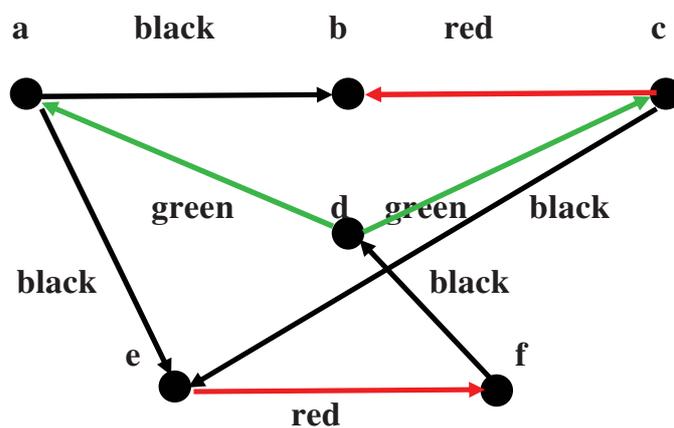


## Tutorial Session (5)

### Exercise 1:

Let  $G$  the following graph:



1. Decompose the cycle  $(a, d, c, e, f, d, a)$  into elementary cycles.
2. Decompose the cocycle  $\omega(\{a, d, f\})$  into elementary cocycles.
3. Determine whether the arc  $(a, b)$ , colored in black, belongs to an elementary circuit or to an elementary cocircuit.
4. Calculate the cyclomatic number  $\nu(G)$ .
5. How many edges must be removed from graph  $G$  to transform it into a tree?
6. Give the spanning tree  $T$  of  $G$ .
7. Give the cotree  $T^*$  associated with  $T$ .
8. Give a cycle basis for the graph  $G$ .

9. Give the vectors associated with each cycle of the basis.
10. Calculate the cocyclomatic number  $\lambda(\mathbf{G})$ .
11. Give a cocycle basis for the graph  $\mathbf{G}$ .
12. Give the vectors associated with each cocycle of the basis.

**Exercise 2:**

Show that the multigraphs  $\mathbf{K}_{3,3}$  and  $\mathbf{K}_5$  are not planar.

**Exercise 3:**

Represent the arithmetic expression  $(\mathbf{e}^x - \mathbf{y}) * (\mathbf{c} + \mathbf{d} / \mathbf{z}) + 4$  in the form of a tree, respecting the rules of operator precedence.