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Chapter 1

Subprograms: *Functions and Procedures*

MI-L1-UEF121 : Algorithms and Data Structures II

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Course Topics

1. Modularity

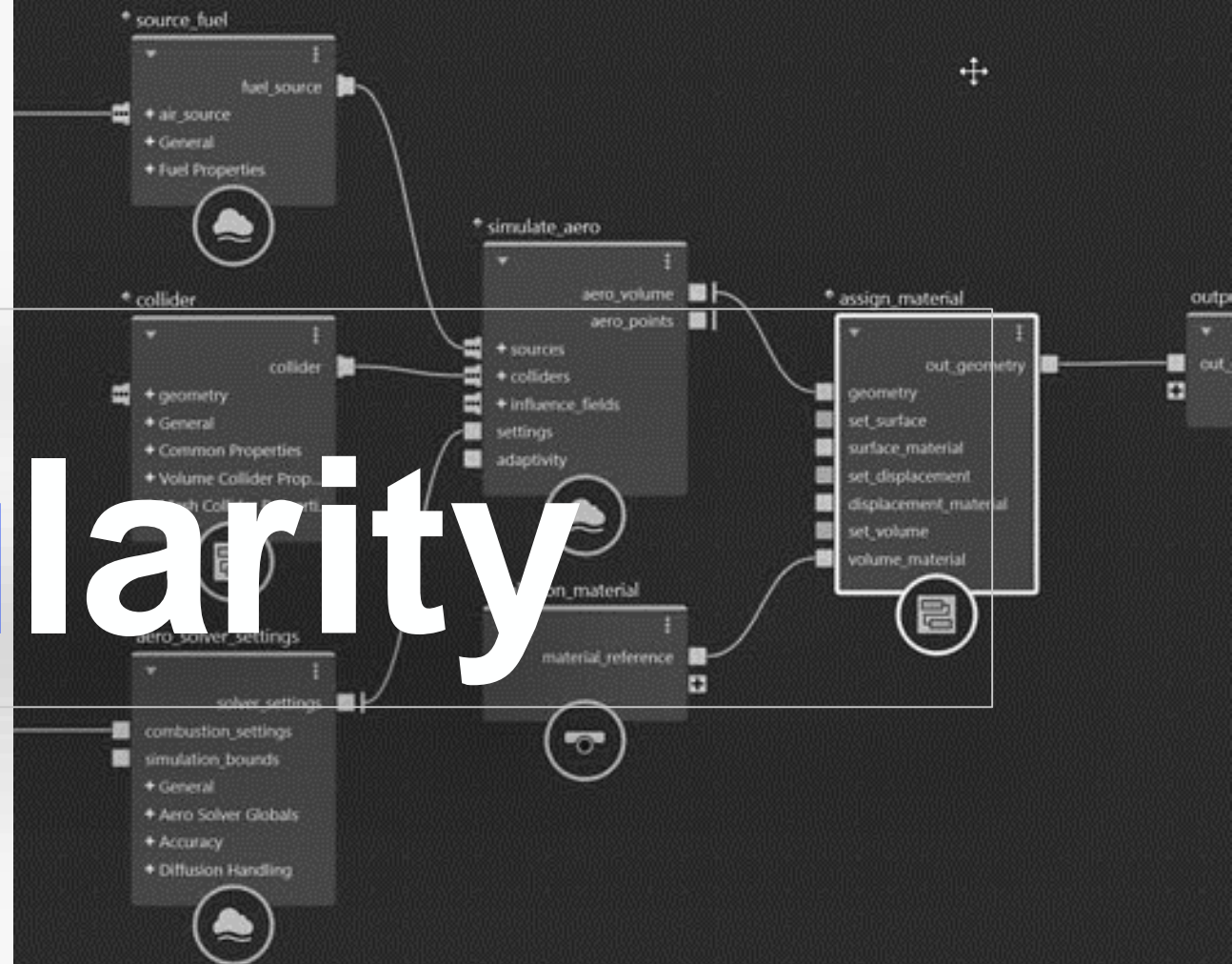
2. Passing parameters

3. Local variables and global variables

4. Functions

5. Procedures

Modularity



Problem

Combination Calculation

Find the number of combinations of p objects among n such that

$$C_n^p = \frac{n!}{p!(n-p)!}$$

```

Algorithm Calcul_Combinaison ;
Var n,p,c : integer ;
    fact_n, fact_p, fact_np: integer;
Begin
  //inputs
  Read (n,p);

  //manipulating data
  fact_n = 1;
  For i ← 1 to n Do
    fact_n ← fact_n * i;

  fact_p = 1;
  For i ← 1 à p Do
    fact_p ← fact_p * i;

  fact_np = 1;
  For i ← 1 à (n-p) Do
    fact_np ← fact_np * i;

  c ← fact_n/(fact_p*fact_np);

  //outputs
  Write ('number of combinations=',c);
End.

```



Problem

Repeating
the
factorial
calculation

```
fact_n = 1;  
For i ← 1 to n Do  
    fact_n ← fact_n * i;
```

```
fact_p = 1;  
For i ← 1 to p Do  
    fact_p ← fact_p * i;
```

```
fact_np = 1;  
For i ← 1 to n-p Do  
    fact_np ← fact_np * i;
```



How to
write the
solution
only once?
Organize
the code?

Modules / Subprograms



Definition

- ✓ A **subprogram** or module is a set of instructions with a well-defined interface that performs a specific task.
- ✓ The purpose of a subroutine is:
 1. Receive input data
 2. Carry out processing/transformation of this data
 3. Return one or more results
- ✓ The **interface** consists of the inputs/outputs of the module. It makes it possible to establish the link between the module and its environment (main algorithm, other modules).



Subprograms

Structure



Type that depends on the output

Type of Subprograms

0 to n inputs

name_sub_programs

0 to n outputs

Role of Sub-Program

unique and meaningful **name** that is used in the declaration and appeal

Role that indicates what exactly the subroutine does

Modularity

Types

✓ Depending on the number and type of outputs, there are two (02) types of Subprograms (modules):

1. Function : When the module returns a **single (1)** result and this result is **elementary** (basic) type data, example:

- Function that calculates the sum of an array of integers (return ***an integer***)
- Function that checks if a number is prime (return ***a boolean***)

2. Procedure : When the module returns **0 to n** results or the result is of **structured** type, examples:

- Procedure that displays a matrix (return ***0 result***)
- Procedure solves a 2nd degree equation (return ***2 results***)
- Procedure that reverses the content of an array (return ***an array***)



Qualities

- ✓ In order to decide whether a sequence of instructions deserves to be designed in the form of a subroutine or module, the following qualities must be checked:
 1. **Reuse**: a module is designed so that it can be **reused** in several solutions. It must be **generalized** as much as possible.
 2. **Independence**: avoid using global variables in a module so that it is **independent** of the main algorithm. Same thing for reads and writes.
 3. **Simplicity**: keep your code **readable** and design a module that meets a **specific task**.



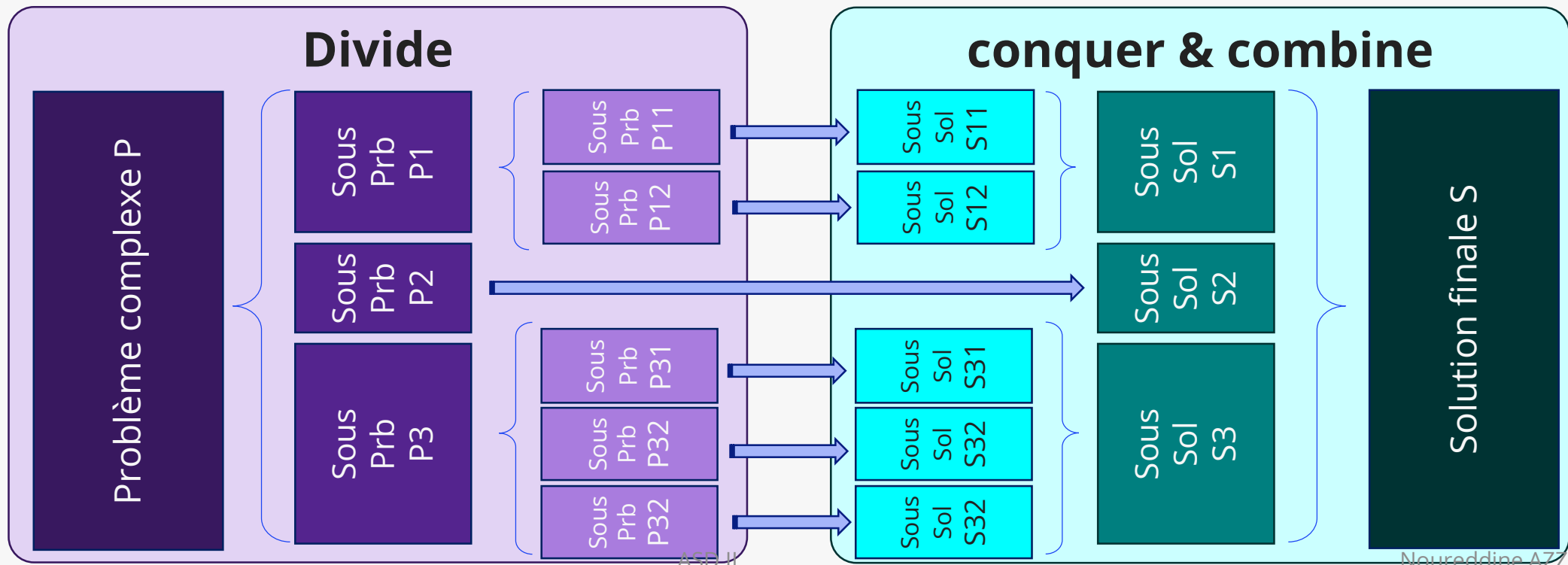
Definitions

- ✓ **Modularity**: “It is a way of thinking aimed at building algorithms starting from a very general level and gradually detailing each treatment, until arriving at the lowest level of description.”
- ✓ **Modularity**: is a **Top-down Analysis** which **divides** (cuts) a problem into sub-problems to **conquer** them then **combine** the sub-solutions and obtain an overall result.
- ✓ **Modularity**: the basis of **structured programming** consists of solving a problem by building simple, readable and reusable **modules**.



Objectifs / Goals

- ✓ Cut (divide) a complex problem into simple sub-problems which will be solved separately.
- ✓ Propose a solution to a (sub)problem once and only once



Modular Approach Stages

1st STEP:
Understanding
the problem

2nd STEP: Analysis
and Design

- Modular Cutting/Split
- Construction of Modules

3rd STEP:
Realization



Modular Breaking/Splitting

- ✓ Break the problem into coherent modules:
 - ❑ Start extracting obvious modules that are easy to detect.
 - ❑ Improve and enrich the breakdown as you progress in solving the problem



Build Modules

- ✓ To build a module, we start with its description:
 - Draw the Module
 - Give it a name
 - Define your interface
 - Specify its nature (function or procedure)
 - Indicate its role
- ✓ If the module already exists, we do not build it. Its description is given only

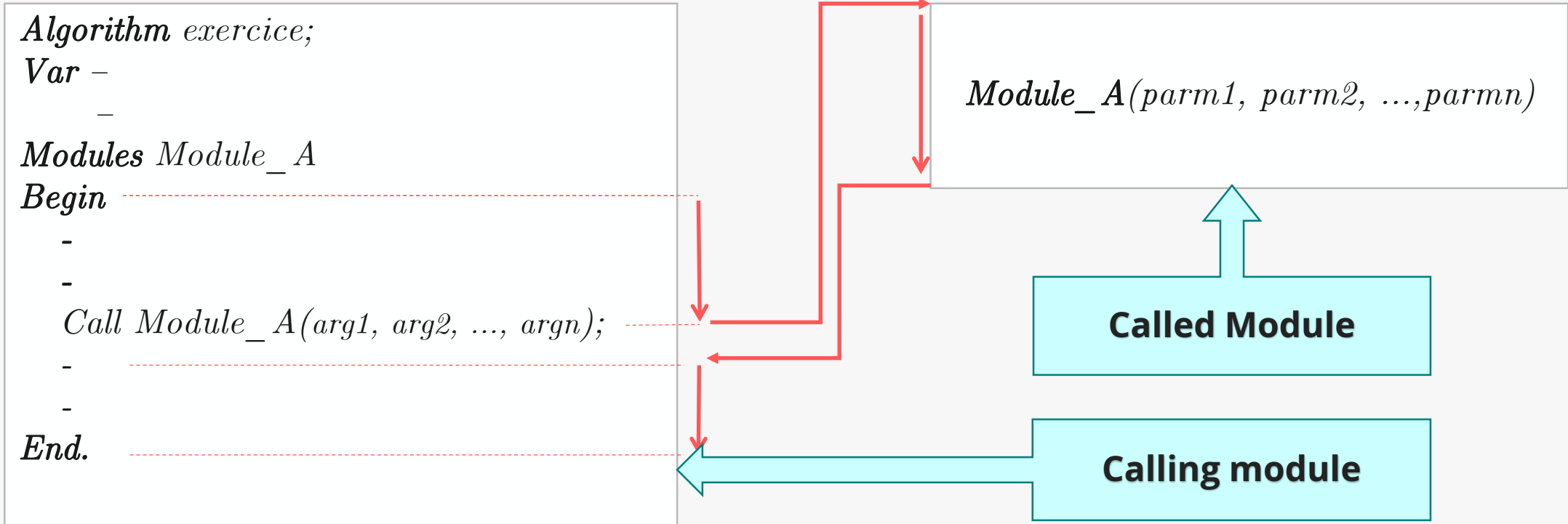


Avantages / Benefits

- ✓ Cutting into coherent modules is done using a Top-Down Approach
- ✓ Simplifies design
- ✓ Independent and separate construction of modules
- ✓ Readability and ease of understanding of algorithms
- ✓ Ease of maintenance and code updating
- ✓ Reuse of modules (Subprograms) already designed



Communication between Modules



- ✓ When a **call** to a module is encountered,
 - ❑ Suspend the execution of the **calling module** (For example: Main algorithm)
 - ❑ Start and run the **called module** (For example: Module_A)
 - ❑ Resume execution of the calling module just after the calling instruction

Parameters and Arguments

- ✓ The variables used during the construction of the module (subroutine header) are called **Parameters** or **formal parameters**
 - ❑ **Example** : les paramètres (ou paramètre formels) du module « **Module_A** » sont :
parm1, parm2, ..., parm_n
- ✓ The variables used when calling (using) a module are called **Effective parameters** or **arguments**. They replace the formal parameters during the call.
 - ❑ **Example** : les arguments (ou paramètre effectifs) du module « **Module_A** » utilisés dans son appel à l'algorithme principale sont : *arg1, arg2, ..., arg_n*
- ✓ The **number** of arguments must match the number of parameters.
- ✓ The **order** of arguments must match the order of parameters.
- ✓ The **type** of the k_{th} argument must match the type of the k_{th} parameter.
- ✓ The correspondence between arguments and parameters is done using the **order**.

Parameters Passing Modes

- ✓ It is the **substitution** of **formal** parameters by an **effective** parameters when calling a subprogram.
- ✓ On distingue deux mode de passage :
 - ❑ **Passing by Value**: Any modification of the content of the parameter in the called program has no effect on the value of the effective parameter in the calling program.
 - ❑ **Passing by Variable (by Reference)**: any modification of the content of the formal parameter automatically results in the modification of the effective parameter.
- ✓ formal parameters passed by variable are preceded by the keyword **VAR** in the header of the

type_ module nom_fonction (Formal input parameters; VAR Formal output parameters);

Passing Parameters

Passing by Value

- ✓ Copy the argument values to the start of the subprogram.
 - ✓ This is in fact an assignment of the values of the arguments in the associated formal parameters.
 - ✓ Can receive any expression (constant, variable, expression, function call, etc.)
 - ✓ Peut recevoir n'importe qu'elle expression (constant, variable, expression, appel de fonct ...)
- ❑ **Example** subroutine (function) which calculate the area of a rectangle.

```
surf ← Surface (x, y);
```

Call

equivalent to

Module

```
Function Surface(long, larg:real):real;
Var    S: integer;
Begin
  S ← long * larg;
  Surface ← S;
End;
```

```
Function Surface(long, larg:real): real;
Var    S: integer;
Begin
  long ← x; larg ← y;
  S ← long * larg;
  Surface ← S;
End;
```

Passing Parameters

Passing by Variable

- ✓ In passing by variable (or reference) the parameter itself becomes the argument,
- ✓ that is, the parameter becomes an alias of the argument.
- ✓ Can only be linked to variables..
 - ❑ **Example** : subroutine (procedure) which swaps (exchanges) the values of two variables..

Echange (a, b);

Call

équivalent à

Module

```

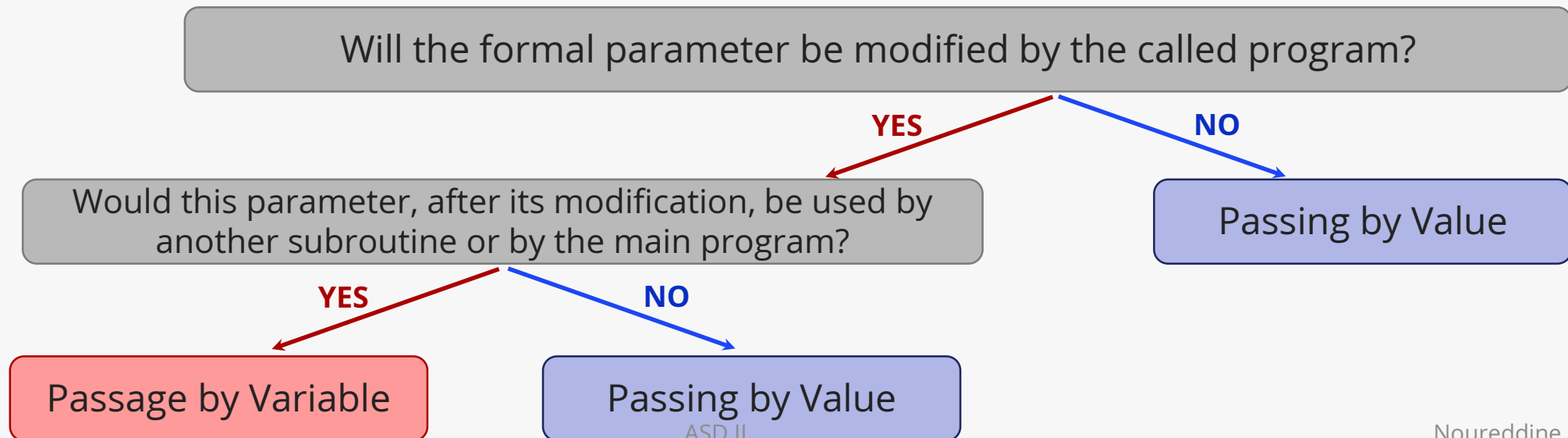
Procedure Echange(VAR x, y:integer);
  Var      z: integer;
  Begin
    z ← x;
    x ← y;
    y ← z;
  End;
  
```

```

Procedure Echange(VAR x, y: integer);
  Var      z: integer;
  Begin
    z ← a;
    a ← b;
    b ← z;
  End;
  
```

Params Passing Modes

- **Passing by Value**: is adopted when we want the module to return the **same value** that the parameter had at the input, or the parameter **is not used** in other modules (useless to find the final result).
- **Passage by Variable (by Reference)**: is adopted when the input parameter **is modified** during the execution of a subroutine and it is the **modified content** of the parameter that we want.



Notes

- It is recommended to use:
- A **passing by values** for the **input** parameters of a **function**.
- A **passing per variable** for all the **output** parameters of a **procedure**.

Local Variables and Global Variables

There are two categories of variables:

- **Local Variables**: which are defined in a module and which can only be manipulated in this module.
 - **Global Variables**: which are defined in a calling module and can be manipulated in this module and in all modules called by this module.
- ❑ **The scope**: of a variable is the set of modules where this variable is accessible (or defined).

Local Variables and Global Variables

Module_Apellant

Var A, B, X: real;

Module_1

Var X: integer;

T: boolean;

Module_2

Var C: integer;

Module_3

Var X, Y, Z: integer;

Begin

-

-

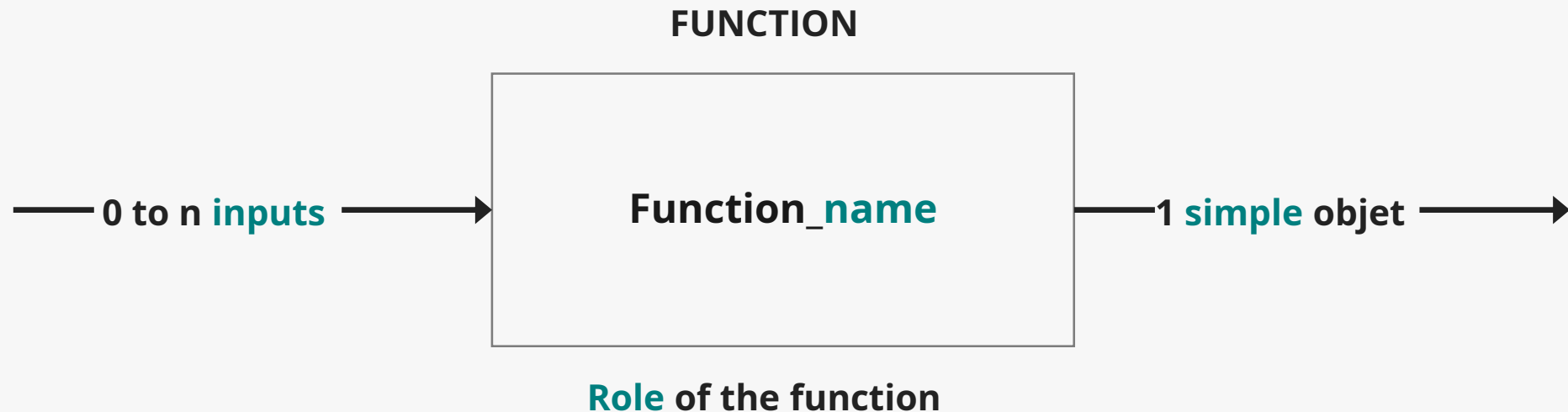
End;

Variable	Scope (Portée)
A,B	Module_Apellant , Module_1, Module_2, Module_3
T	Module_1, Module_2
C	Module_2
X:déclaré au Module_Apellant	Module_Apellant
X:déclaré au Module_1	Module_1, Module_2
X:déclaré au Module_3	Module_3
Y, Z	Module_3

Functions

Definition and Description

- ✓ A function is a sub-programme (subroutine or module) which returns a **single result** (single output) of **simple** (elementary) type: integer, real, boolean, character. It can receive **0 to n input parameters**.



Description of a fuonction

Structure and Syntax

Header

Function *fonction_name* (*List of formal input parameters :Type*): *Return Type*;

Type – { *Déclaration des*
Const – { *données (objets)*
Var – { *locales* }

Body

Begin

-

-

-

-

-

{ *Traitements* }

- *fonction_name* ← *Result*;

End;

Properties & Notes

- ✓ The body of a function can contain all **declarations** (Type, Const, Var, etc.) and algorithmic **structures** (Assignment, Repetition, Conditional, etc.).
- ✓ The calculated result (return value) must be **passed in the function name**. This assignment is located – in most cases – at the end of the function.
- ✓ **Formal parameters** describe the input parameters used in the function as well as their **type** and their passing **mode**.
- ✓ In Functions, formal parameters are used in **passing-by-value** mode.

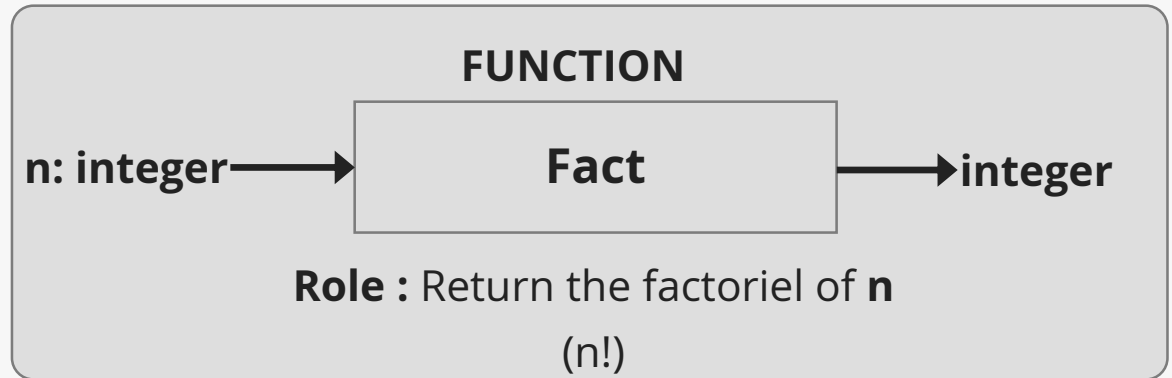
Calls

- ✓ Calling a function can be used as:
 - ❑ *Expression* in an **assignment**,
 - ❑ *Operand* in a **condition**
 - ❑ *Argument* in a **procedure** or **function call**
- ✓ **Examples:**
 - ❑ $X \leftarrow \text{Prime}(a)$
 - ❑ `if Prime (a) = True then write (a, 'is prime')`
 - ❑ $\text{Res} \leftarrow \text{Prime}(\text{Fact}(n))$

1st Step : Split Modules

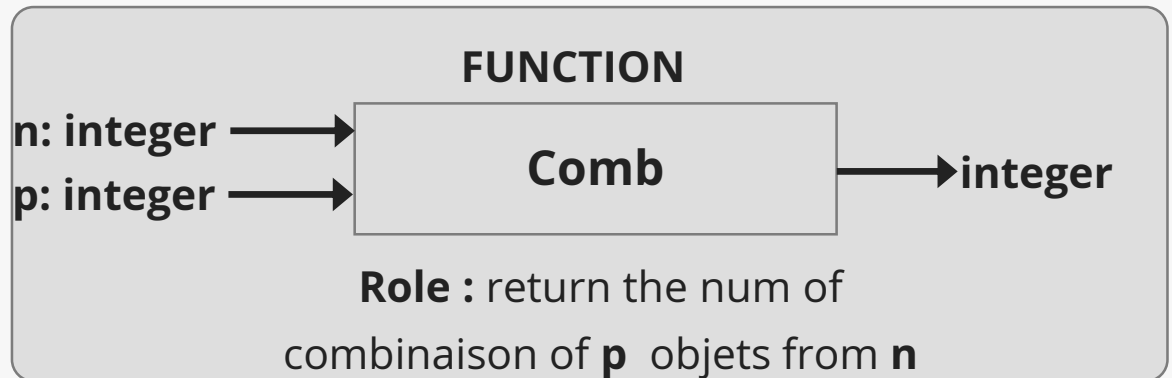
Function : Fact

$$\begin{aligned} \text{Fact}(n) &= n! \\ &= n*(n-1)*\dots*3*2*1 \end{aligned}$$



Function : Comb

$$\begin{aligned} \text{Comb}(n,p) &= C_n^p = \frac{n!}{p!*(n-p)!} \\ &= \text{Fact}(n)/\text{Fact}(p)*\text{Fact}(n-p) \end{aligned}$$



2nd Step: Construction of modules

```
Function Fact (n: integer): integer;  
Var F, i: integer;  
Begin  
  F ← 1;  
  for i ← 1 to n Do  
    F ← F * i;  
  
  Fact ← F;  
End;
```

```
Function Comb (n , p: integer): integer;  
Functions : Fact;  
Begin  
  Comb ← Fact(n)/ Fact(p)* Fact(n-p);  
End;
```

3rd Step: Main Algorithm

```
Algorithm Calcul_comb;  
Var          x,y,c: integer;  
Functions : Comb;  
Begin  
  Read(x,y);  
  c ← Comb(x,y);  
  Write ('Le nombre de combinaison = ', c);  
End;
```

Function declaration

PASCAL

```
FUNCTION nom_fonction (Input parameters): type_retour;  
var      { Déclaration des données locales }  
begin  
  -      { Instructions }  
  -  
  -  
  nom_fonction ← valeur_retour;  
fin;
```

```
function Fact(n: integer) : integer;  
  var F,i : integer;  
  begin  
    F := 1;  
    for i := 2 to n do  
      F := F*i;  
    Fact := F;  
  end;
```

C

```
type_retour nom_fonction (Input parameters)  
{  
  { Déclaration des données locales }  
  - { Instructions }  
  -  
  -  
  -  
  return valeur_retour;  
}
```

```
int Fact (int n)  
{  
  int F , i;  
  F = 1;  
  for (i=2; i<=n; i++){  
    F = F*i;  
  }  
  return F;  
}
```

Function declaration

PASCAL

- ✓ In PASCAL, Functions and procedures must be declared **before** the main program.
- ✓ In general, each called module must be constructed **before** the calling module for it to be **recognized**.
- ✓ In this example:
 - ❑ A **Call** to a Fact function (line 17)
 - ❑ **n**: **parameter** (**formal** parameter) (line 5)
 - ❑ **x**: **argument** (**effective** parameter)(line 17)

```
1 program factoriel;  
2 uses Crt;  
3 var x : integer;  
4  
5 function Fact(n: integer) : integer;  
6 var F,i : integer;  
7 begin  
8     F := 1;  
9     for i := 2 to n do  
10        F := F*i;  
11  
12        Fact := F;  
13     end;  
14  
15 begin  
16     Readln(x);  
17     Writeln(x, '! =', Fact(x));  
18 end.
```

Function declaration

C

- ✓ In C language, Functions and procedures can be declared **before** and **after** the *main* function.
- ✓ If the function is placed **before** the *main*, the compiler checks the parameters and executes the function.
- ✓ If the function is placed **after** the *main*, we need to define a **prototype** of the function for it to be recognized.

```

1  #include <stdio.h>
2
3  int Fact (int n)
4  {
5      int F , i;
6      F = 1;
7      for (i=2; i<=n; i++){
8          F = F*i;
9      }
10
11     return F;
12 }
13
14 int main()
15 {
16     int x;
17     scanf("%d", &x);
18     printf("%d! = %d", x, Fact(x));
19
20     return 0;
21 }

```

Function declaration

C

- ✓ **A prototype** is a function declaration so that it can be used (called) even before it is coded.
- ✓ The prototype is placed at the **beginning of the program** (just after the libraries declaration).
- ✓ A prototype is declared as a function

type_retour nom_fonction (Input parameters)

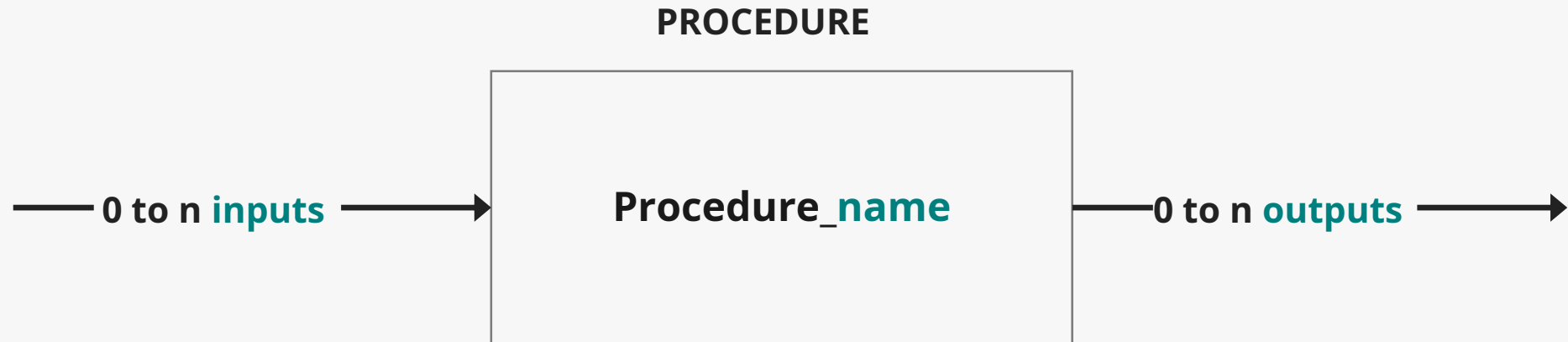
```
1  #include <stdio.h>
2
3  int Fact (int n);
4
5  int main()
6  {
7      int x;
8      scanf("%d", &x);
9      printf("%d! = %d", x, Fact(x));
10
11     return 0;
12 }
13
14 int Fact (int n)
15 {
16     int F , i;
17     F = 1;
18     for (i=2; i<=n; i++){
19         F = F*i;
20     }
21
22     return F;
23 }
```

Procedures

```
17 string sInput;  
18 int iLength, iN;  
19 double dblTemp;  
20 bool again = true;  
21  
22 while (again) {  
23     iN = -1;  
24     again = false;  
25     getline(cin, sInput);  
26     system("cls");  
27     stringstream(sInput) >> dblTemp;  
28     iLength = sInput.length();  
29     if (iLength < 4) {  
30         again = true;  
31         continue;  
32     } else if (sInput[iLength - 3] !=  
33         '0') {  
34         again = true;  
35         continue;  
36     } while (++iN < iLength) {  
37         if (isdigit(sInput[iN])) {  
38             continue;  
39         } else if (iN == (iLength - 3) &&  
40             sInput[iN] != '0') {  
41             again = true;  
42             continue;  
43         }  
44     }  
45     if (iN < 0) {  
46         again = true;  
47         continue;  
48     }  
49     if (iN > iLength) {  
50         again = true;  
51         continue;  
52     }  
53     if (iN < 0 || iN > iLength) {  
54         again = true;  
55         continue;  
56     }  
57     if (iN < 0 || iN > iLength) {  
58         again = true;  
59         continue;  
60     }  
61     if (iN < 0 || iN > iLength) {  
62         again = true;  
63         continue;  
64     }  
65     if (iN < 0 || iN > iLength) {  
66         again = true;  
67         continue;  
68     }  
69     if (iN < 0 || iN > iLength) {  
70         again = true;  
71         continue;  
72     }  
73     if (iN < 0 || iN > iLength) {  
74         again = true;  
75         continue;  
76     }  
77     if (iN < 0 || iN > iLength) {  
78         again = true;  
79         continue;  
80     }  
81     if (iN < 0 || iN > iLength) {  
82         again = true;  
83         continue;  
84     }  
85     if (iN < 0 || iN > iLength) {  
86         again = true;  
87         continue;  
88     }  
89     if (iN < 0 || iN > iLength) {  
90         again = true;  
91         continue;  
92     }  
93     if (iN < 0 || iN > iLength) {  
94         again = true;  
95         continue;  
96     }  
97     if (iN < 0 || iN > iLength) {  
98         again = true;  
99         continue;  
100    }
```

Definition and Description

- ✓ A procedure is a sous-programme (subroutine or module) which returns 0 to n results (multiple output) of simple or compound type. It can receive 0 to n input parameters.



Role of the procédure

Description of a procedure

Structure & Syntax

Header

Procedure *procedure_name* (*List of formels input and output parameters :Type*);

Type – { *Déclaration des données (objets) locales* }

Const – { }

Var – { }

Body

Begin

- { *Traitements* }

-

-

-

-

End;

Properties & Notes

- ✓ The body of a procedure can contain all **declarations** (Type, Const, Var, etc.) and algorithmic **structures** (Assignment, Repetition, Conditional, etc.).
- ✓ The **formal parameters** describe the **input** and **output** parameters used in the procedure as well as their **type** and their **passing mode**.
- ✓ In Procedures, formal **output** parameters must always be described in a **passing-by-variable** mode.

Calls

- ✓ Calling a procedure is a **primitive action**. It is composed of the name of the procedure followed in parentheses by the list of effective input and output parameters separated by commas.
- ✓ As for functions, the **number**, **order**, and **type** of the effective parameters must be identical to those of the formal parameters.
- ✓ **Examples:**
 - ❑ `remplir_tab (n, T)`
 - ❑ `echange (x, y)`

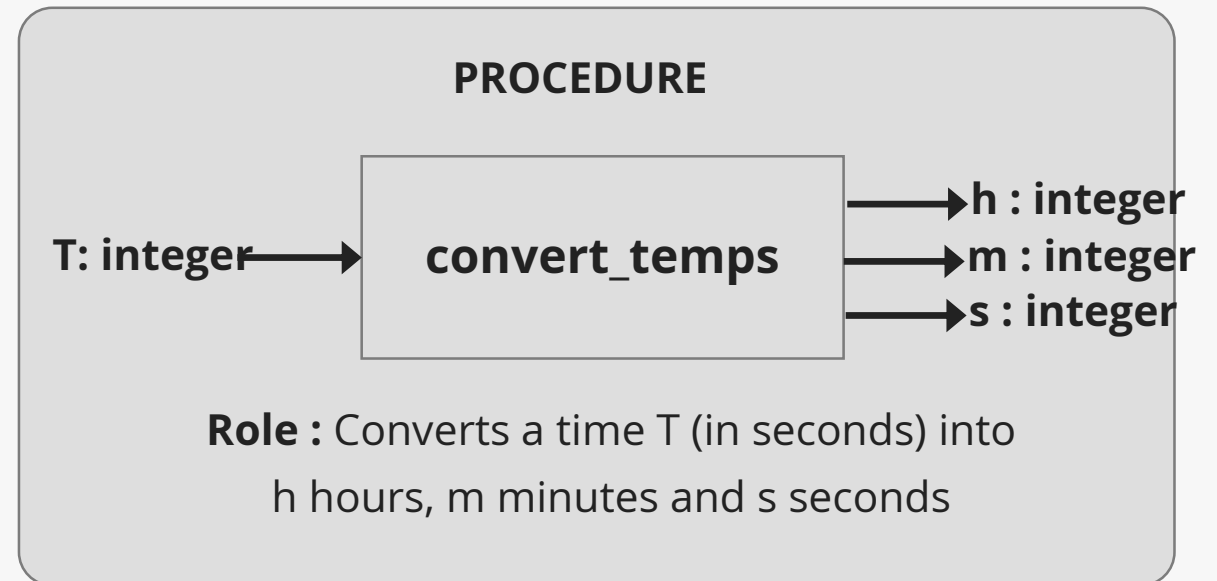
Example: Convert a time T (in seconds) to hours, minutes and seconds

1st Step : Split Modules

Procedure: `convert_temps`

`convert_temps (T, h, m, s)`

1. On divise T sur 360 : le quotient est h
2. Le reste de cette division est divisé sur 60
 - a. Le quotient est m
 - b. Le reste est s



Example: Convert a time T (in seconds) to hours, minutes and seconds

2nd Step: Construction of modules

```
Procedure convert_temps (T: integer; VAR h, m, s : integer);  
Var      R: integer;  
Begin  
    h ← T DIV 3600;  
    R ← T MOD 3600;  
    m ← R DIV 60;  
    s ← R MOD 60;  
End;
```

3rd Step: Main Algorithm

```
Algorithm Convert;  
Var          A, x, y, z: integer;  
Procedures : convert_temps;  
Begin  
  Read(A);  
  convert_temps(A, x, y, z);  
  Write (A, '=', x, 'heures et ', y, ' minutes et ', z, 'secondes');  
End;
```

Exemple: Convertir un temps T (en secondes) en heures, minutes et secondes

PASCAL

C

```
PROCEDURE nom_procedure (Input/output parameters);  
var { Déclaration des données locales }  
begin  
- { Instructions }  
-  
-  
fin;
```

```
void nom_fonction (Input/output parameters)  
{  
- { Déclaration des données locales }  
- { Instructions }  
-  
-  
}
```

```
procedure convert_temps(T: integer; VAR h,m,s: integer);  
var R : integer;  
begin  
  h := T DIV 3600;  
  R := T MOD 3600;  
  m := R DIV 60;  
  s := R MOD 60;  
end;
```

```
void convert_temps (int T, int *h, int *m, int *s)  
{  
  int R;  
  
  *h = T / 3600;  
  R = T % 3600;  
  *m = R / 60;  
  *s = R % 60;  
}
```

Declaration of a Procedure

PASCAL

- ✓ Dans cet exemple:
 - ❑ Un *Appel* d'une procédure convert_temps (ligne 5)
 - ❑ T : *paramètre* (paramètre *formel* d'entrée) (ligne 5)
 - ❑ h,m,s : *paramètre* (paramètre *formel* de sortie) (ligne 5)
 - ❑ A : *argument* (paramètre *effectif* d'entrée (ligne 17)
 - ❑ x,y,z : *argument* (paramètre *effectif* de sortie (ligne 17)

```

1 program Convert;
2 uses Crt;
3 var A,x,y,z : integer;
4
5 procedure convert_temps(T: integer; VAR h,m,s: integer);
6   var R : integer;
7   begin
8     h := T DIV 3600;
9     R := T MOD 3600;
10    m := R DIV 60;
11    s := R MOD 60;
12  end;
13
14 begin
15   Readln(A);
16   convert_temps(A, x, y, z);
17   Writeln(A, '=', x, 'heures et ', y, ' minutes et ', z, 'secondes');
18 end.

```

Declaration of a Procedure

C

- ✓ In C language, the return type of procedures is specified as *void*.
- ✓ When declaring the procedure, formal output parameters are preceded by ***.
- ✓ When calling this procedure, the effective output parameters are preceded by *&*.

```
1 #include <stdio.h>
2
3 void convert_temps (int T, int *h, int *m, int *s);
4
5 int main()
6 {
7     int A, x, y, z;
8     scanf("%d", &A);
9     convert_temps(A, &x, &y, &z);
10    printf("%d = %d heures et %d minutes et %d secondes", A, x, y, z);
11
12    return 0;
13 }
14
15 void convert_temps (int T, int *h, int *m, int *s)
16 {
17     int R;
18
19     *h = T / 3600;
20     R = T % 3600;
21     *m = R / 60;
22     *s = R % 60;
23 }
```

Exercice 12 : Soit la suite : 1, 11, 21, 1112, 3112,

On voudrait afficher les N premiers éléments ?