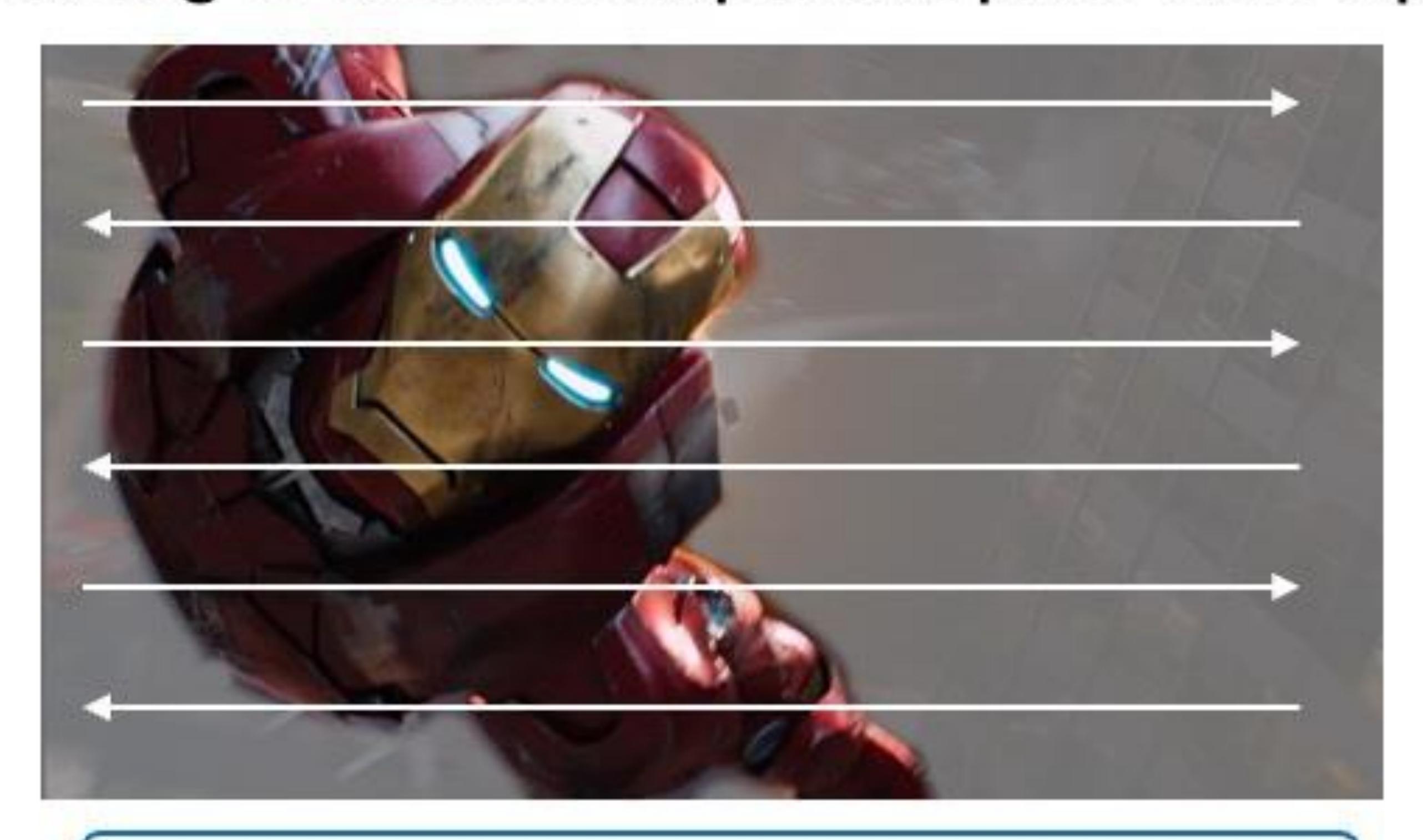
Can we eliminate the need for recurrence entirely?



Attention Is All You Need

Intuition Behind Self-Attention

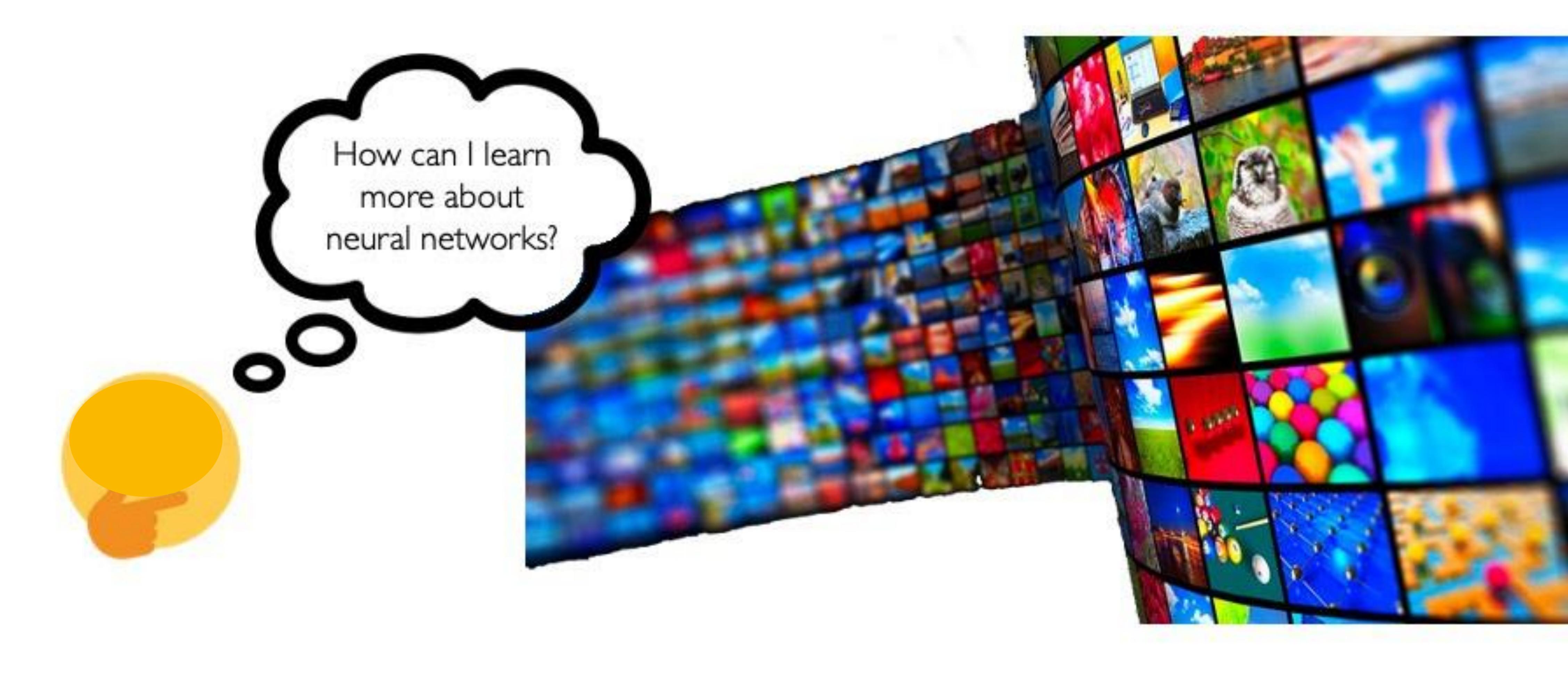
Attending to the most important parts of an input.



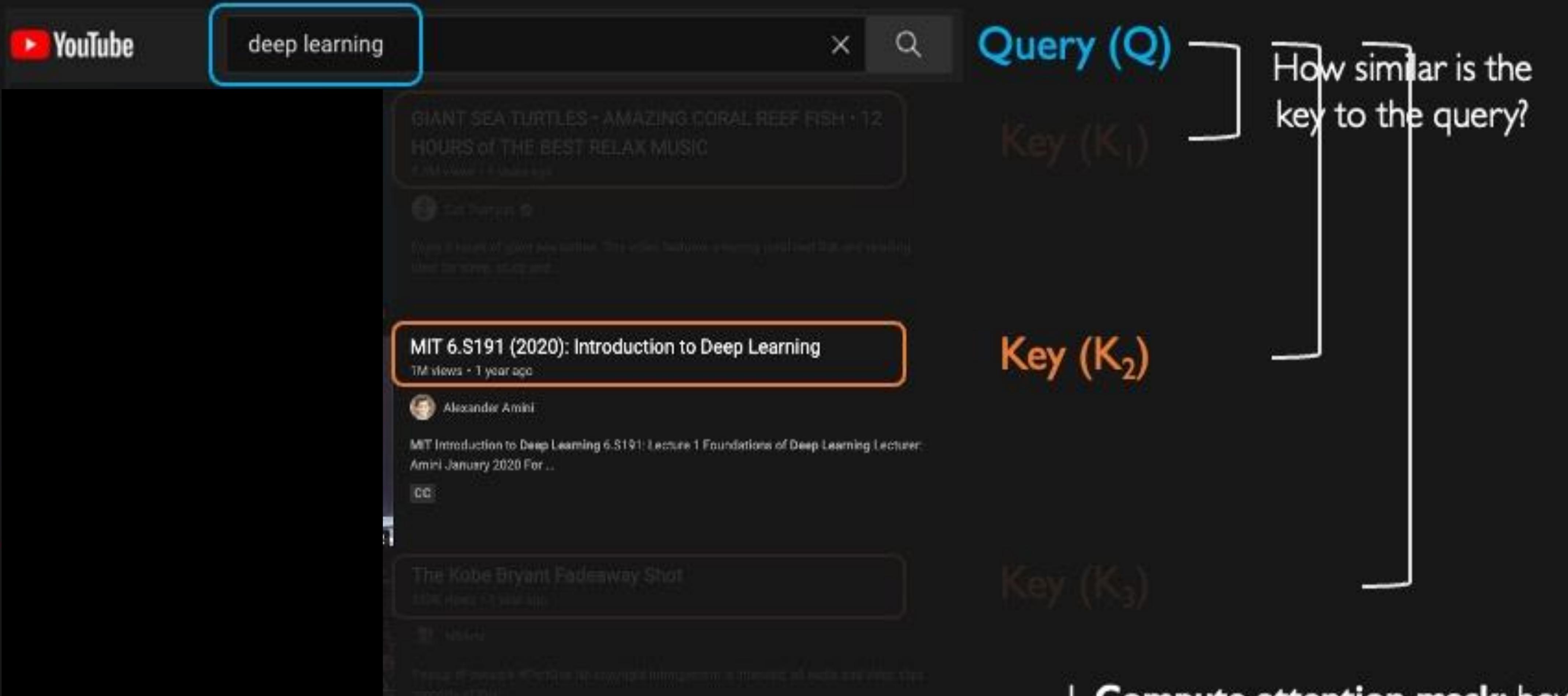
- 1. Identify which parts to attend to
- 2. Extract the features with high attention

Similar to a search problem!

A Simple Example: Search

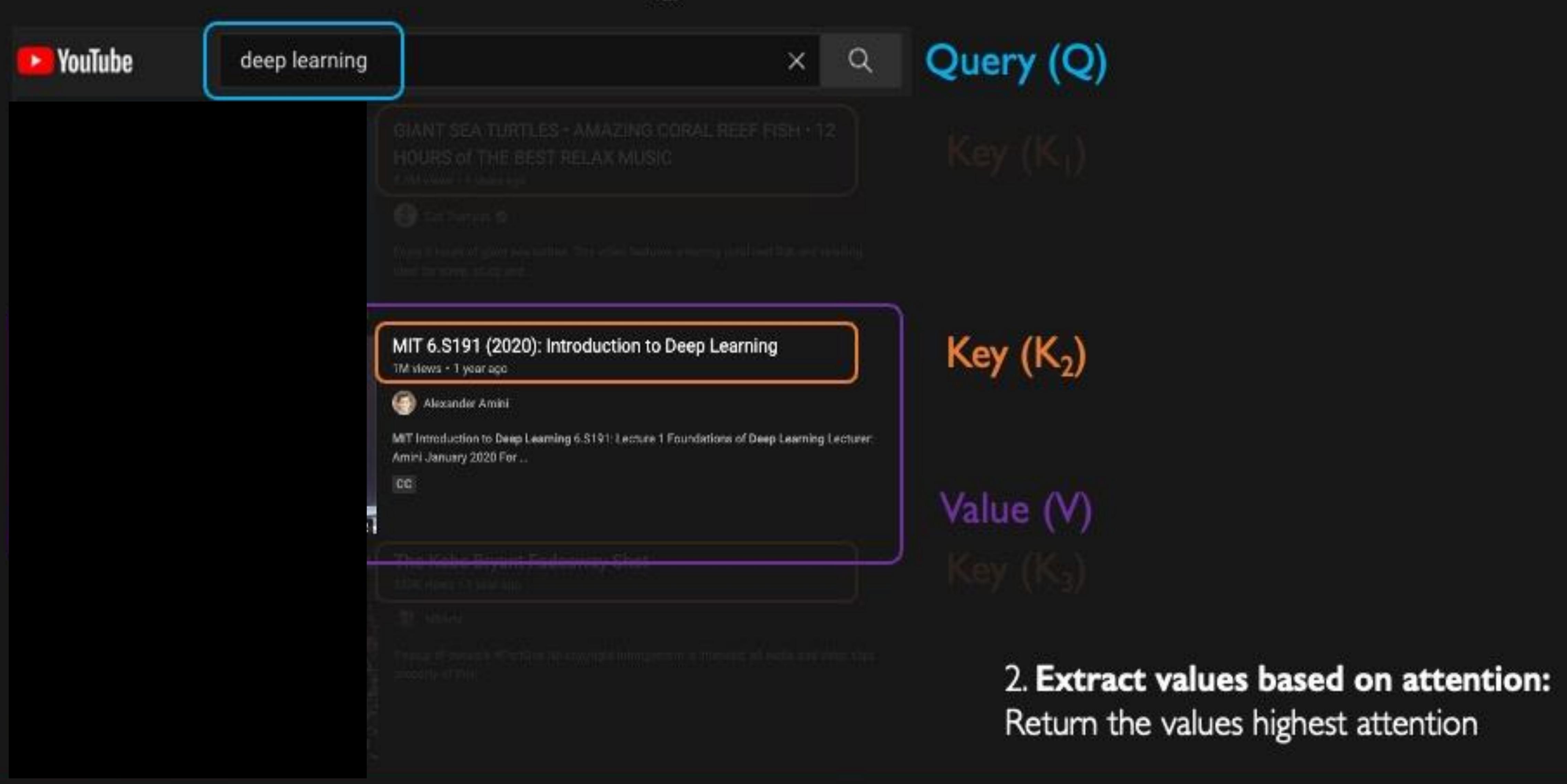


Understanding Attention with Search



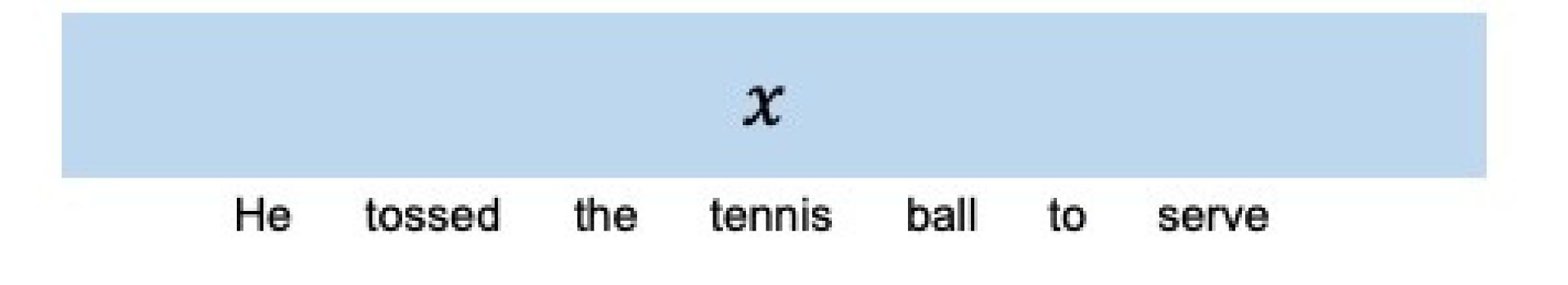
I. Compute attention mask: how similar is each key to the desired query?

Understanding Attention with Search



Goal: identify and attend to most important features in input.

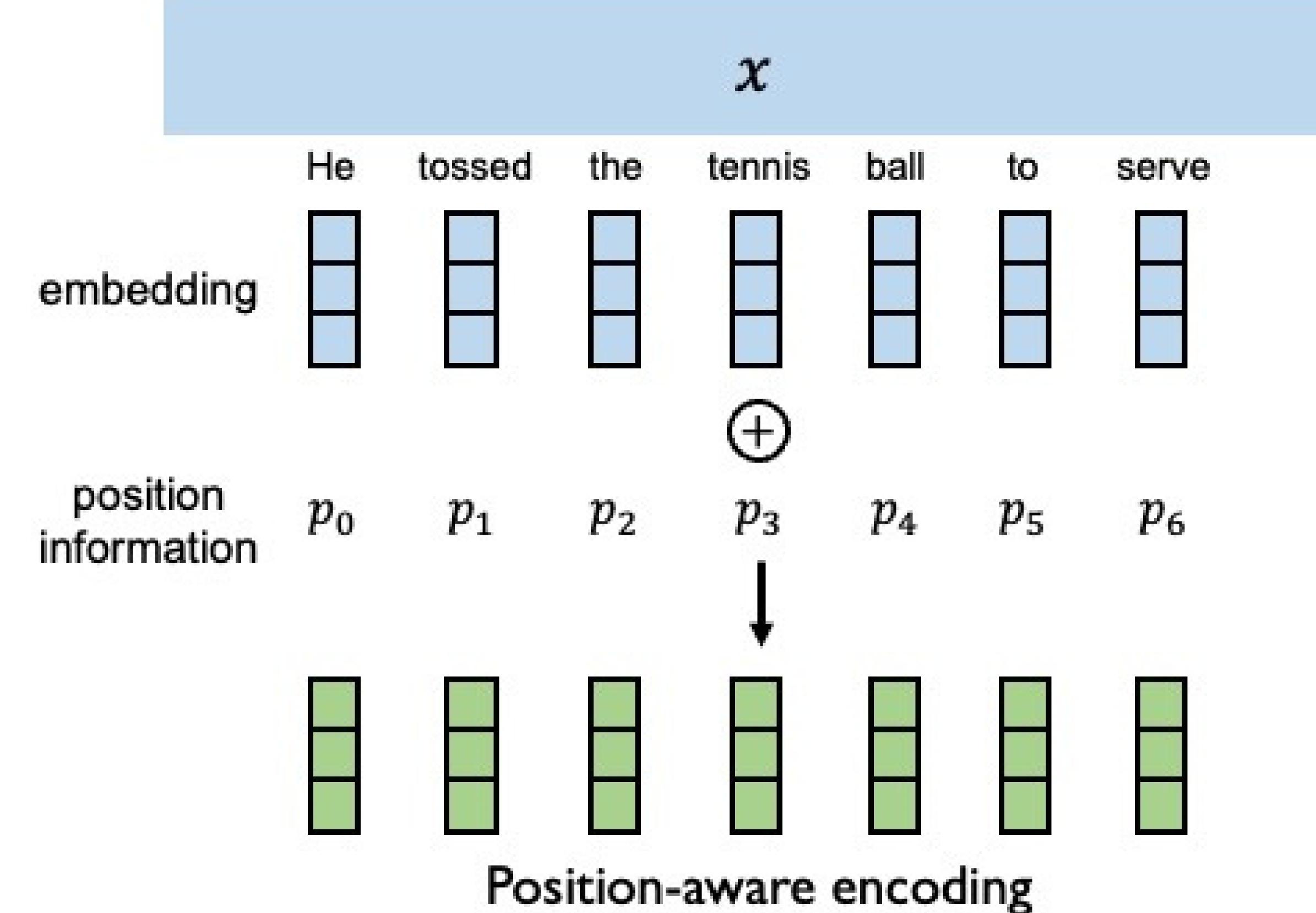
- 1. Encode **position** information
- 2. Extract query, key, value for search
- 3. Compute attention weighting
- 4. Extract features with high attention



Data is fed in all at once! Need to encode position information to understand order.

Goal: identify and attend to most important features in input.

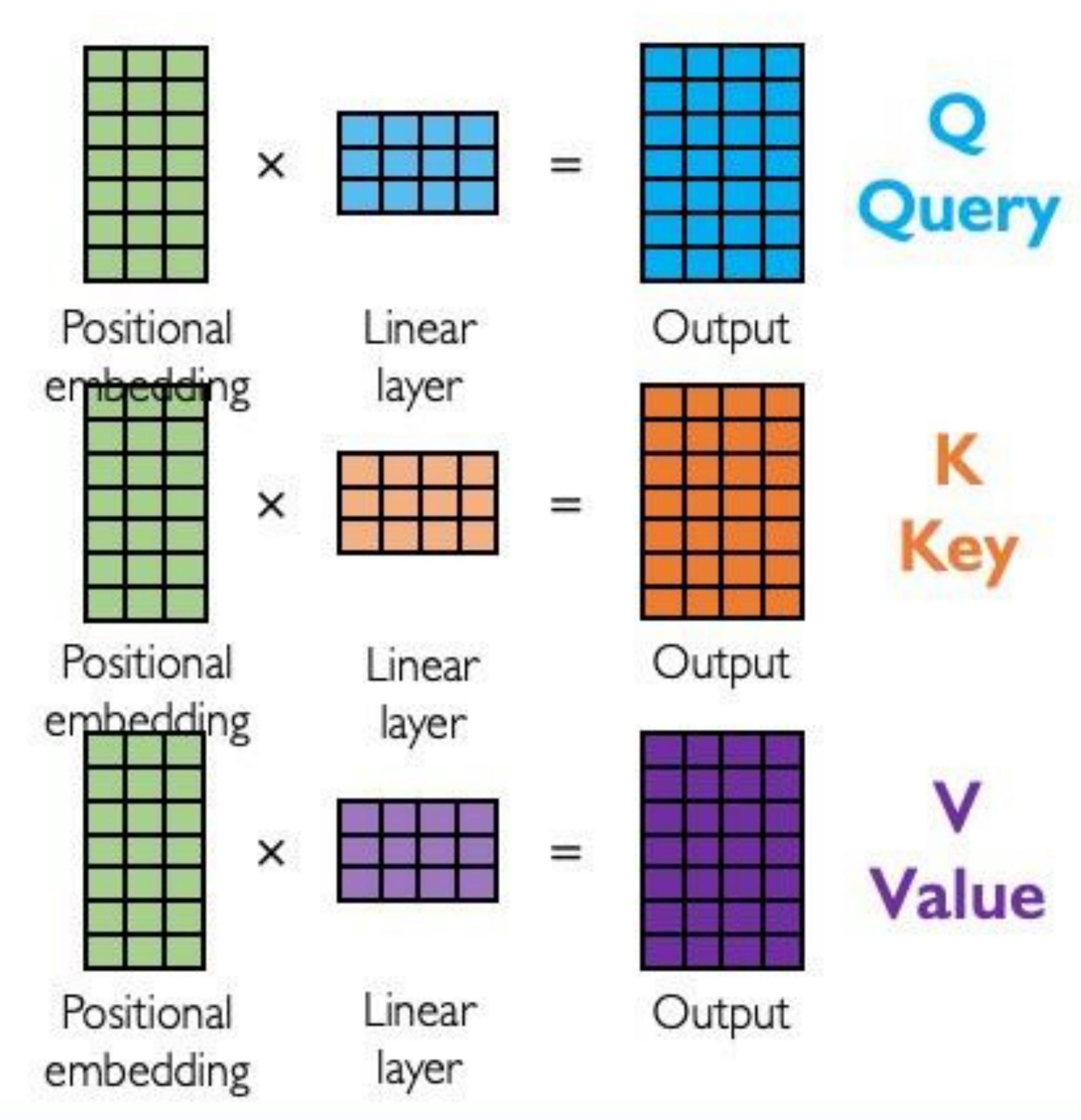
- 1. Encode **position** information
- 2. Extract query, key, value for search
- 3. Compute attention weighting
- 4. Extract features with high attention



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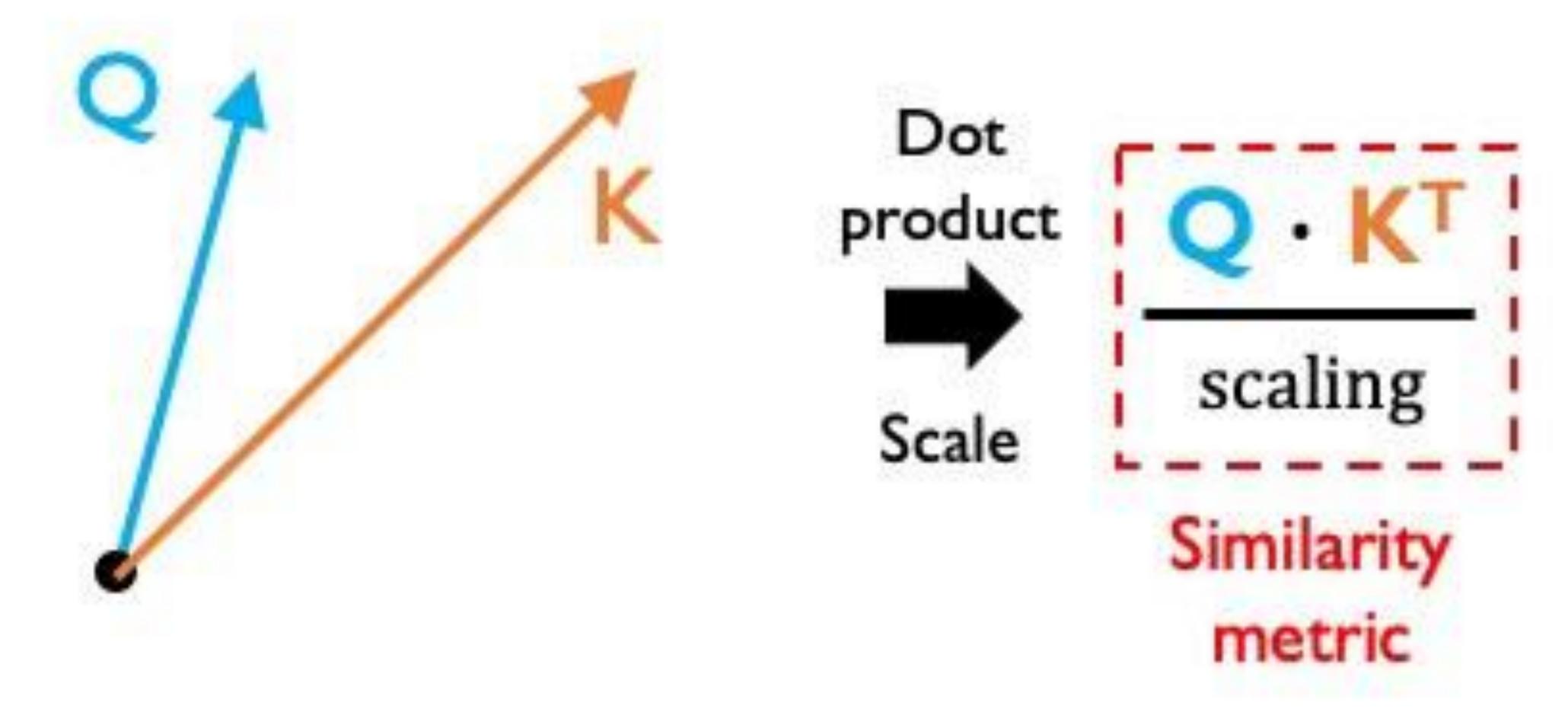


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Attention score: compute pairwise similarity between each query and key

How to compute similarity between two sets of features?



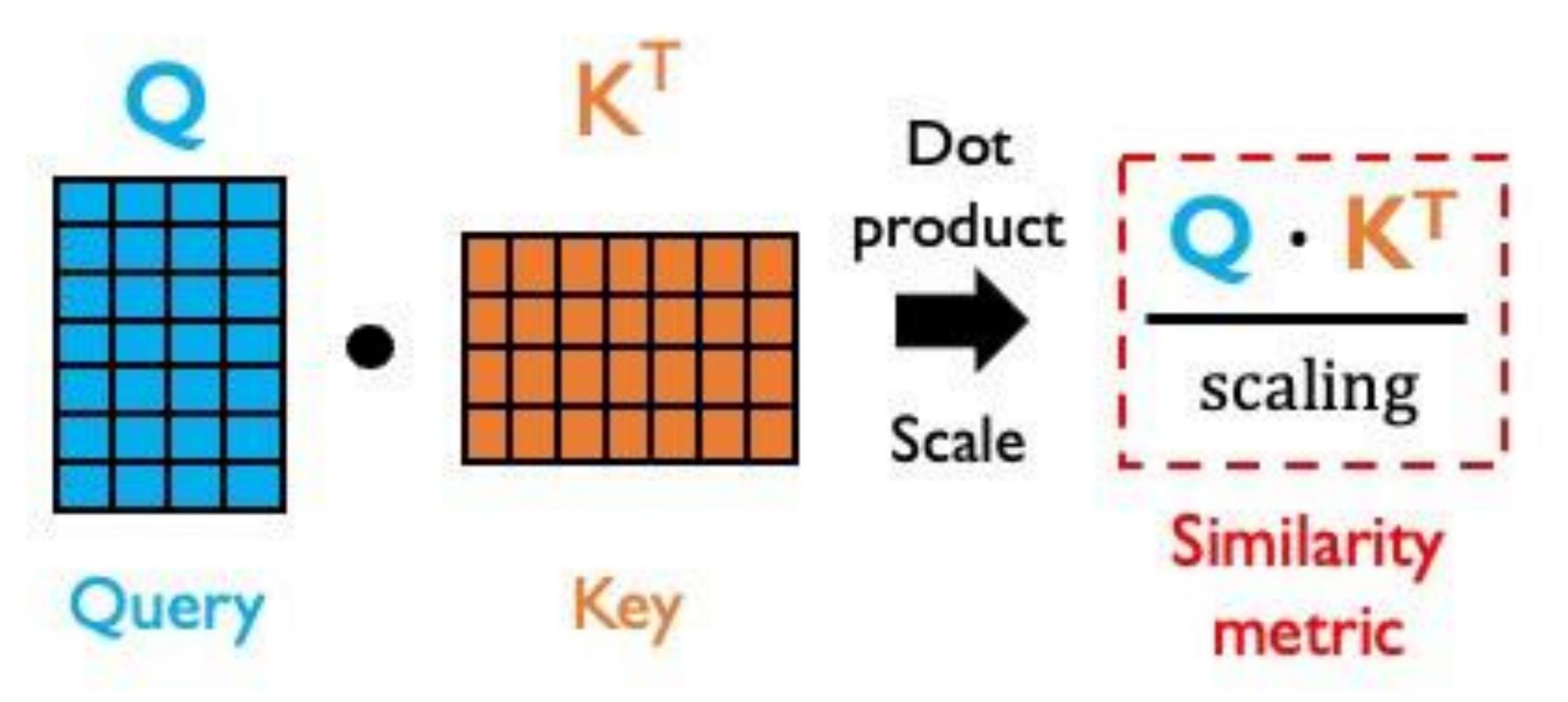
Also known as the "cosine similarity"

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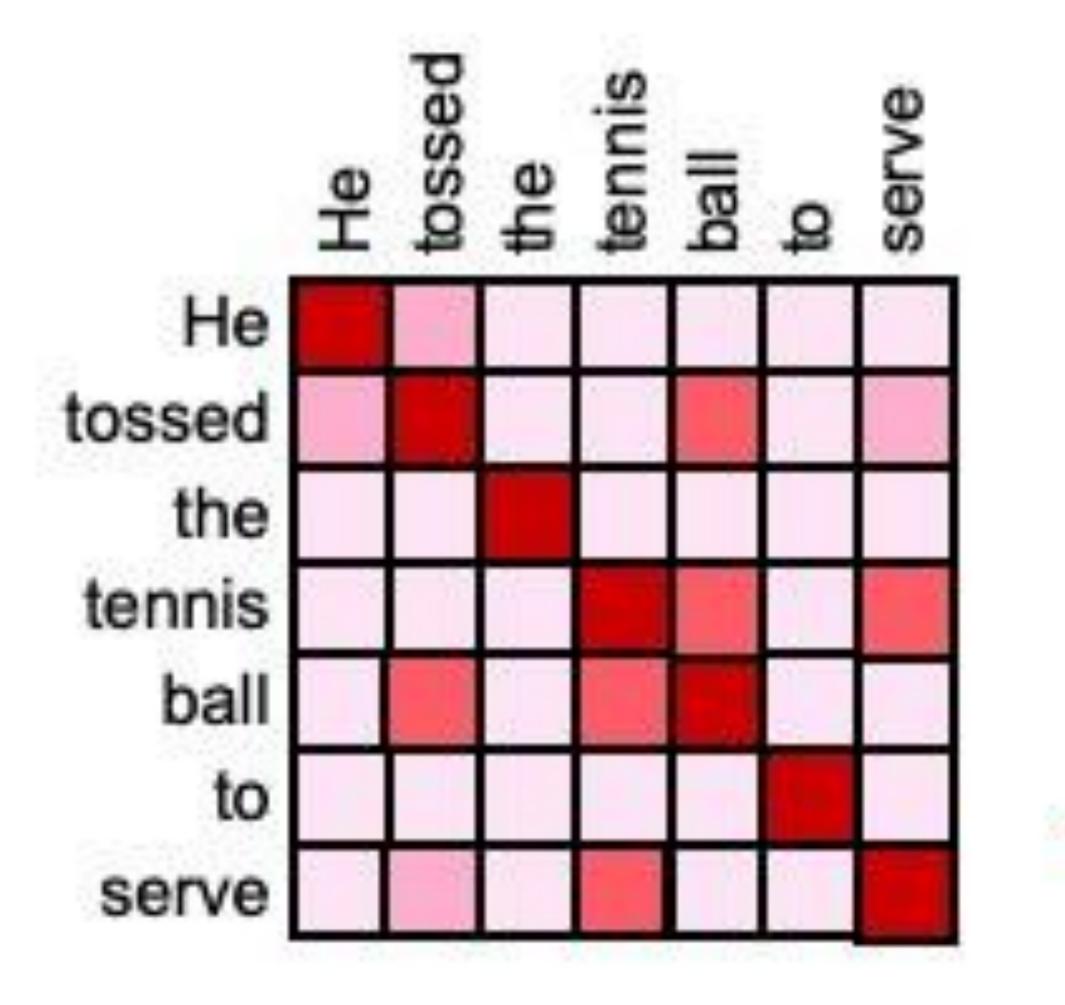


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Attention weighting: where to attend to! How similar is the key to the query?



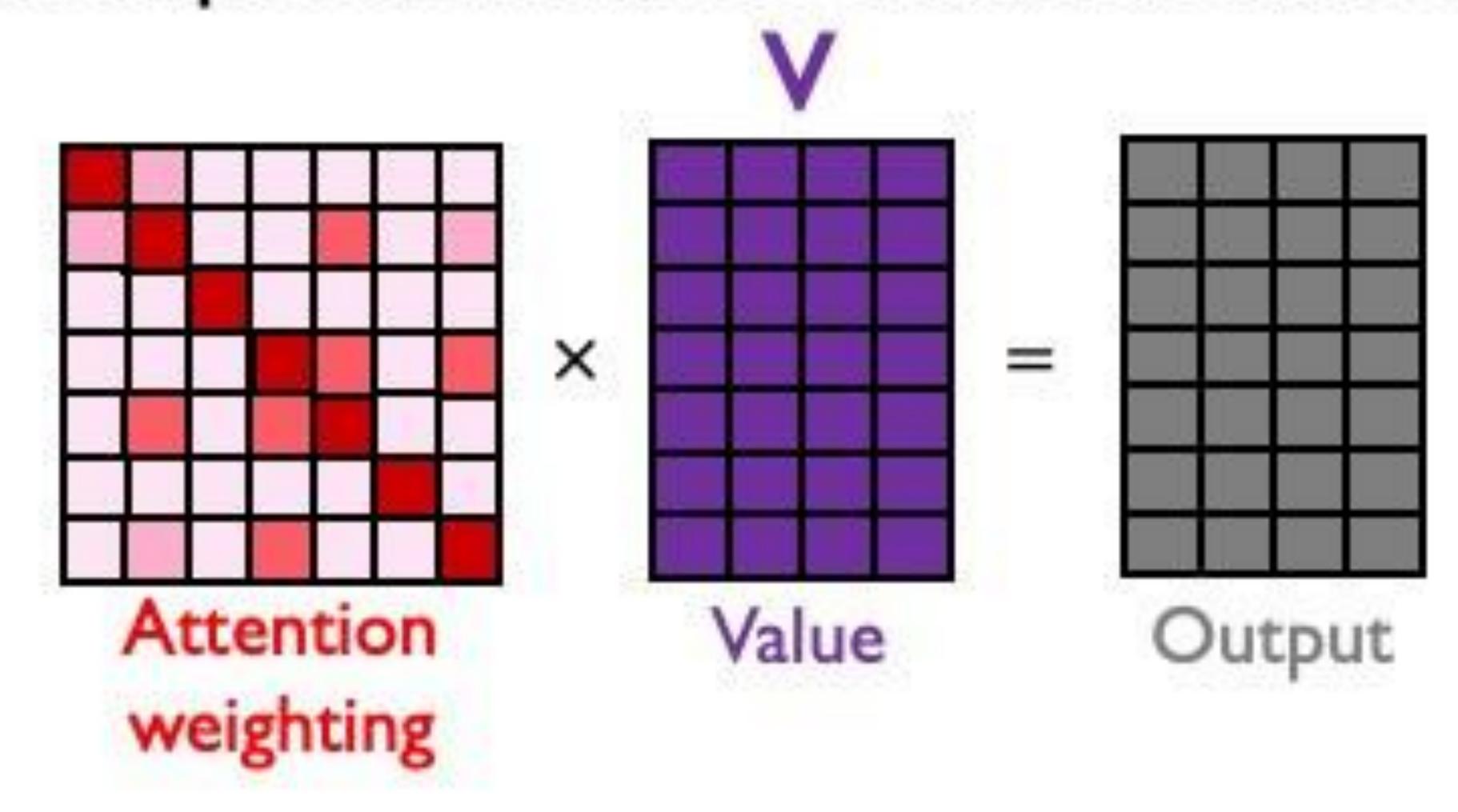
$$softmax \left(\frac{Q \cdot K^T}{scaling} \right)$$

Attention weighting

Goal: identify and attend to most important features in input.

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Last step: self-attend to extract features

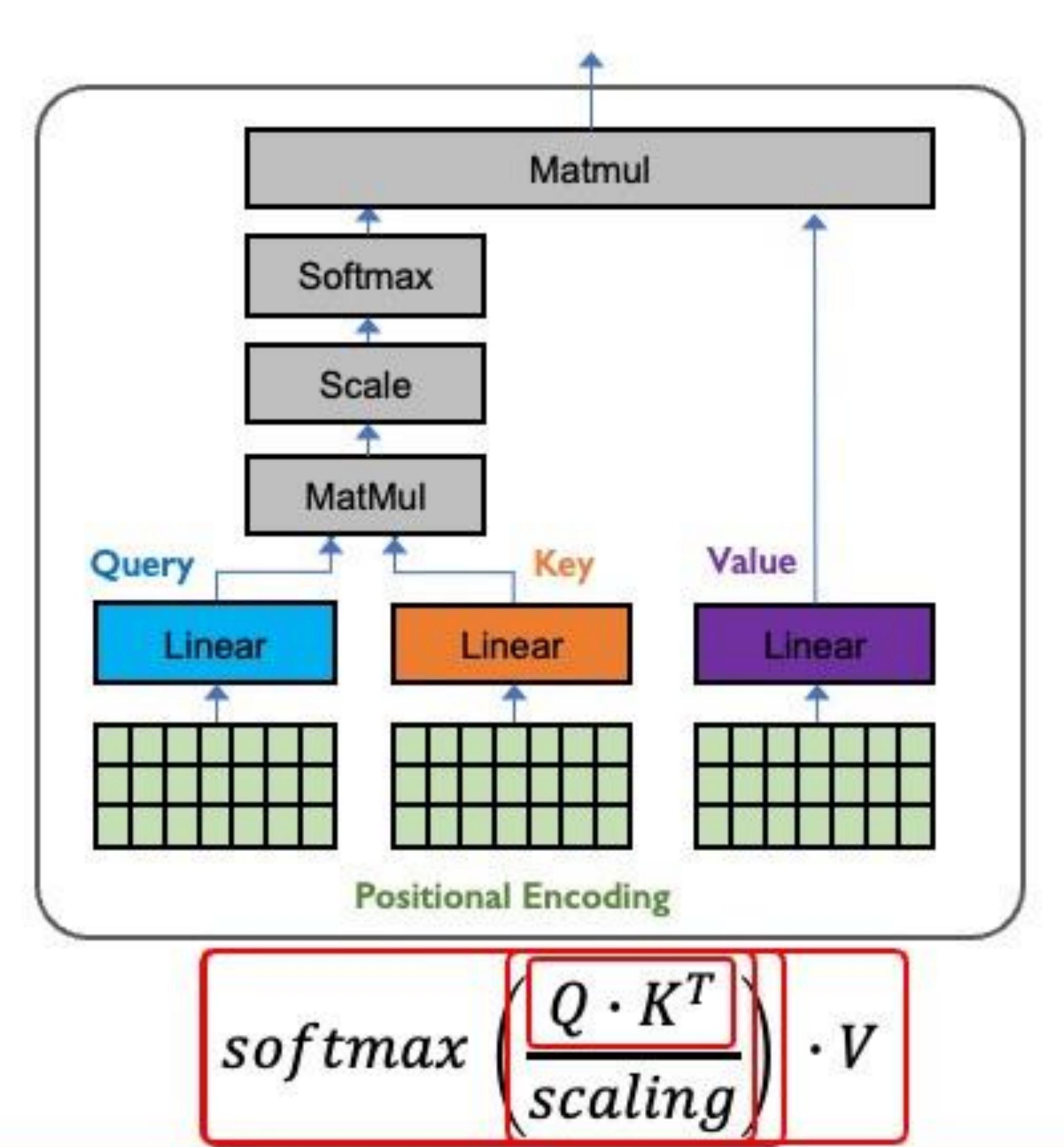


$$softmax\left(\frac{Q \cdot K^{T}}{scaling}\right) \cdot V = A(Q, K, V)$$

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These operations form a self-attention head that can plug into a larger network. Each head attends to a different part of input.



Applying Multiple Self-Attention Heads



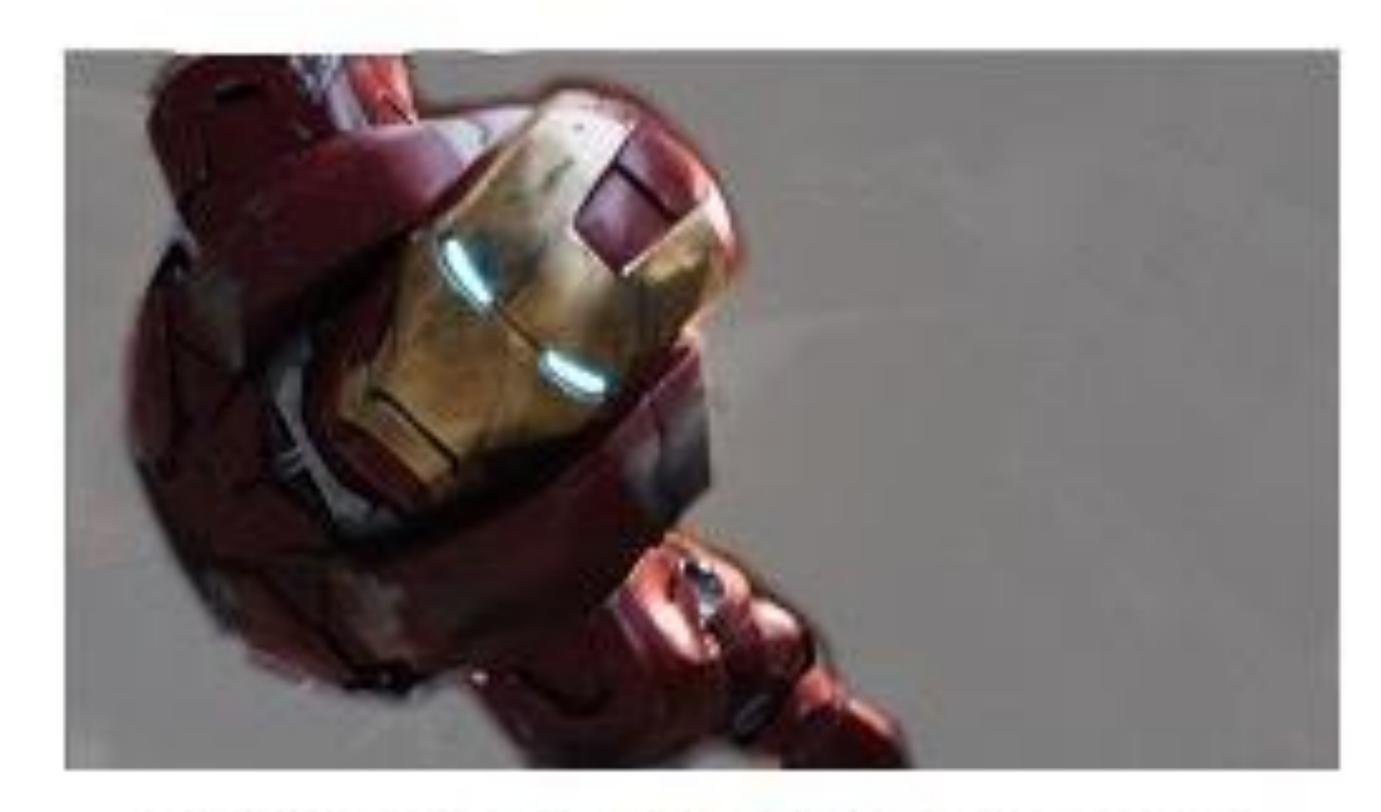
Attention weighting



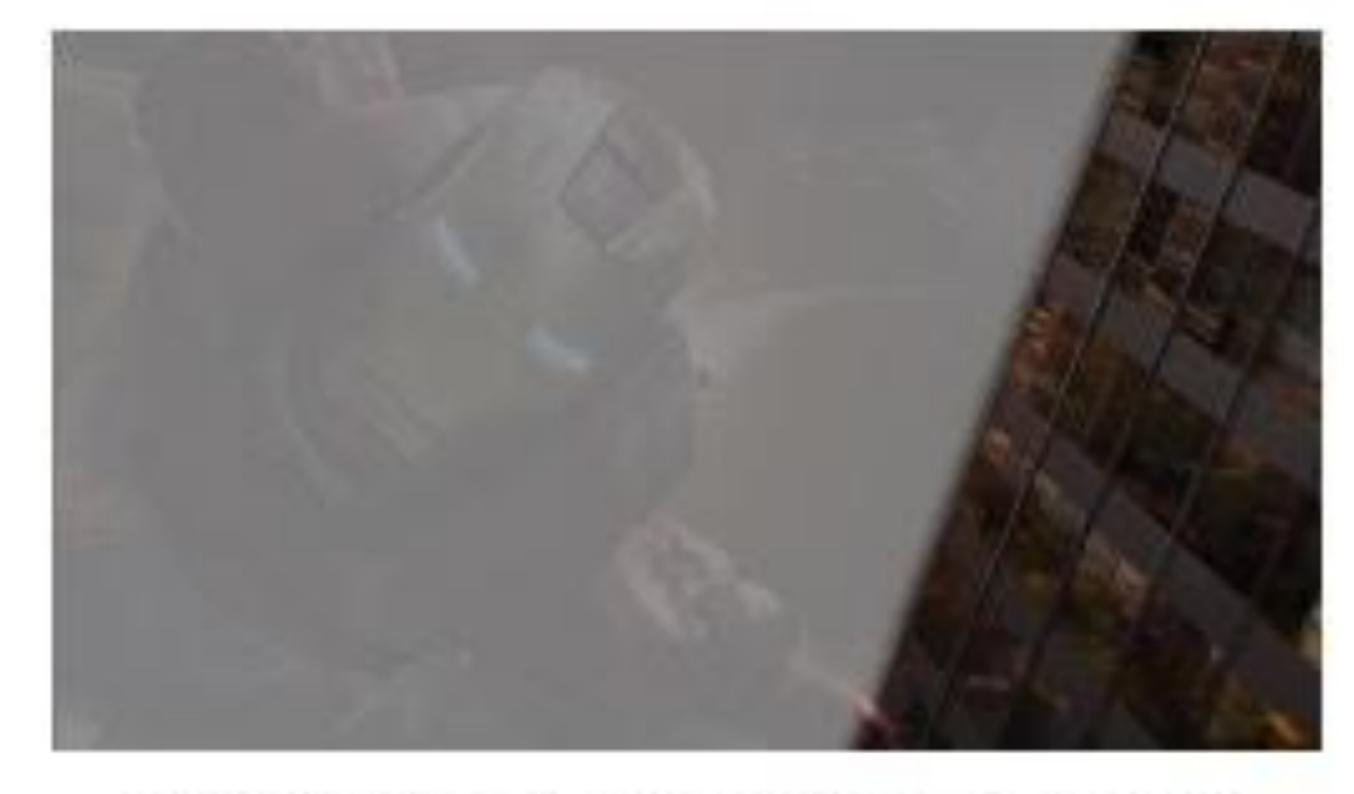
Value



Output



Output of attention head I



Output of attention head 2



Output of attention head 3

Self-Attention Applied

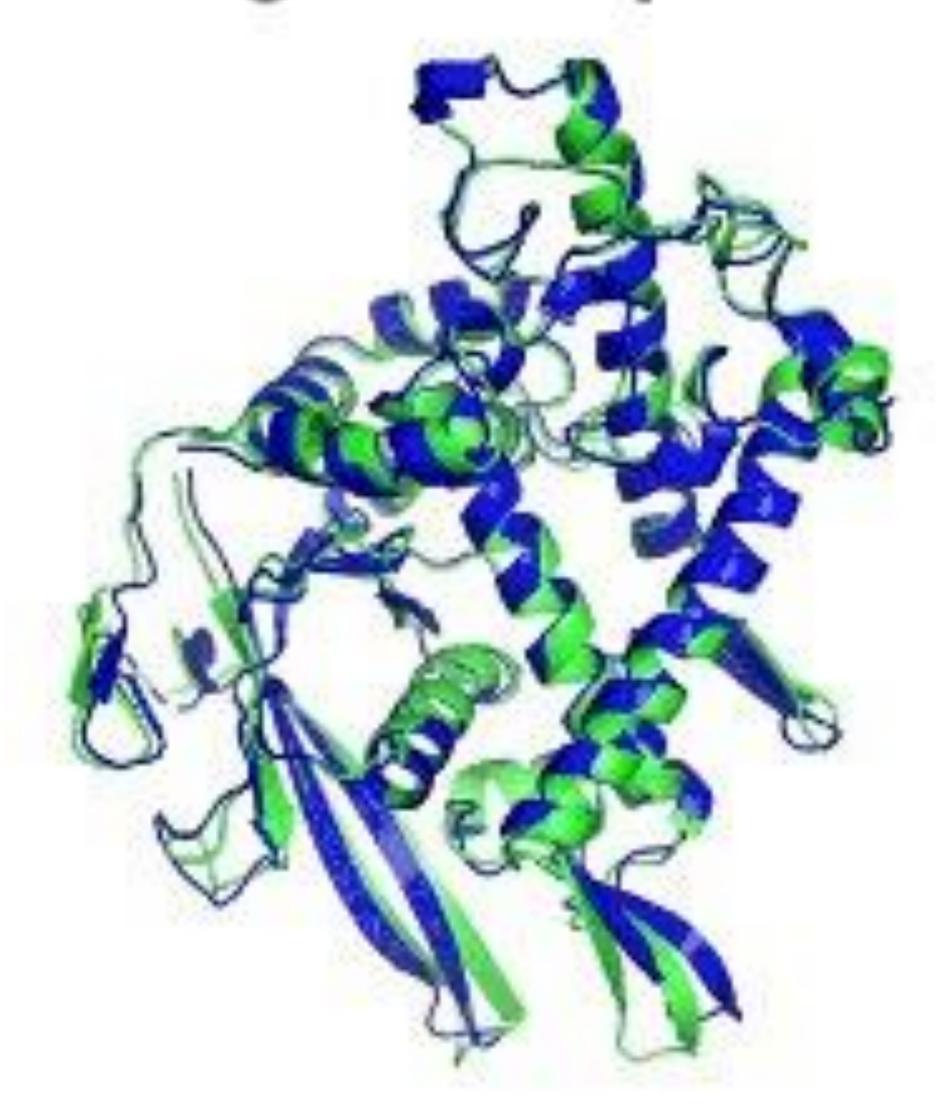
Language Processing



Transformers: BERT, GPT

Devlin et al., NAACL 2019 Brown et al., NeurlPS 2020

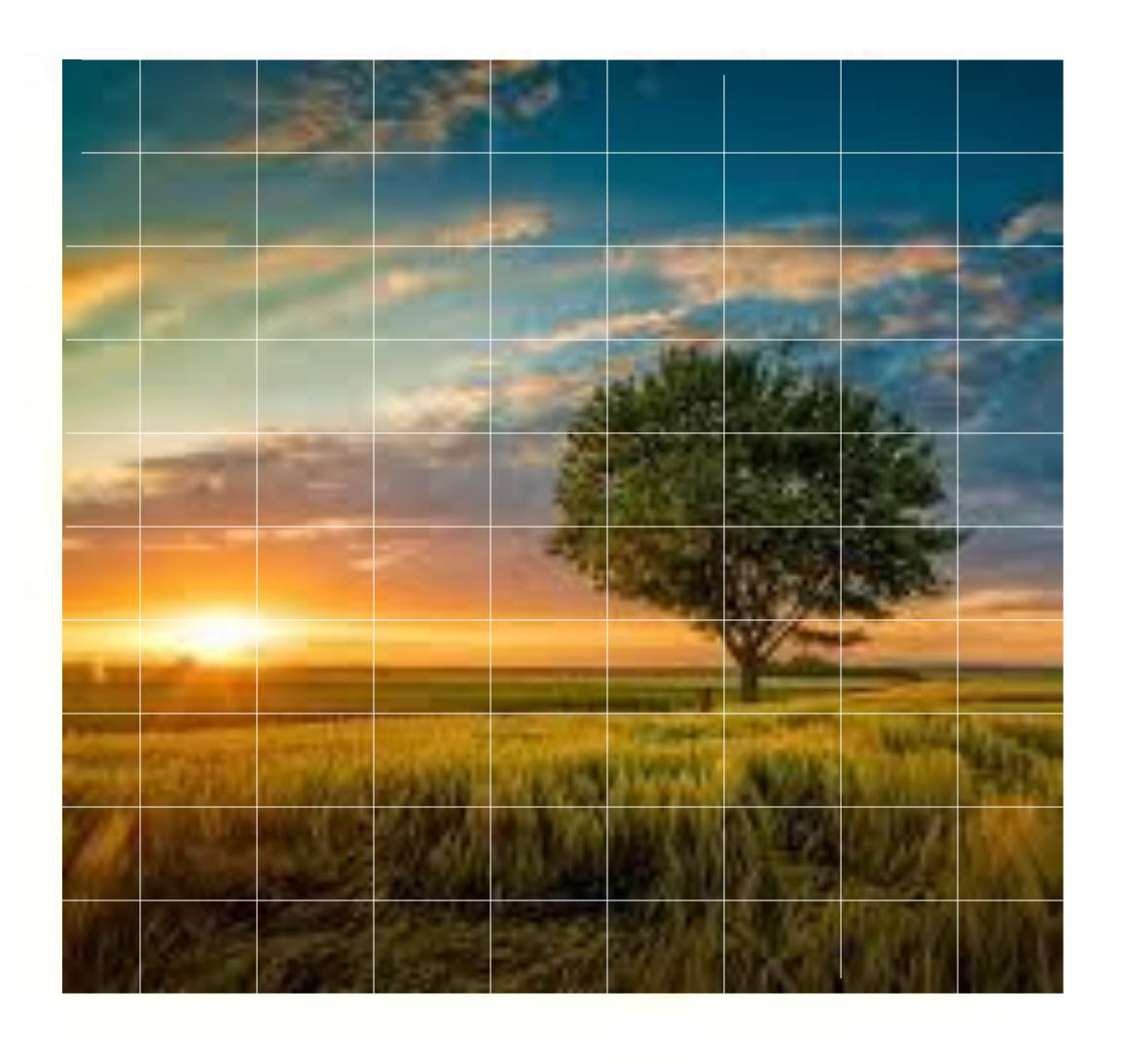
Biological Sequences



AlphaFold2

Jumper et al., Nature 2021

Computer Vision



Vision Transformers

Dosovitskiy et al., ICLR 2020

Deep Learning for Sequence Modeling: Summary

- 1. RNNs are well suited for sequence modeling tasks
- 2. Model sequences via a recurrence relation
- 3. Training RNNs with backpropagation through time
- 4. Models for music generation, classification, machine translation, and more
- 5. Self-attention to model sequences without recurrence
- 6. Self-attention is the basis for many large language models stay tuned!

