

**2.1. Concept of work:****2.1.1. Expression of the work of the pressure forces:**

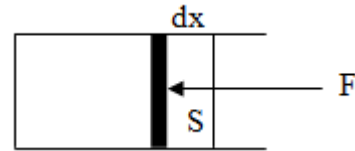
Work (**W**) is defined as a force **F** acting through a displacement **x**, the displacement being in the direction of the force.

$$\partial W = -F \cdot dx$$

$$P = \frac{F}{S} \rightarrow F = P \cdot S$$

$$\partial W = -P \cdot S \cdot dx \quad ; \quad S \cdot dx = dV$$

$$\partial W = -P \cdot dV \rightarrow \mathbf{W = - \int P \cdot dV}$$

**\*Units of work :**

$$[W] = \text{Pa} \cdot \text{m}^3 = \text{Joule (J)}$$

$$[W] = \text{calorie (cal)}$$

**Remark :**

\*If :  $V_2 > V_1 \rightarrow \Delta V > 0 \rightarrow W < 0$  (Expansion).

\*If :  $V_2 < V_1 \rightarrow \Delta V < 0 \rightarrow W > 0$  (Compression).

**2.1.2. Work for the different reversible transformations for an ideal gas:****a) Isochoric transformation:**

$$V = \text{constant} \rightarrow dV = 0$$

$$\mathbf{W = 0}$$

**b) Isobaric transformation:**

$$P = \text{constant} ; \text{ and } ; W = -P \int_{V_1}^{V_2} dV$$

$$\mathbf{W = -P (V_2 - V_1)}$$

$$V = \frac{nRT}{P} \rightarrow W = -P \left( \frac{nRT_2}{P} - \frac{nRT_1}{P} \right)$$

$$\mathbf{W = -nR (T_2 - T_1)}$$

**c) Isothermal transformation:**

$$T = \text{constant}$$

$$W = - \int P \cdot dV = - \int nRT \frac{dV}{V} = -nRT \int_{V_1}^{V_2} \frac{dV}{V} = -nRT [\text{Ln}V]_{V_1}^{V_2}$$

$$\mathbf{W = -nRT \cdot \text{Ln} \left( \frac{V_2}{V_1} \right)}$$

$$P_1 V_1 = P_2 V_2 \rightarrow \frac{V_2}{V_1} = \frac{P_1}{P_2}$$

$$\mathbf{W = -nRT \cdot \text{Ln} \left( \frac{P_1}{P_2} \right)}$$

**2.2. Concept of heat:****2.2.1. Definition:**

**Heat** or **quantity of heat (Q)** is the thermal energy that is transferred from one system at a higher temperature to another system (or the surroundings) at a lower temperature as the result of a temperature difference.

The expression for the quantity of heat is:

$$\partial Q = m \cdot c' \cdot dT \rightarrow Q = \int_{T_1}^{T_2} m \cdot c' \cdot dT$$

If  $c'$  is constant, we will have:  $Q = m \cdot c' \cdot \Delta T$

With:  $\Delta T = T_2 - T_1$

m: Mass of the substance.

$c'$ : *Specific heat capacity* (J/g.K, cal/g.K).

$\Delta T$ : Temperature change.

$T_1$ : Initial temperature.

$T_2$ : Final temperature.

**Note:** We can also write:

$$\partial Q = n \cdot c \cdot dT \rightarrow Q = \int_{T_1}^{T_2} n \cdot c \cdot dT$$

If  $c$  is constant, we will have:

$$Q = n \cdot c \cdot \Delta T \quad \text{With : } \Delta T = T_2 - T_1$$

n: number of moles.

$c$ : *molar heat capacity* (cal/mol.K, J/mol.K).

### Units of heat :

[Q] = Joule (J)

[Q] = calorie (cal)

### 2.1.2. Specific heat capacity (c):

*Specific heat capacity*, also called *specific heat* is the quantity of heat required to raise the temperature of 1g (or 1mol) of a substance by 1 °C.

We distinguish the following different types of specific heat capacity :

- Specific heat capacity " $c'_v$ " (molar heat capacity " $c_v$ ") at constant volume.
- Specific heat capacity " $c'_p$ " (molar heat capacity " $c_p$ ") at constant pressure.

### 2.1.3. Heat capacity (C):

Is the product of the specific heat capacity (molar heat capacity) of a substance by its mass (number of moles).  $C = m \cdot c' = n \cdot c$

So:  $Q = C \cdot \Delta T$

**C:** Heat capacity (cal /K ; J/ K)

There are two types of heat capacity:

$C_v$ : Heat capacity at constant volume.

$C_p$ : Heat capacity at constant pressure.

For  $C_p$ ,  $C_v$ ,  $c_p$  and  $c_v$ ; we have the following two cases:

**Case of pure substances in the solid or liquid states:**  $c_p \approx c_v$ , and,  $C_p \approx C_v$

**Case of pure substances in the gaseous state:**  $c_p \neq c_v$ , and,  $C_p \neq C_v$

### 2.1.4. Heat capacity for ideal gases:

- **Monatomic ideal gases:**

**Examples :** He, Ar, Ne...

$$C_p = \frac{5}{2} nR$$

$$C_v = \frac{3}{2} nR$$

With:

n: number of moles.

R: ideal gas constant.

- **Diatomic ideal gases:**

**Examples :** O<sub>2</sub>, N<sub>2</sub>, H<sub>2</sub>...

$$C_p = \frac{7}{2} nR$$

$$C_v = \frac{5}{2} nR$$

- **Relationship between  $c_p$  and  $c_v$  for an ideal gas:**

$c_p$  and  $c_v$  are linked by the **Mayer relation:  $c_p - c_v = R$**

We also have :  $\frac{c_p}{c_v} = \gamma$  ( $\gamma$ : adiabatic index)

From these two relationships; we find:

$$c_v = \frac{R}{\gamma - 1}$$

$$c_p = \frac{\gamma R}{\gamma - 1}$$

### **2.1.5. Quantities of heat for the different transformations:**

#### **\*Isochoric transformation:**

$$\int_1^2 \partial Q = \int_{T_1}^{T_2} m \cdot c'_v \cdot dT = \int_{T_1}^{T_2} n \cdot c_v \cdot dT \rightarrow \int_1^2 \partial Q = m \cdot c'_v \int_{T_1}^{T_2} dT = n \cdot c_v \int_{T_1}^{T_2} dT$$

$$Q = m \cdot c'_v \cdot (T_2 - T_1) = n \cdot c_v \cdot (T_2 - T_1)$$

#### **\*Isobaric transformation:**

$$\int_1^2 \partial Q = \int_{T_1}^{T_2} m \cdot c'_p \cdot dT = \int_{T_1}^{T_2} n \cdot c_p \cdot dT \rightarrow \int_1^2 \partial Q = m \cdot c'_p \int_{T_1}^{T_2} dT = n \cdot c_p \int_{T_1}^{T_2} dT$$

$$Q = m \cdot c'_p \cdot (T_2 - T_1) = n \cdot c_p \cdot (T_2 - T_1)$$

#### **\*Isothermal transformation:**

$$Q = -W \quad (\text{According to the first principle of thermodynamics})$$

$$Q = nRT \cdot \ln\left(\frac{P_1}{P_2}\right) = nRT \cdot \ln\left(\frac{V_2}{V_1}\right)$$

#### **\*Adiabatic transformation:**

$$Q = 0$$

### **2.1.6. Latent heat of physical state change:**

*Latent heat* is the quantity of heat absorbed or released by 1g (or 1mol) of a substance during a change in its physical state that occurs at constant temperature. It is denoted  $L'$  (or  $L$ ).

The quantity of heat for physical state change is given by:

$$Q = m \cdot L' = n \cdot L$$

$$[L'] = \text{cal/g, J/g}$$

$$[L] = \text{cal/mole, J/mole}$$

Solid  $\rightarrow$  Liquid: Latent heat of fusion or melting ( $L_f > 0$ )

Liquid  $\rightarrow$  Solid: Latent heat of solidification or freezing ( $L_s = -L_f < 0$ )

Liquid  $\rightarrow$  Gas: Latent heat of vaporization ( $L_v > 0$ )

Gas  $\rightarrow$  Liquid: Latent heat of liquefaction ( $L_{\text{liq}} = -L_v < 0$ )

Solid  $\rightarrow$  Gas: Latent heat of sublimation ( $L_{\text{sub}} > 0$ )

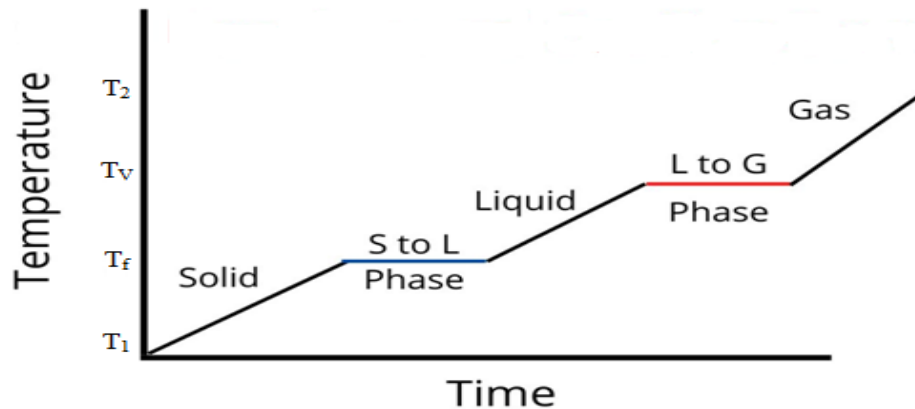
Gas  $\rightarrow$  Solid: Latent heat of condensation ( $L_{\text{cond}} = -L_{\text{sub}} < 0$ )

### Examples :

For water:  $L_f = 80 \text{ cal/g}$  ( $p = 1 \text{ atm}$  ;  $T = 0^\circ\text{C}$ )

$L_v = 535 \text{ cal/g}$  ( $p = 1 \text{ atm}$  ;  $T = 100^\circ\text{C}$ )

### \* Calculating (Q) during the heating of a pure substance :



The quantity of heat for 1g of a pure substance undergoing fusion and vaporization, transitioning from temperature  $T_1$  to temperature  $T_2$ , is expressed as:

$$Q = Q_1 + Q_2 + Q_3 + Q_4 + Q_5$$

$$Q =$$

$$m \cdot c'_{p(\text{solid})} \cdot (T_f - T_1) + m \cdot L'_f + m \cdot c'_{p(\text{liquid})} \cdot (T_v - T_f) + m \cdot L'_v + m \cdot c'_{p(\text{vapor})} \cdot (T_2 - T_v)$$

$T_f$ : temperature of fusion (melting).

$T_v$ : temperature of vaporization.

## 2.3. First principle of thermodynamics:

### 2.3.1. Statement of the first principle of thermodynamics:

First principle of thermodynamics is thus *conventionally* stated as: « **The change in internal energy of a system is equal to the energy exchanged between the system and the surroundings in the form of work and heat.** »

Mathematically, this can be put as :

$$dU = \partial W + \partial Q \longrightarrow \Delta U = W + Q$$

U: is the internal energy; it is a state function.

W and Q are not state functions.

### 2.3.2. Internal energy (U):

Is the sum of potential and kinetic energies of all particles in a system. Its differential expression is:

$$dU = n \cdot c_v \cdot dT$$

[U] = joule, calorie.

### \*1<sup>st</sup> law of Joule:

For an ideal gas, the internal energy (U) only depends on the temperature, it is independent of pressure and volume.

**2.3.3. Enthalpy (H):**

Enthalpy is defined as the sum of a system's internal energy (U) and the work that the system has done on its surroundings. It is a state function.

$$H = U + P \cdot V$$

The differential expression for enthalpy is:

$$dH = n \cdot c_p \cdot dT$$

[H] = joule, calorie

**\*2<sup>nd</sup> law of Joule:**

For an ideal gas, the enthalpy (H) only depends on the temperature, it is independent of pressure and volume.

**2.3.4. Internal energy change for the different transformations:****a) Isochoric transformation:**

$$\int_{U_1}^{U_2} dU = \int_{T_1}^{T_2} n \cdot c_v \cdot dT = n \cdot c_v \int_{T_1}^{T_2} dT$$

$$\Delta U = U_2 - U_1 = n \cdot c_v \cdot (T_2 - T_1)$$

$$V = \text{Cte} \rightarrow W = 0 ; \text{ and; } \Delta U = W + Q; \text{ Hence } \Delta U = Q_v$$

**b) Isobaric transformation:**

$$\int_{U_1}^{U_2} dU = \int_{T_1}^{T_2} n \cdot c_v \cdot dT$$

$$\Delta U = U_2 - U_1 = n \cdot c_v \cdot (T_2 - T_1)$$

**c) Isothermal transformation:**

$$T = \text{cte} \longrightarrow \Delta T = 0$$

$$\int_{U_1}^{U_2} dU = \int_{T_1}^{T_2} n \cdot c_v \cdot dT \rightarrow \Delta U = n \cdot c_v \cdot \Delta T$$

$$\Delta U = 0$$

We have:  $\Delta U = W + Q$  (According to the 1<sup>st</sup> principle of thermodynamics)

and :  $\Delta U = 0$  (According to the 1<sup>st</sup> law of Joule)

$$\text{So: } Q = -W$$

**d) Adiabatic transformation:**

$$\int_{U_1}^{U_2} dU = \int_{T_1}^{T_2} n \cdot c_v \cdot dT = n \cdot c_v \int_{T_1}^{T_2} dT$$

$$\Delta U = U_2 - U_1 = n \cdot c_v \cdot (T_2 - T_1)$$

We have:  $\Delta U = W + Q$ ; and;  $Q = 0$

$$\text{Hence : } \Delta U = W$$

**2.3.5. Enthalpy change for the different transformations:****a) Isochoric transformation:**

$$\int_{H_1}^{H_2} dH = \int_{T_1}^{T_2} n \cdot c_p \cdot dT = n \cdot c_p \int_{T_1}^{T_2} dT$$

$$\Delta H = H_2 - H_1 = n \cdot c_p \cdot (T_2 - T_1)$$

**b) Isobaric transformation:**

$$\int_{H_1}^{H_2} dH = \int_{T_1}^{T_2} n \cdot c_p \cdot dT = n \cdot c_p \int_{T_1}^{T_2} dT$$

$$\Delta H = H_2 - H_1 = n \cdot c_p \cdot (T_2 - T_1)$$

$$P = \text{Cte} \rightarrow W = -P(V_2 - V_1)$$

$$Q_p = \Delta U - W = (U_2 - U_1) + P(V_2 - V_1)$$

$$Q_p = (U_2 + P \cdot V_2) - (U_1 + P \cdot V_1)$$

$$\text{We have: } H = U + P \cdot V$$

$$\text{Hence: } Q_p = H_2 - H_1 = \Delta H$$

$$Q_p = \Delta H$$

**c) Isothermal transformation:**

$$T = \text{cte} \longrightarrow \Delta T = 0$$

$$\int_H^{H_2} dH = \int_{T_1}^{T_2} n \cdot c_p \cdot dT \rightarrow \Delta H = n \cdot c_p \cdot \Delta T$$

$$\Delta H = 0 \quad (\text{According to the 2}^{\text{nd}} \text{ law of Joule})$$

**d) Adiabatic transformation:**

$$\int_{H_1}^{H_2} dH = \int_{T_1}^{T_2} n \cdot c_p \cdot dT = n \cdot c_p \int_{T_1}^{T_2} dT$$

$$\Delta H = H_2 - H_1 = n \cdot c_p \cdot (T_2 - T_1)$$

**Note:**

$$\Delta H = n \cdot c_p \cdot \Delta T$$

$$\Delta U = N \cdot C_v \cdot \Delta T$$

$$\frac{\Delta H}{\Delta U} = \frac{c_p}{c_v} = \gamma \rightarrow \Delta H = \gamma \cdot \Delta U$$

**2.3.6. Reversible adiabatic transformation:**

$$dU = \partial Q + \partial W, \text{ and, } \partial Q = 0 \text{ (adiabatic), so: } dU = \partial W$$

$$dU = n c_v dT = n \frac{R}{\gamma-1} dT, \text{ and, } \partial W = -P dV = -nRT \frac{dV}{V}$$

$$\text{So: } n \frac{R}{\gamma-1} dT = -nRT \frac{dV}{V} \rightarrow \int \frac{dT}{T} = -(\gamma-1) \int \frac{dV}{V}$$

$$\text{Ln}T = -(\gamma-1)\text{Ln}V + \text{Cte} \rightarrow \text{Ln}T + \text{Ln}V^{(\gamma-1)} = \text{Cte} \rightarrow \text{Ln}(T \cdot V^{(\gamma-1)}) = \text{Cte}$$

$$T \cdot V^{(\gamma-1)} = K$$

**We have also:**

$$T \cdot V^{(\gamma-1)} = K \quad ; \text{ and; } \quad T = \frac{P \cdot V}{n \cdot R}$$

$$\text{Hence: } \left(\frac{P \cdot V}{n \cdot R}\right) \cdot V^{(\gamma-1)} = K \rightarrow P \cdot V^\gamma = K \cdot n \cdot R = k'$$

$$P \cdot V^\gamma = k'$$

**And we have also:**

$$T \cdot V^{(\gamma-1)} = K \quad ; \text{ and; } \quad V = \frac{nRT}{P}$$

$$T \cdot \left(\frac{nRT}{P}\right)^{(\gamma-1)} = K \rightarrow T^\gamma \cdot P^{(1-\gamma)} = \frac{K}{(n \cdot R)^{(\gamma-1)}} = K''$$

$$T^\gamma \cdot P^{(1-\gamma)} = K''$$

$$\left. \begin{array}{l} T \cdot V^{(\gamma-1)} = K \\ P \cdot V^\gamma = k' \\ T^\gamma \cdot P^{(1-\gamma)} = K'' \end{array} \right\} \text{Laws of LAPLACE}$$

**2.3.7. Reversible adiabatic work:**

Adiabatic transformation :  $Q = 0$ ; So :

$$W = \Delta U = n \cdot c_v \cdot (T_2 - T_1) ; \text{ and } ; c_v = \frac{R}{\gamma-1}$$

$$W = n \frac{R}{\gamma-1} (T_2 - T_1)$$

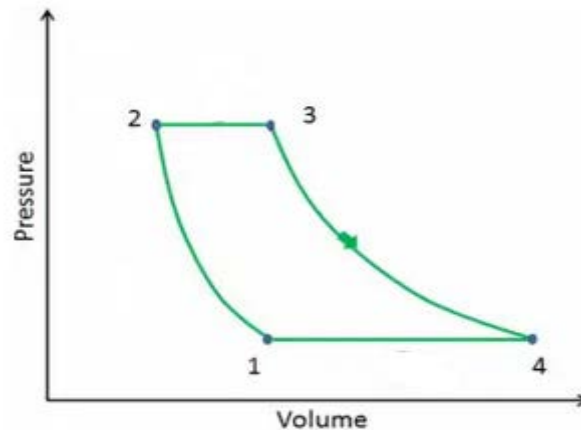
$$W = \frac{1}{\gamma-1} (nRT_2 - nRT_1) ; \text{ and } ; PV = nRT$$

$$\text{Hence : } W = \left(\frac{1}{\gamma-1}\right)(P_2V_2 - P_1V_1)$$

$$W = \frac{P_2V_2 - P_1V_1}{\gamma-1}$$

**2.3.8. Special cases:****a) Cyclic transformation (Cyclic process):**

Is a process in which the initial and final states are the same. It is a sequence of processes that leave the system in the same state in which it started.



$$U_1 = U_2 \rightarrow \Delta U = U_2 - U_1 = 0$$

$$\Delta U = Q + W = 0 \rightarrow Q = -W \quad Q \neq 0 ; \text{ and } ; W \neq 0$$

**b) Isolated system:**

The isolated system does not exchange energy with the surroundings.

$$Q = 0 \quad ; \text{ and } ; W = 0$$

$$\Delta U = Q + W = 0 \rightarrow \Delta U = U_2 - U_1 = 0 \rightarrow U_2 = U_1$$