

## Tutorials. No. 1: Thermal Machines

### **Exercise 01: (Thermal motor/ refrigeration machine)**

Consider a dithermal heat machine, where the hot source is at a temperature  $T_1$  and the cold source is at a temperature  $T_2$ . The fluid of this machine exchanges heat  $Q_1$  with the hot source,  $Q_2$  with the cold source, and performs work. The fluid is assumed to behave as an ideal gas. Initially, the fluid in state A undergoes the following transformations: an isothermal compression AB at  $T_2$ , an adiabatic compression BC, an isothermal expansion CD at  $T_1$ , and finally an adiabatic expansion DA.

1. Represent this cycle on a Clapeyron diagram. Indicate the direction in which it is traversed and the sign of the work.
2. Show that:  $(V_A/V_B) = (V_D/V_C)$ .
3. Determine the expressions for the heat  $Q_1$  and  $Q_2$  exchanged by the fluid. Deduce the Clausius equality:  $(Q_1/T_1) + (Q_2/T_2) = 0$ .

Provide a simple interpretation of this equality.

4. This machine is used as a refrigeration machine. Sketch the schematic diagram of this machine, indicating the directions of the exchanged heat and work.
5. Calculate the efficiency of this machine for  $\theta_1 = 25^\circ\text{C}$  and  $\theta_2 = -15^\circ\text{C}$ .
6. Calculate the heat extracted from the cold source if the machine has consumed 12 kJ of work.

### **Exercise 02: (Diesel motor)**

We consider the following Diesel motor: the same amount of an ideal gas undergoes a reversible cycle ABCDA:

- Transformations AB and CD are adiabatic.
- Transformation BC is isobaric, during which the gas receives heat  $Q_c$  from a hot source.
- Transformation DA is isochoric, in contact with the atmosphere acting as the cold source.

Given: ratio of specific heat capacities  $\gamma = C_p/C_v = 1.4$ , and  $R = 8.314 \text{ J/(K}\cdot\text{mol)}$ .

The table below summarizes the data regarding the different states of the gas.

	A	B	C	D
P (Bar)	1,00			
T (K)	323	954		
V (L)	2,40		0,24	2,40

- 1- Copy the table above and complete it by determining the volumes, temperatures, and pressures of states B, C, and D.
- 2- Plot the shape of the cycle described by the gas on the Clapeyron diagram, specifying its direction.

- 3- Calculate the number  $n$  of moles of gas undergoing these four transformations.
- 4- Calculate the specific heat capacities at constant volume and constant pressure.
- 5- Calculate the work and heat exchanges for the gas during each of the transformations AB, BC, CD, and DA.
- 6- Define the thermal efficiency of the studied Diesel engine and calculate it numerically.
- 7- Provide the expression for the efficiency of a Carnot engine operating between two sources at equal temperatures  $T_A$  and  $T_C$ , and calculate it numerically.
- 8- Compare the two efficiencies. What conclusions can you draw?